

EXAM FUNCTIONAL PROGRAMMING

Tuesday the 30th of September 2014, 11.00 h. - 13.00 h.

Name:

Student number:

Before you begin: Do not forget to write down your name and student number above. If necessary, explain your answers (in English or Dutch). For multiple choice questions, clearly circle what you think is the (one and only) best answer. Use the empty boxes under the other questions to write your answer and explanations in; if you run out of space, you can use the empty sixth page of the exam. Use the empty paper provided with this exam only as scratch paper (kladpapier). At the end of the exam, only hand in the filled-in exam paper. Answers will not only be judged for correctness, but also for clarity and conciseness. A total of one hundred points can be obtained; divide by 10 to obtain your grade. Good luck!

In any of your answers below you may (but do not have to) use the following well-known Haskell functions/operators: *id*, *concat*, *foldr* (and variants), *map*, *filter*, *const*, *flip*, *fst*, *snd*, *not*, *(.)*, *elem*, *take*, *drop*, *takeWhile*, *dropWhile*, *head*, *tail*, *(++)*, *lookup* and all members of the type classes *Eq*, *Num*, *Ord*, *Show* and *Read*.

- (i) Write a function *intersperse* $:: a \rightarrow [a] \rightarrow [a]$, which places its first argument between the elements of its second argument; i.e. *intersperse* 'a' "xyz" should return "xayaz". You *must* use direct recursion.

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- (ii) Give an alternative definition of *intersperse* without direct recursion, using higher-order functions.

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- (i) Write a function $sumIntTrie :: Trie Int \rightarrow Int$ that adds all the payloads (of type Int) together. For example, $sumIntTrie (Leaf\ 3)$, should return 3, and $sumIntTrie\ ex$ should return 100.

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- (ii) Write a function $searchTrie :: [Char] \rightarrow Trie\ a \rightarrow Maybe\ a$, that follows a path down the tree as indicated by the first argument, and just returns the payload of the *branch or leaf* it reaches in this way, and *Nothing* otherwise. For example, $searchTrie []\ ex$ gives *Just 40*, $searchTrie ['b']\ ex$ gives *Just 30*, $searchTrie ['b', 'a']\ ex$ returns *Just 3*, and $searchTrie ['b', 'a', 'h']\ ex$ returns *Nothing*. Here you may use a function $lookup :: Char \rightarrow [(Char, b)] \rightarrow Maybe\ b$ such that $lookup\ c\ ps$ returns v if (c, v) is the first pair in ps in which c is the first component, and *Nothing* if no such pair exists.

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- (iii) A problem with the definition of $Trie$ is that the type system does not forbid values like $Branch\ 45 [('a', Leaf\ 33), ('a', Leaf\ 78)]$. Give a definition for $Trie\ a$ that does not have that problem.

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4. .../20 The following multiple choice questions are each worth 5 points.

(i) Let f be any function of type $Int \rightarrow Int$. Which expression has the same value as the following list comprehension?

$[f\ x \mid x \leftarrow [1..6],\ even\ x]$

- a. $map\ f\ (filter\ even\ [1..6])$
- b. $filter\ even\ (map\ f\ [1..6])$
- c. $f\ (map\ even\ [1..6])$
- d. $filter\ f\ (map\ even\ [1..6])$

(ii) Given is the following unnecessarily complicated function definition:

$$\begin{aligned} f\ g &= f\ 0\ g \\ \mathbf{where}\ f\ g\ h \mid g < length\ h &= foldr\ (const\ (+1))\ 0\ (h\ !!\ g) + f\ (g + 1)\ h \\ &\mid otherwise &= 0 \\ const\ f\ g &= f \end{aligned}$$

Which of the following implementations is equivalent?

- a. $sum\ .\ map\ length$
- b. $foldr\ (+)\ 0\ .\ map\ (const\ 1)$
- c. $foldr\ ((+)\ length)\ 0$
- d. $foldl1\ (+)\ .\ map\ length$

(iii) I Both function application and the \rightarrow in function types associate to the left so that Currying becomes possible.

II Function application has precedence over all operators.

- a. Both I and II are true
- b. Only I is true
- c. Only II is true
- d. Both I and II are false

(iv) What is the type of $map\ .\ foldr$?

- a. $(a \rightarrow a \rightarrow a) \rightarrow [a] \rightarrow [[a] \rightarrow a]$
- b. $(a \rightarrow a \rightarrow a) \rightarrow [b] \rightarrow [b \rightarrow a]$
- c. $(b \rightarrow a \rightarrow a) \rightarrow [b] \rightarrow [[a] \rightarrow a]$
- d. $(b \rightarrow a \rightarrow a) \rightarrow [a] \rightarrow [[b] \rightarrow a]$

5. (i) Explain why the expression $\lambda x \rightarrow (x \text{ '1'}, x \text{ '1'})$ is type incorrect.

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- (ii) Determine the type of *map filter*. You should not just write down the type below, but also explain how you arrived at that type (for example, in the way that this is done in the lecture notes of this course).

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