INFOB3CC: Concurrency EXAM 3 16 April 2020, 09:00 – 11:00

Please read the following instructions carefully:

- This exam is to be completed at home
- Enter your results using the template provided. Submit your solutions on blackboard.
- The template contains further information regarding the rules and regulations for this exam. Please read these regulations and type your name and date in the space provided to acknowledge that you have read and accept these rules.
- A maximum of 93 points can be obtained by answering the questions of this exam, to be divided by 9.3 to obtain the final mark.
- Provide brief and concise answers. Overly verbose responses or nonsense added to otherwise good answers can deduct from your grade.
- If a question does not give you all the details you need, you may make reasonable assumptions. Your assumptions must be clearly stated. If your solution only works under certain conditions, state them.
- Read through the paper first and plan your time accordingly.
- Good luck! (:

Question	Points	Score
Polynomials	15	
Furniture shop (1)	25	
Furniture shop (2)	23	
Epidemiology	30	
Total:	93	

Polynomials

1. A polynomial p of degree n is an expression in the form:

$$p(x) = a_0 + a_1 x + a_2 x^2 + a_3 x^3 + \dots + a_n x^n$$

where we can store the polynomial coefficients a in an array of size n + 1.

- (a) (5 points) To add two polynomials a and b to a new polynomial c, it suffices to add the coefficients such that $c_i = a_i + b_i$. Give a parallel algorithm that calculates the sum of two polynomials with the lowest possible work and span. Motivate your response.
- (b) (5 points) Melinda discovers that you can multiply two polynomials of degree n-1 by making four independent multiplications of degree $\frac{n}{2} 1$ and three polynomial additions of degree n. Analyse the work and span of Mel's algorithm.
- (c) (5 points) Sara tells Melinda that the product can also be calculated by six additions of degree n-1 and three independent multiplications of degree $\frac{n}{2}-1$. Analyse the work and span of Sara's algorithm.

Furniture shop (1)

- 2. A large furniture company wants to develop an application to manage the stock in their warehouse. This will be used to check which products are in stock. Each product consists of one or multiple part. A part may also be used for different products. For instance, different tables may use the same legs, as seen in these example products:
 - Table Utrecht
 - $-1 \times \text{tabletop oak}$
 - 4 \times oak leg
 - Table Amsterdam
 - $-1 \times \text{tabletop oak}$
 - 2 \times steel leg
 - Table Amersfoort
 - $-1 \times \text{tabletop glass}$
 - $-2 \times \text{steel leg}$

In this database, we have three different products (three tables), which are built from four different parts (two kinds of tabletops, two kinds of table legs).

The application keeps track of the number of each part is in stock. When making a new order, the system should check the stock of each part, and if everything is in stock, decrease the stock count of the used parts.

- (a) (5 points) The system should handle multiple orders in parallel. Alex proposes to use a single lock for the whole database. Explain why this is a bad idea.
- (b) (5 points) Billy suggests to use a lock per part. When ordering a product, we acquire the lock of each part of that product, in the same order as listed in the product description. We verify the stock of each part and if everything is in stock, decrease the stock counts. Finally we release all the locks.

Using the following product database, demonstrate an execute sequence where this method would fail:

- Wardrobe Australia
 - $-1 \times \text{frame}$
 - $-1 \times door$
 - $-1 \times$ clothes rail
- Wardrobe New Zealand
 - $-1 \times drawer$
 - $-1 \times \text{frame}$
 - $-1 \times door$
- Wardrobe accessories
 - $-1 \times \text{clothes rail}$
 - $-1 \times drawer$
- (c) (5 points) How should a product database be constructed to prevent these issues?
- (d) (5 points) Consider the following product database:
 - Couch Neptune
 - $-1 \times \text{seat module (small)}$
 - $-1 \times \text{seat module (large)}$
 - Couch Mars

- $-1 \times \text{seat module (small)}$
- Couch Venus
 - $-1 \times \text{seat module (large)}$

The couches Mars and Venus are ordered very frequently. Omar is afraid that it could occur that handling orders of couch Mars are blocked for a long time, because an order containing couch Neptune is busy for a long time.

Which general property of locks should hold, to prevent this situation? Explain why this situation cannot occur when that property holds.

(e) (5 points) An MVar can be empty or contain a value. Ivar says that you can use this to implement the locks. The stock counts will be stored in a value of type MVar Int per part, where the Int is the actual stock count. Explain how this can be done and how the empty state and blocking functions make this easy to implement.

Furniture shop (2)

3. To further increase the capacity of the system, the furniture shop considers to use data parallelism to process orders in bulk. Instead of checking the stock level for each product one at a time, the system will now check whether every part for every product of the entire order is in stock at once.

In the following questions answer using the data parallel operations discussed in the course (map, zipWith, fold, scan1, scanr, permute, backpermute, and stenci1). Nested data parallelism is not allowed. Write code in Haskell.

(a) (8 points) An order is given as an array of products. Write a function which computes an array of the parts required to fulfil the order.

You may use n(i) to denote the number of parts required for product *i*, and f(i,k) to denote the *k*-th part of item *i*, where $0 \le k < n(i)$.

- (b) (5 points) Given an array of parts required for an order, we need to compute the total number of each part which is required. Write a function which computes an array such that the value at index *i* of the array contains the count of the number of parts of kind *i* required for this order.
- (c) (5 points) Given the output of the previous question, and an array containing the current stock level for every part in the warehouse, where both are represented as an array where the *i*-th element denotes the count for parts of kind *i*. Write a function which determines whether everything for the order is in stock.
- (d) (5 points) If all of the parts are in stock for the order, how can we compute the new stock levels, after reserving the parts required for this order?

Epidemiology

4. The scale and connectivity of the global air travel network increases the risk for infectious diseases to spread. Epidemic control measures can be applied to air travel networks to minimise the risk of large-scale contagion. In order to design the most effective outbreak control measures, we must build a model of the dynamics of infection which can then be used to evaluate the impact of various outbreak control policies.

We will use an SIR model¹ to represent the evolution of an outbreak in a given population over time, using a set of differential equations specifying the proportion of the population in each possible state an individual can assume: susceptible (S), infected (I), and recovered (R). We have the following discrete form equations:

$$S_{i,t+1} = S_{i,t} - \frac{\beta_i I_{i,t} S_{i,t}}{N_{i,t}} + \sum_{j \in \theta(i)} S_{ji,t} - \sum_{j \in \theta(i)} S_{ij,t}$$
(12)

$$I_{i,t+1} = I_{i,t} + \frac{\beta_i I_{i,t} S_{i,t}}{N_{i,t}} - \gamma I_{i,t} + \sum_{j \in \theta(i)} I_{ji,t} - \sum_{j \in \theta(i)} I_{ij,t}$$
(13)

$$R_{i,t+1} = R_{i,t} + \gamma I_{i,t} + \sum_{j \in \theta(i)} R_{ji,t} - \sum_{j \in \theta(i)} R_{ij,t}$$
(14)

where $\theta(i)$ is the set of nodes (cities) which have a direct connection to node i, β is the probability of contact between a susceptible and an infected person causing infection, and γ the proportion of infected people recovering per day (the inverse of this value is the number of days it takes for an infected individual to recover). In this question we consider the spread of influenza, for which we can treat these last two terms as constants: $\beta = 0.15$ and $\gamma = 1/7$.

For example, equation (12) says that the number of susceptible individuals in city i at time t+1 is given by the number of susceptible individuals at time t (first term), minus the number of susceptible individuals which became infected through contact with an infected individual (second term), then modified by the number of susceptible individuals entering (third term) and leaving (fourth term) the city.

In the following questions you will implement this model using the data parallel operations discussed in the course (map, zipWith, fold, scan1, scanr, permute, backpermute, and stenci1). Nested data parallelism is not allowed. Write code in Haskell.

(a) (6 points) At each time step t, the number of individuals in each category (S, I, and R) is modified by the rate at which individuals travel between cities. We can model this with an $N \times N$ adjacency matrix travelFlows, where the value at index Z :. j :. i represents the number of passengers traveling from city i to city j, where $0 \le i < N$ and $0 \le j < N$.

Give a function which computes in data parallel:

- i the total number of individuals departing each city
- ii the total number of individuals arriving at each city
- (b) (9 points) Given a vector N (the total population at each node i) and vectors S, I, and R containing the current number of individuals in each category respectively at time t, write a function to compute in data parallel each of the vectors S, I, and R at time t + 1.
- (c) (5 points) The *infection attack rate* is the percentage of the population which contracts the disease in an at-risk population during a specified time interval. Write a function to compute in data parallel the attack rate at each city for a given time step.
- (d) (5 points) In order to model the dynamics of the infection, we iteratively apply equations (12)–(14). You are given matrices S', I', and R' containing the number of individuals in each category for every time step of the simulation. Write a function to compute in data parallel the *peak prevalence* of the infection in each city.

¹Chen, Nathan, Rey, David, and Gardner, Lauren. Multiscale Network Model for Evaluating Global Outbreak Control Strategies. In *Journal of the Transporation Research Board*, 2017. http://dx.doi.org/10.3141/2626-06

(e) (5 points) Infectious disease spread is an example of exponential growth because the number of cases on a given day is proportional to the number of cases in the previous day. However, exponential growth like this can not continue forever, and must start slowing down at some point. Given the matrices S', I', and R' from the previous question, write a function to compute in data parallel the inflection point of the curve, the time t at which the growth factor first drops to (at or below) one.

THERE ARE NO MORE QUESTIONS

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