# **B3CC: Concurrency** *13: Data Parallelism (2)*

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- Single point of concurrency
- 
- Good cost model (work & span): conceptually very simple!
- BUT! the "something" has to be sequential

• Data parallelism: well understood & supported approach to massive parallelism

- Easy to implement: well supported (Fortran, MPI, OpenMP…), scales to large number of processors, etc.

 $parallel_f$ or (i = 1..N) { // ... do something to xs[i] }





- The map operation applies the *same* function to each element of a set
	- This is a parallelisation of a loop with a *fixed* number of iterations
	- and/or index

- There must not be any dependencies between loop iterations: the function uses only the input element value







- A map with access to the neighbourhood around each element
	- The set of neighbours is fixed, and relative to the element
	- Ubiquitous in scientific, engineering, and image processing algorithms



### **Data parallelism on CPUs**

- Distribute work via
	- Static schedule (like count & list mode of IBAN)
	- fork-join
	- divide-and-conquer (like search mode of IBAN)

 $\cdots$ 





# **Data parallelism on GPUs**

- A GPU program consists of the kernel that runs on the GPU
	- Kernel functions are executed *n* times in parallel by *n* different threads
	- Each thread executes the same sequential program
	- Each thread can distinguish itself from all others *only* by it's thread identifier
		- Any information a thread needs should be directly derivable from this ID

```
\{ if ( idx < n ) { 
       / do something
 } 
}
```
- \_global\_ void kernel( float\* xs, float\* ys, int n, ...)
	- int idx =  $blockDim.x * blockIdx.x + threadIdx.x;$



# **More parallel patterns**

- We have seen:
	- Map
	- Stencil
- We will discuss today and next time:
	- Gather or backwards permute: random reads
	- Scatter or permutation: random writes
	- Fold or reduction: combined value of all items
	- Scan prefix sum: at each index, combined value of all prior elements

### **Gather**

- The *gather* pattern performs independent random *reads* in parallel
	- Also known as a *backwards permutation*
	- Collects all the data from a source array at the given locations



<https://hackage.haskell.org/package/accelerate-1.3.0.0/docs/Data-Array-Accelerate.html#g:29> 8



### **Gather**

- The *gather* pattern performs independent random *reads* in parallel
	- Requires a function from output index to input index
	- Not all input values have to be read
	- Some values may be read twice
	- Input and output may have different dimensions









### **Example: matrix transpose**



• Transpose rows and columns of a matrix

### **Example: matrix transpose**

• Transpose the rows and columns of a matrix

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```
transpose :: Elt a \Rightarrow Acc (Matrix a) \rightarrow Acc (Matrix a)
transpose xs = 
   let I2 rows cols = shape xs 
   in backpermute (I2 cols rows) (\(I2 y x) \rightarrow I2 x y) xs
{
   int idx = blockDim.x * blockIdx.x + threadIdx.x; if ( idx < n ) { 
       int row = idx / rows; 
       int col = idx % cols; 
 .
 } 
}
```
\_\_global\_\_ void transpose( float\* xs, float\* ys, int rows, int cols)

### **Example: matrix transpose**







• In memory, this is stored as:



• To write one row of the output, we read one column of the input

### **Example: matrix transpose**



$$
\begin{array}{|c|c|c|c|}\n\hline\n1 & 2 & 3 & 4 \\
\hline\n5 & 6 & 7 & 8 \\
\hline\n9 & 10 & 11 & 12\n\end{array}
$$







- The memory access pattern for transpose is not ideal
	- On the CPU work in tiles to improve cache behaviour
	- On the GPU use shared memory explicitly to do coalesced reads & writes

# **Example: matrix vector multiply**

- The *dense* matrix-vector multiply
	- Perform a dot-product of each row of the matrix against the vector
	- Can be parallelised in different ways

```
for (r = 0; r < rows; +r) {
 result[r] = 0;for (c = 0; c < cols; +c) {
    / dot product of this row with the vector
   result[r] += matrix[r][c] * vector[c]; } 
}
```










- Multiply a *sparse* matrix by a dense vector
	- Example: Hardesty3 dataset
		- Matrix size is 8.2M x 7.6M
		- Only 40M non-zero entries (0.000065%)
	- Want to store only the non-zero entries, as only these will contribute to the result
	- Together with the row/column index of each element (various encodings possible)





- Store matrix in *compressed sparse row* format (CSR)
	- Stores only the non-zero elements together with their column index
	- Also need the number of non-zero elements in each row

 $[(0, 1.0), (1, 1.0), (1, 7.0), (2, 3.0), (3, 2.0)]$ 1 1 0 0 0



- Store matrix in *compressed sparse row* format (CSR)
	- Stores only the non-zero elements together with their column index
	- Also need the number of non-zero elements in each row







• Store matrix in *compressed sparse row* format (CSR)

- The sparse-matrix dense-vector multiply is then:
	- 1. *gather* the values from the input vector at the column indices
	- 2. pair-wise multiply (1) with the matrix values (*zipWith*)
	- 3. segmented *reduction* of (2) with the matrix segment descriptor
		- *- … more on reductions and segmented operations next time!*

indices [ 0, 1, 1, 2, 3, 1, 3, 4 ] segment descriptor [ 2, 3, 0, 1, 2 ] values [ 1.0, 1.0, 7.0, 3.0, 2.0, 1.0, 3.0, 3.0 ]





<https://github.com/tmcdonell/accelerate-examples/tree/master/examples/smvm> 21



• This can be viewed as a kind of *nested* data-parallel computation: parallel computations which spawn further



- parallel work
	- More difficult to parallelise (for both hardware and software)
	- Segmented operators allow us to convert nested parallel computations into *flat* parallel computations





- Gather or backwards permutation transforms indices in the *output* array to indices in the *input* array
	- But; arbitrary memory access patterns are slow (especially on the GPU)
	- Simple pattern; many common cases which can be made more efficient
- 

• Next is scatter, forward permutation, which transforms indices in the *input* array to indices in the *output* array





### **Scatter**

- The *scatter* pattern performs independent random *writes* in parallel
	- Also known as forward permutation
	- Puts data from the source array into the specified locations



<https://hackage.haskell.org/package/accelerate-1.3.0.0/docs/Data-Array-Accelerate.html#g:28> 24





- The *scatter* pattern performs independent random *writes* in parallel
	- Analogously to gather, we can consider scatter as an index mapping *f*  transforming indices in the *input* (source) array to indices in the *output* (destination) array
	- More complex than gather, especially if
		- *f* is not surjective: the range of *f* might not cover the entire codomain
		- *f* is not injective: distinct indices in the domain may map to the same index in the codomain
		- *f* is partial: elements in the domain may be ignored



- The index permutation might not cover every element in the output
	- We need to first initialise the output array







# **Collisions**

- Multiple values may map to the same output index
	- Possible strategies to handle *collisions:*
		- Disallow
		- Non-deterministically, one write succeeds
		- Merge values with a given associative and commutative operation





# **Collisions: atomic instructions**

Possible strategies to handle *collisions:*

- 1. Non-deterministically, one write succeeds
	- Requires atomic writes
	- Writes of single words are typically atomic, but that depends on architecture
- 2. Merge values with a given associative and commutative operation
	- Use an atomic read-modify-write instruction (e.g. atomic\_fetch\_add), if it exists for this operation
	- Use an atomic compare-and-swap loop, if a value is a single word
		- Maximal size of a word for compare-and-swap depends on the architecture
- 3. Use (per element) locks otherwise





# **Collisions: locks**

do { old = atomic\_exchange(&lock[i], 1);  $}$  while (old  $= 1$ );  $/*$  critical section  $*/$ 

- A general merge function might need to implement some locking strategy
	- If no atomic instruction exists; or multiple words are updated
	- Recall: this classic spin lock executed on the GPU can deadlock:



atomic\_exchange(&lock[i], 0);

# **Example: histogram**

- Computing a histogram requires merging writes to the same location
- 



<https://hackage.haskell.org/package/accelerate-1.3.0.0/docs/Data-Array-Accelerate.html#v:permute> 30



# **Example: filter (compact)**

- Return only those elements of the array which pass a predicate
	- 1. *map* the predicate function over the values to determine which to keep
	- 2. exclusive *scan* the boolean flags to determine the output locations and number of elements to keep
	- 3. *permute* the values into the position given by  $(2)$  if  $(1)$  is true

<https://hackage.haskell.org/package/accelerate-1.3.0.0/docs/Data-Array-Accelerate.html#v:filter> 31







- Due to the behaviour of caches, there is inter-core communication when threads access the same cache *line*,

- If the target locations are known in advance, scatter can be converted into a gather operation (this may require



- Scatter is more expensive than gather for a number of reasons
	- Not only to handle collisions!
	- even if there is no actual collision
	- extra processing)



### **Scatter**

- Reframing an algorithm can be key to converting scatter to gather
	- As always, there are different tradeoffs in computation vs. communication
	- Per element: scatter









- Performance is often more limited by data movement than computation
	- Transferring data across memory layers is costly
	- Data organisation and layout can help to improve locality & minimise access times
	- Design the application around the data movement
- Similar consistency issues arise as when dealing with computation parallelism
- Might involve the creation of additional intermediate data structures
- Some applications are all about data movement: searching, sorting…



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# tot ziens

