

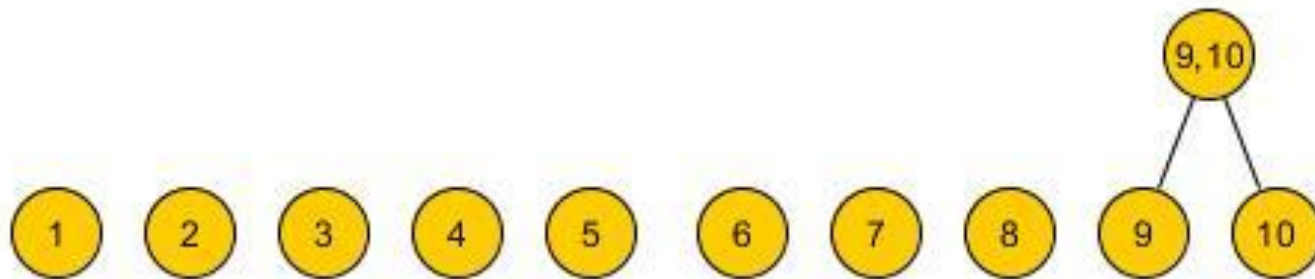
Building the Linkage Tree (LT) in LTGA

1. Start with singleton linkage sets



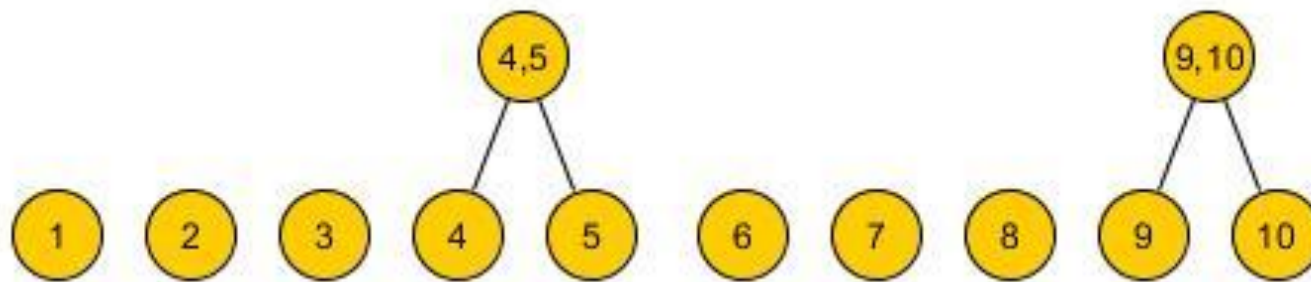
Building the Linkage Tree (LT) in LTGA

2. Compute MI for all pairs of clusters
3. Cluster 2 sets with the highest MI
4. Repeat steps 2 and 3 until 2 cluster remain



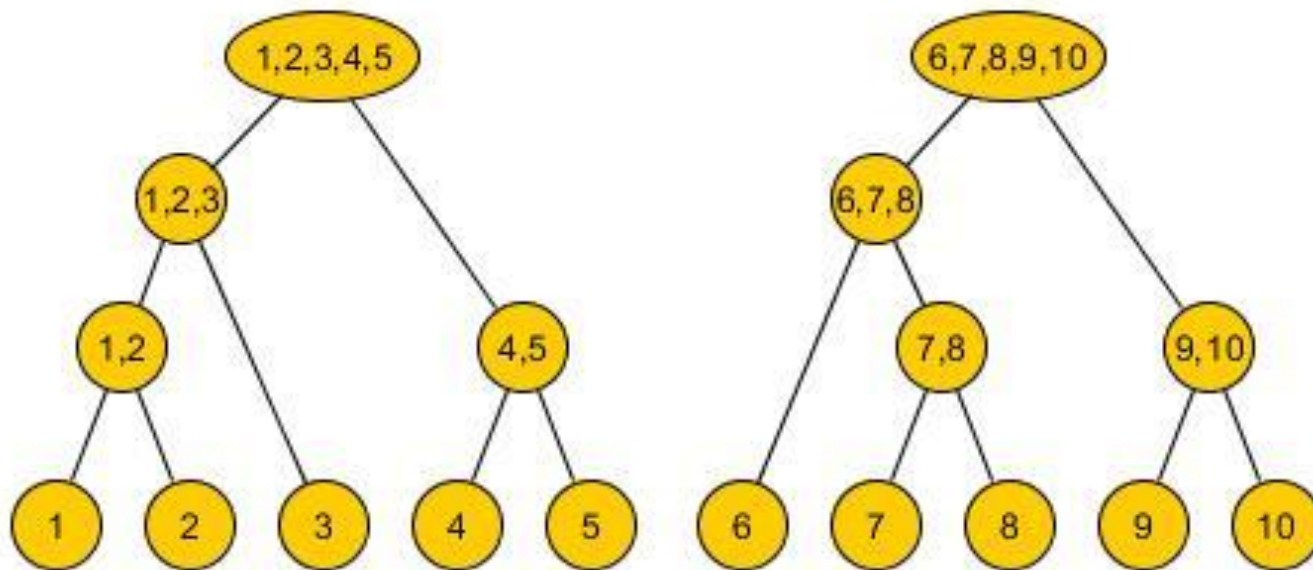
Building the Linkage Tree (LT) in LTGA

2. Compute MI for all pairs of clusters
3. Cluster 2 sets with the highest MI
4. Repeat steps 2 and 3 until 2 cluster remain



Building the Linkage Tree (LT) in LTGA

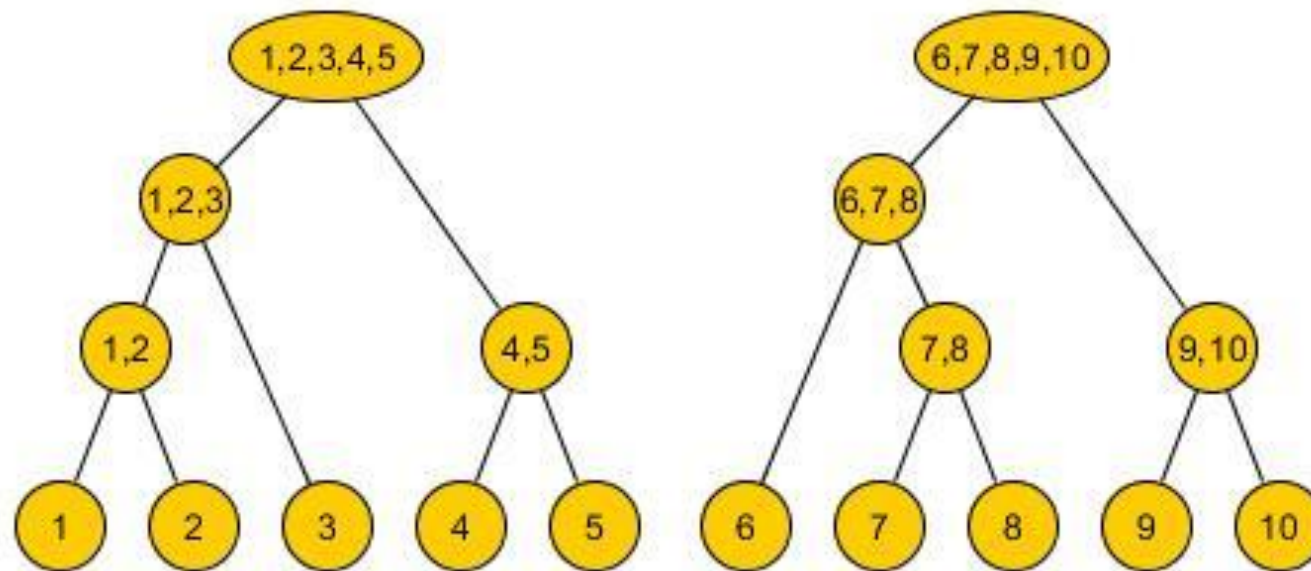
2. Compute MI for all pairs of clusters
3. Cluster 2 sets with the highest MI
4. Repeat steps 2 and 3 until 2 cluster remain



Optimal Mixing (OM) in LTGA

- ▶ For each individual p_i in the population
- ▶ Traverse all masks in the Linkage Tree

p_i	3	3	2	2	1	-1	0	0	0	0
-------	---	---	---	---	---	----	---	---	---	---



- ▶ For each mask (in reversed order of merging), randomly select a parent p from the population
- ▶ Donate values of the variables in the mask from the parent to p_i
- ▶ If this leads to an improvement, continue the search with the updated solution

p_i	3	3	2	2	1	-1	0	0	0	0
-------	---	---	---	---	---	----	---	---	---	---

Initial solution (5 mil)

+

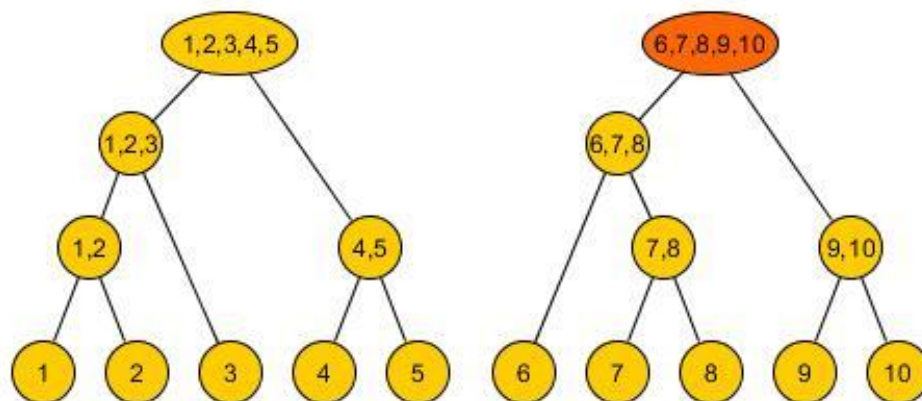
p	3	0	1	2	1	-1	0	0	2	0
-----	---	---	---	---	---	----	---	---	---	---

Random parent



o_i	3	3	2	2	1	-1	0	0	2	0
-------	---	---	---	---	---	----	---	---	---	---

Improved offspring (4.8 mil)



- ▶ For each mask (in reversed order of merging), randomly select a parent p from the population
- ▶ Donate values of the variables in the mask from the parent to p_i
- ▶ If this leads to an improvement, continue the search with the updated solution

o_i	3	3	2	2	1	-1	0	0	2	0
-------	---	---	---	---	---	----	---	---	---	---

Intermediate solution (4.8 mil)

+

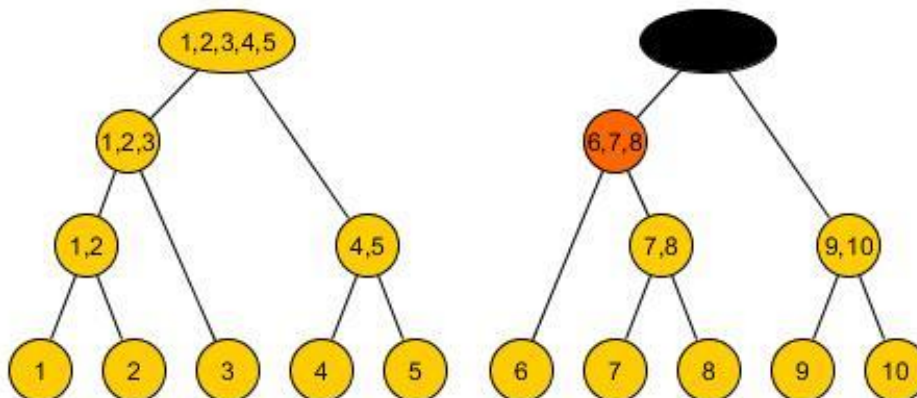
p	0	0	0	1	1	2	-2	-2	1	1
-----	---	---	---	---	---	---	----	----	---	---

Random parent



	3	3	2	2	1	2	-2	2	2	0
--	---	---	---	---	---	---	----	---	---	---

Infeasible solution



- ▶ For each mask (in reversed order of merging), randomly select a parent p from the population
- ▶ Donate values of the variables in the mask from the parent to p_i
- ▶ If this leads to an improvement, continue the search with the updated solution

o_i	3	3	2	2	1	-1	0	0	2	0
-------	---	---	---	---	---	----	---	---	---	---

Intermediate solution (4.8 mil)

+

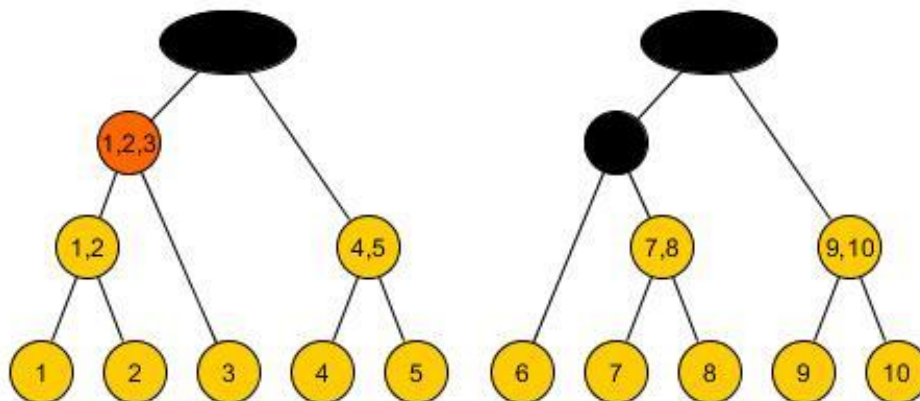
p	3	3	3	1	1	0	0	0	0	0
-----	---	---	---	---	---	---	---	---	---	---

Random parent



	3	3	3	2	1	-1	0	0	2	0
--	---	---	---	---	---	----	---	---	---	---

Worse offspring (6 mil)



- ▶ For each mask (in reversed order of merging), randomly select a parent p from the population
- ▶ Donate values of the variables in the mask from the parent to p_i
- ▶ If this leads to an improvement, continue the search with the updated solution

o_i	3	3	2	2	1	-1	0	0	2	0
-------	---	---	---	---	---	----	---	---	---	---

Intermediate solution (4.8 mil)

+

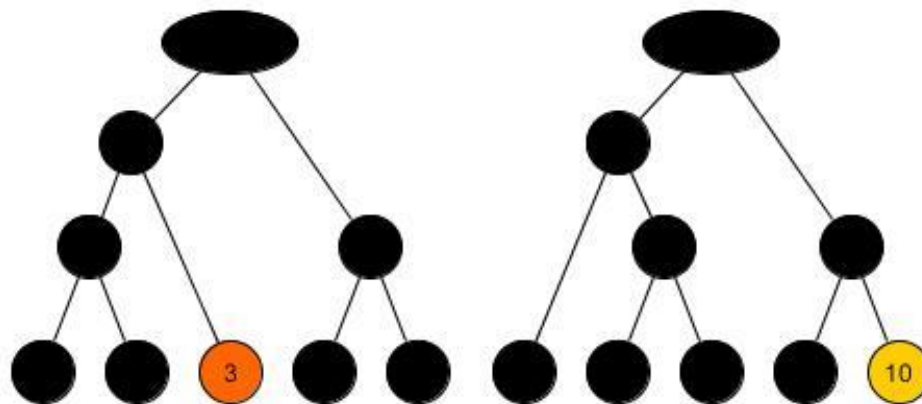
p	3	3	1	1	-1	1	2	0	1	0
-----	---	---	---	---	----	---	---	---	---	---

Random parent



o_i	3	3	1	2	1	-1	0	0	2	0
-------	---	---	---	---	---	----	---	---	---	---

Improved offspring (4 mil)



Thierens, D., & Bosman, P. A. (2011, July). Optimal mixing evolutionary algorithms. In *Proceedings of the 13th annual conference on Genetic and evolutionary computation* (pp. 617-624). ACM.

Linkage Tree Genetic Algorithm (LTGA)

```
for all  $i \in \{0, 1, \dots, n - 1\}$  do
   $\mathbb{P}_i \leftarrow \text{RANDOM SOLUTION}(n)$ 
end for
while Termination criteria not met do
5:   if  $\mathbb{F}$  not predetermined then
      $\mathbb{F} \leftarrow \text{BUILD LT}(\mathbb{P})$ 
   end if
   for all  $i \in \{0, 1, \dots, n - 1\}$  do
      $b \leftarrow o \leftarrow \mathbb{P}_i$ 
10:     $\text{fitness}[b] \leftarrow \text{fitness}[o] \leftarrow \text{fitness}[\mathbb{P}_i]$ 
     for all  $j \in \{0, 1, \dots, |\mathbb{F}| - 1\}$  do
        $p \leftarrow \text{RANDOM}(\{\mathbb{P}_0, \dots, \mathbb{P}_{n-1}\})$ 
        $o_{\mathbb{F}^i} \leftarrow p_{\mathbb{F}^i}$ 
       if  $o_{\mathbb{F}^i} \neq b_{\mathbb{F}^i}$  then
15:         $\text{EVALUATE FITNESS}(o)$ 
         if  $\text{fitness}[o] > \text{fitness}[b]$  then
            $b_{\mathbb{F}^i} \leftarrow o_{\mathbb{F}^i}$ 
            $\text{fitness}[b] \leftarrow \text{fitness}[o]$ 
         else
20:            $o_{\mathbb{F}^i} \leftarrow b_{\mathbb{F}^i}$ 
            $\text{fitness}[o] \leftarrow \text{fitness}[b]$ 
         end if
       end if
     end for
      $\mathbb{O}_i \leftarrow o$ 
25:   end for
    $\mathbb{P} \leftarrow \text{TOURNAMENT SELECTION}(\mathbb{O}, n, 2)$ 
end while
```
