

INFOGR – Computer Graphics

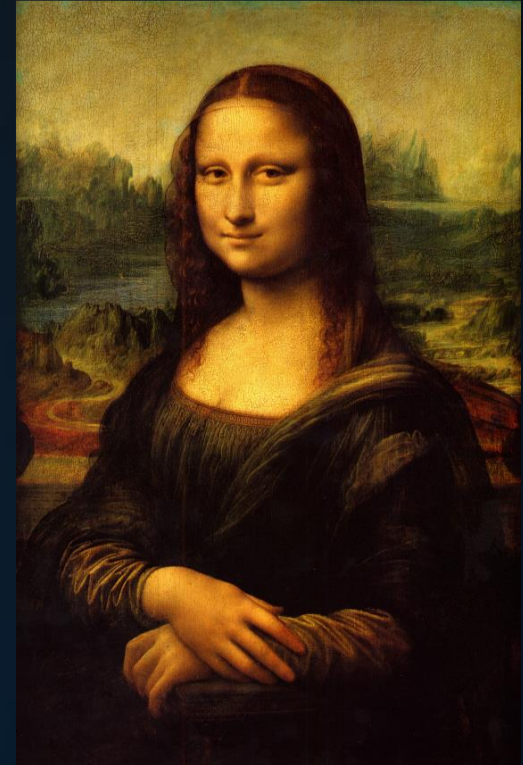
J. Bikker - April-July 2015 - Lecture 9: “Shading Models”

Welcome!



Today's Agenda:

- Introduction
- Light Sources
- Materials
- Sensors
- Shading



Introduction

The Quest for (Photo-)Realism

- Objective in modern games
- Important improvements when using ray tracing (more in the next lecture, ‘ground truth’)

The core algorithms of ray tracing and rasterization model light transport (with or without visibility):

$$L(p \rightarrow r) = L_e(p \rightarrow r) + \sum_{i=1}^{N_L} L(q_i \rightarrow p) f_r(q_i \rightarrow p \rightarrow r) G(q_i \leftrightarrow p)$$

Other factors:

- Material interactions
- Light models
- Sensor models



Introduction

Material interactions



Introduction

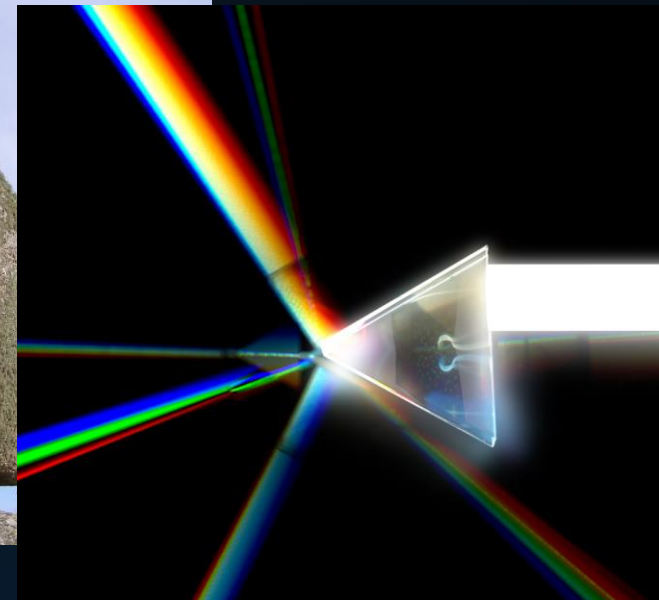
Material interactions

```
rics  
& (depth < MAXD  
t = inside / 1.5  
nt = nt / nc; add  
os2t = 1.0f - nnt  
D, N );  
)  
at a = nt - nc; b  
at Tr = 1 - (R0 +  
Tr) R = (D * nnt  
E * diffuse;  
= true;  
efl + refr)) && (  
D, N );  
-refl * E * diffus  
= true;  
MAXDEPTH)  
survive = Surviva  
estimation - doi  
if;  
-radiance = Sample  
e.x + radiance.y
```

```
v = true;  
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive  
at3 factor = diffuse * INVPI;  
at weight = Mis2( directPdf, brdfPdf );  
at cosThetaOut = dot( N, L );  
E * ((weight * cosThetaOut) / directPdf) * (radiance
```

andom walk - done properly, closely following well-known
rive)

```
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );  
survive;  
pdf;  
n = E * brdf * (dot( N, R ) / pdf);  
sion = true;
```



Introduction

Material interactions

```
rics  
& (depth < MAXD
```

```
t = inside / 1.0  
nt = nt / nc; add  
os2t = 1.0f - nnt
```

```
D, N );  
)
```

```
at a = nt -  
at Tr = 1 -  
Tr) R = (D
```

```
E * diffuse  
= true;
```

```
efl + refr)
```

```
D, N );  
-refl * E *  
= true;
```

```
MAXDEPTH)
```

```
survive = S  
estimation  
if;
```

```
-radiance =  
e.x + radia
```

```
v = true;  
at brdfPdf
```

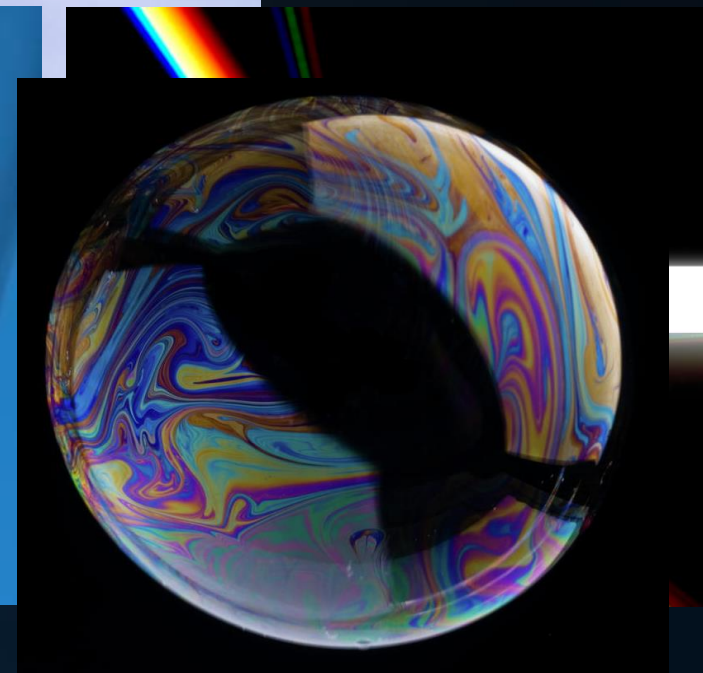
```
at3 factor = diffuse * INVPI;  
at weight = Mis2( directPdf, brdfPdf );
```

```
at cosThetaOut = dot( N, L );  
E * ((weight * cosThetaOut) / directPdf) * (radiance
```

```
andom walk - done properly, closely following walls  
ive)
```

```
;
```

```
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );  
survive;  
pdf;  
n = E * brdf * (dot( N, R ) / pdf);  
ision = true;
```



Introduction

Light models

```
...ics
& (depth < MAXDEPTH)
{
    // Inside / Outside
    int nt = nt / nc; nnt = nnt / nc;
    float cos2t = 1.0f - nnt;
    float D, N;
    // ...
    float a = nt - nc, b = nt;
    float Tr = 1 - (R0 + (1 - R0) * a);
    float R = (D * nnt - N * a);
    // ...
    E * diffuse;
    // ...
    refl + refr)) && (depth <
    D, N);
    refl * E * diffuse;
    // ...
    MAXDEPTH)
    survive = SurvivalProbability(
    estimation - doing it pr
    ff;
    radiance = SampleLight( &
    e.x + radiance.y + radiance
    v = true;
    at brdfPdf = EvaluateDiffuse(
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Monte Carlo
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```



Introduction

Light models

```
...ics
& (depth < MAXD);

... = inside / 1.5;
nt = nt / nc; rdd = ...
os2t = 1.0f - nnt; ...
D, N );
)

... at a = nt - nc; b = nt;
... at Tr = 1 - (R0 + (1 - R0
... Tr) R = (D * nnt - N * (a
...

... E * diffuse;
... = true;

... efl + refr)) && (depth <
... D, N );
... efl * E * diffuse;
... = true;

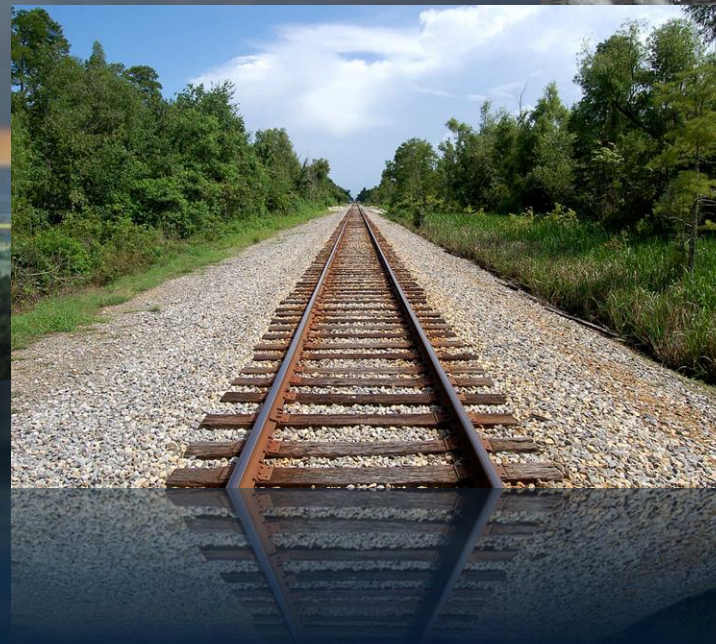
... MAXDEPTH)

... survive = SurvivalProbabl
... estimation - doing it pr
... ff;
... radiance = SampleLight( &
... e.x + radiance.y + radian

... v = true;
... at brdfPdf = EvaluateDiff
... at3 factor = diffuse * INVPI;
... at weight = Mis2( directPdf, brdfPdf );
... at cosThetaOut = dot( N, L );
... E * ((weight * cosThetaOut) / directPdf) * (radiance

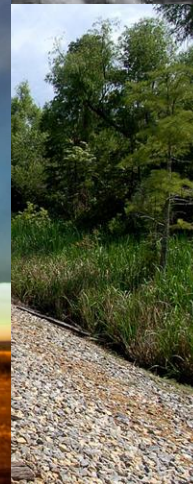
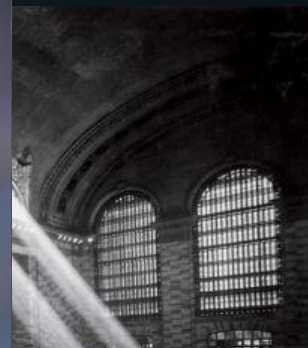
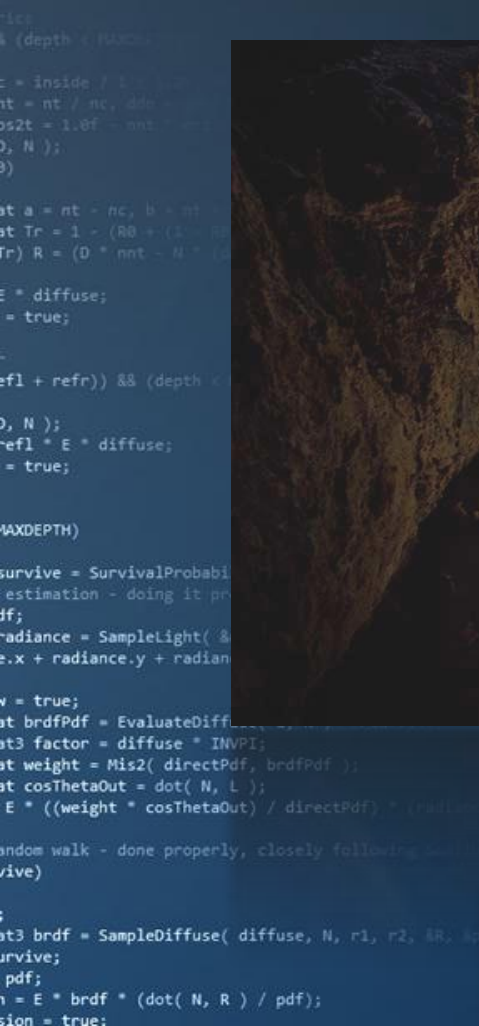
... random walk - done properly, closely following ...
... rive)

...
... at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
... survive;
... pdf;
... n = E * brdf * (dot( N, R ) / pdf);
... sion = true;
```



Introduction

Light models



Introduction

Light models

```
...ics
& (depth < MAXD);

...t = inside / 1.0;
nt = nt / nc; dde = ...
os2t = 1.0f - nnt; ...
D, N );
)

...at a = nt - nc, b = nt - nc;
at Tr = 1 - (R0 + (1 - R0) * ...
Tr) R = (D * nnt - N * (20

...E * diffuse;
= true;

...efl + refr)) && (depth < MAXDEPTH)

D, N );
-refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse, ...
estimation - doing it properly, closely
ff;
-radiance = SampleLight( &rand, I, &t, &ll
e.x + radiance.y + radiance.z) > 0) && (e

v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * P_xxxxxx
at3 factor = diffuse * INVPI;
at weight = Mix2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance

random walk - done properly, closely following walls (survive)
ive)

;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
```

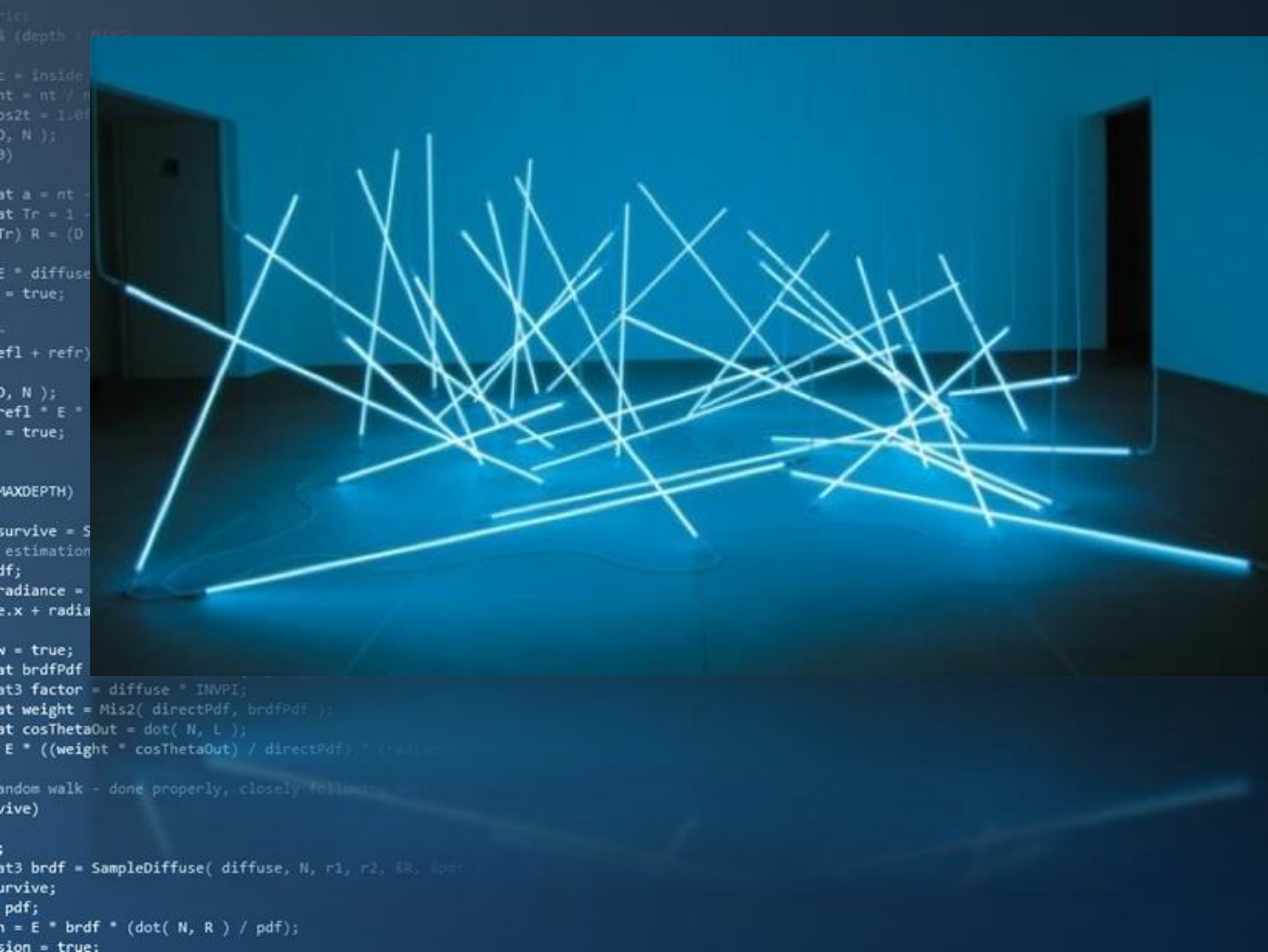


Light models



Introduction

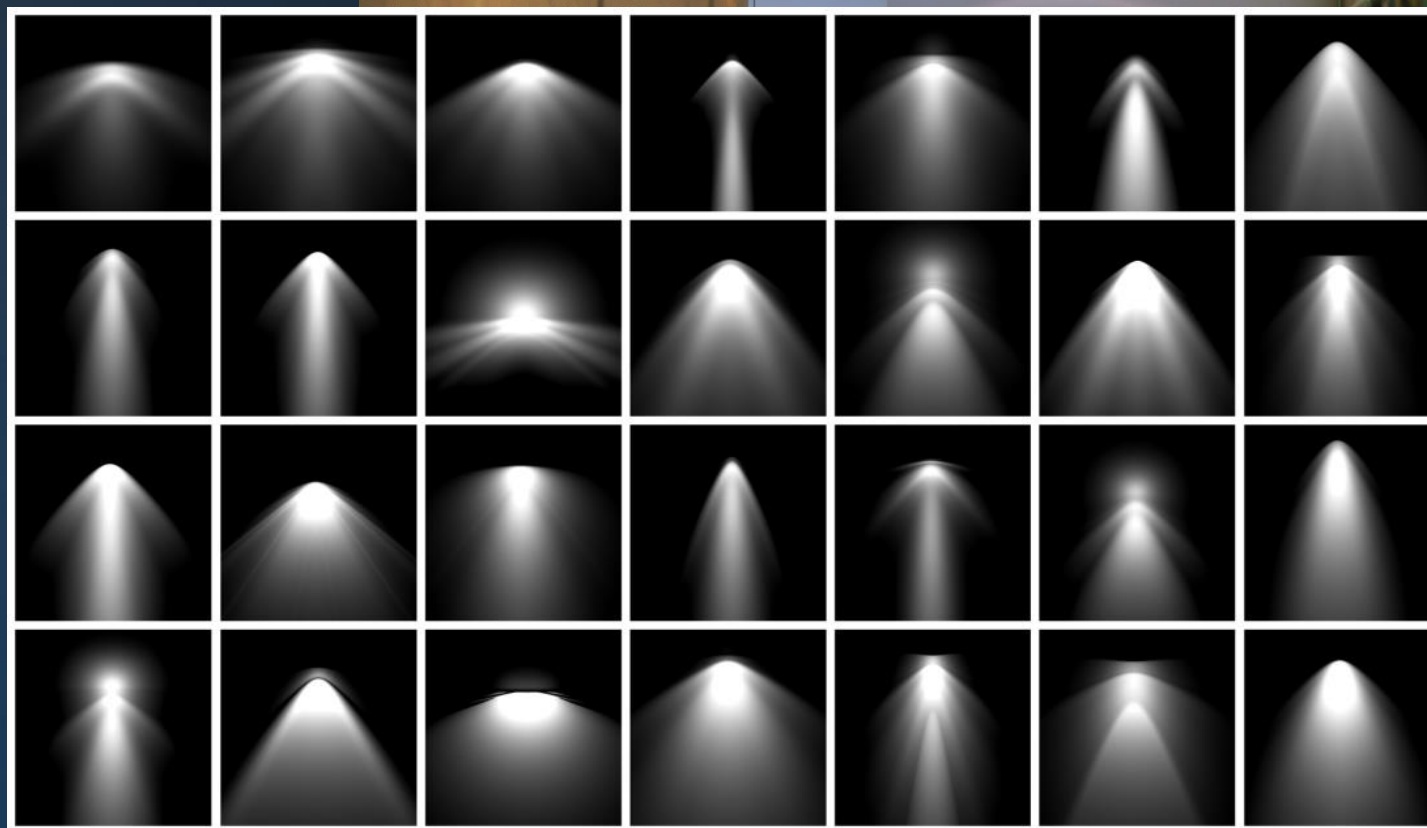
Light models



Light models



Light models

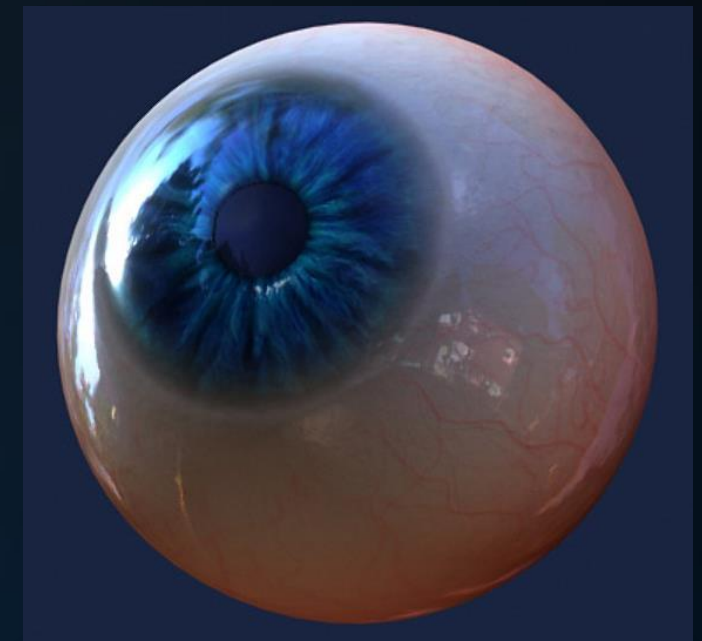
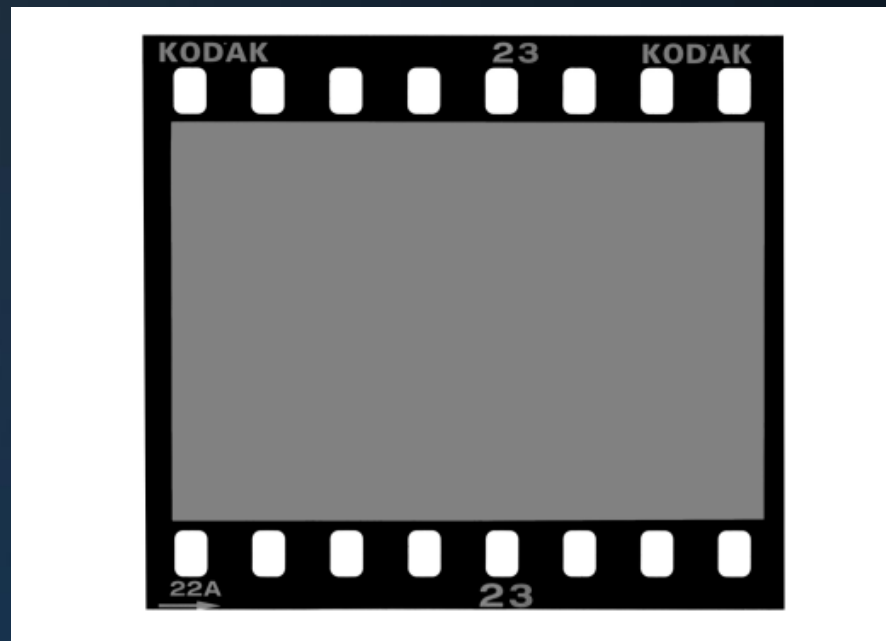
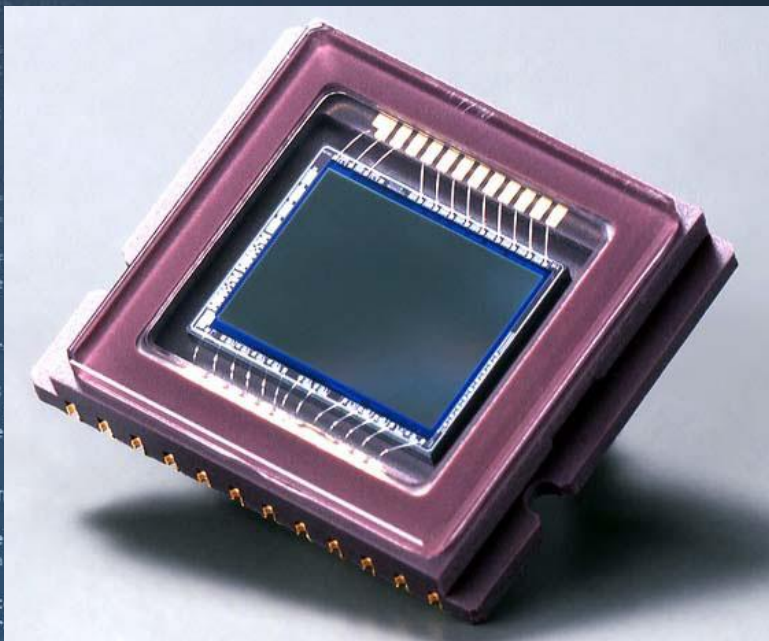


Light models



Introduction

Sensor models



```
...ics  
...A (depl  
...t = ins  
...nt = nt  
...os2t =  
...D, N );  
...9)  
...at a =  
...at Tr =  
...Tr) R =  
...E * dif  
...= true  
...efl + r  
...D, N );  
...refl *  
...= true  
...MAXDEPT  
...survive  
...estima  
...if;  
...radianc  
...e.x + r  
...v = true;  
...at brdfPdf = EvaluateDiffuse( L, N ) * Radiance  
...at3 factor = diffuse * INVPI;  
...at weight = Mis2( directPdf, brdfPdf );  
...at cosThetaOut = dot( N, L );  
...E * ((weight * cosThetaOut) / directPdf) * Radiance  
...random walk - done properly, closely following  
...rive)  
...;  
...at3 brdf = SampleDiffuse( diffuse, N, r1, r2, BR, &pdf );  
...survive;  
...pdf;  
...n = E * brdf * (dot( N, R ) / pdf);  
...ision = true;
```



Introduction

1. Light is emitted by a light source
2. Light interacts with the scene
3. Light is absorbed by a sensor

Absorption

Scattering



Today's Agenda:

- Introduction
- Light Sources
- Materials
- Sensors
- Shading



Light Sources

Directional lights

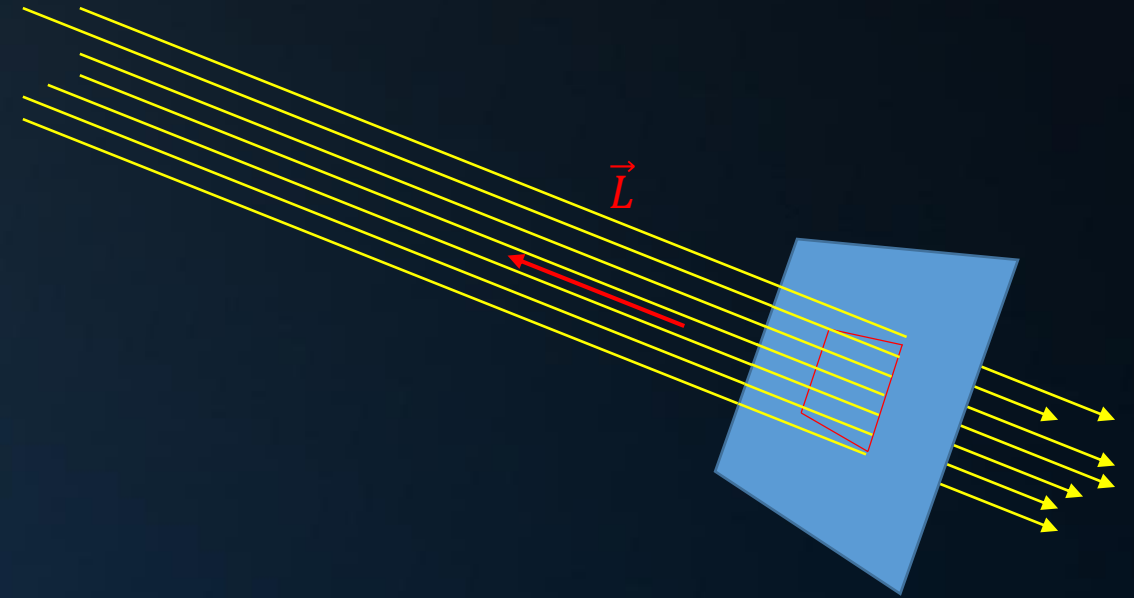
Directional light, such as the light from the sun:

Specified by a normalized, reversed vector $\vec{L}$.

Power is specified as energy travelling through a unit surface area, perpendicular to $\vec{L}$.

This quantity is called *irradiance*; units: $W\ m^{-2}\ s^{-1}$.

The symbol for irradiance is E .



For practical purposes, we will express the energy as RGB vectors. Note that R,G,B can exceed 1, unlike e.g. colors in a painting.



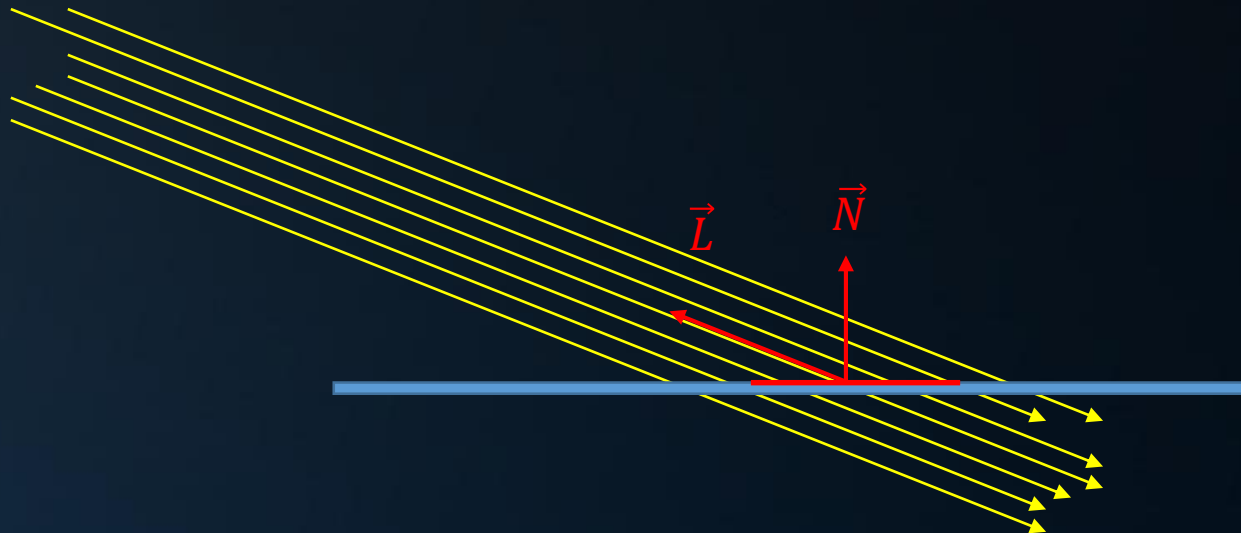
Light Sources

Directional lights

When illuminating a surface, we need to know how much light arrives at a unit area on the surface, i.e. how much light passes through a unit surface area perpendicular to $\vec{N}$.

For this, we multiply by the cosine of the angle between $\vec{N}$ and $\vec{L}$, i.e. $\vec{N} \cdot \vec{L}$.

Note that the cosine is clamped to 0, to prevent negative contributions from light arriving from the backside of the surface.



$$E = E_L \overline{\cos \theta_i}$$

$$E = E_L \max(\vec{N} \cdot \vec{L}, 0)$$



Light Sources

Irradiance

The unit surface may receive light from many directions. For multiple lights, irradiance is additive, and represents the energy arriving over the hemisphere:

$$E = \sum_{k=1}^n E_{L_k} \overline{\cos \theta}_{i_k}$$



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Materials

Material properties:

- Texture + detail texture
- Shader
- Normal map
- Specular map
- Color
- ...

Used to simulate the interaction of light with a material.

Interaction:

- Absorption
- Scattering



Materials

Absorption:

Happens on ‘optical discontinuities’.

Light energy is converted in other forms of energy (typically heat), and disappears from our simulation.

Materials typically absorb light with a certain wavelength, altering the color of the scattered light. This is how we perceive material color.



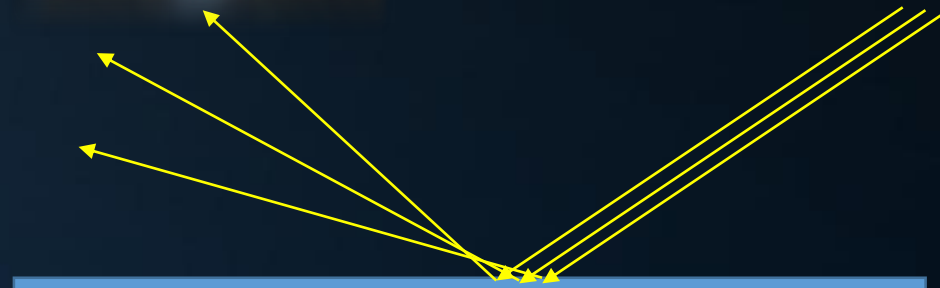
Materials

Scattering

Happens on ‘optical discontinuities’.

Scattering causes light to change direction.
Note that the amount of energy does not change due to scattering.

Light leaving the hemisphere can never exceed light entering the hemisphere, unless the material is emissive.

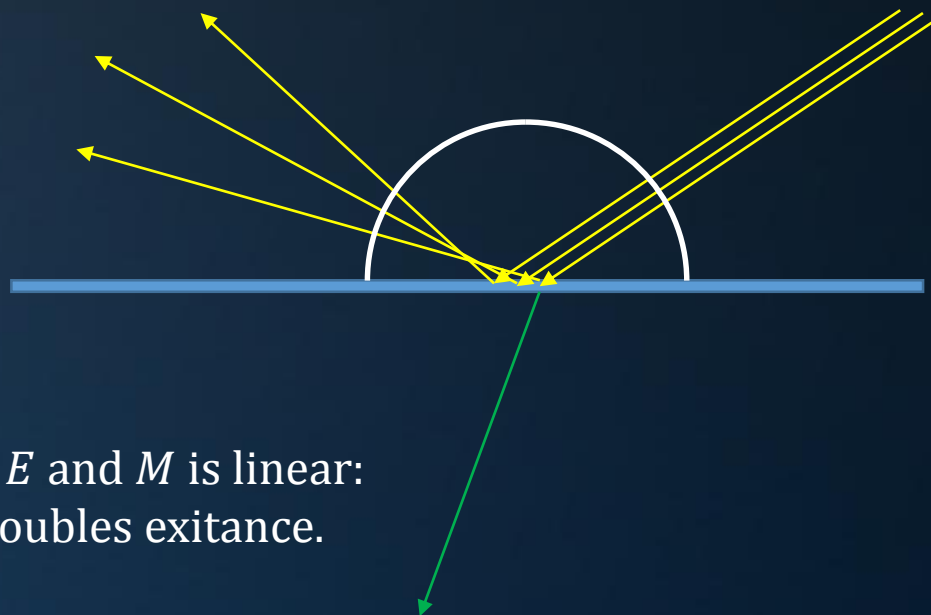


Materials

Light / surface interaction

In: irradiance (E), from all directions over the hemisphere.

Out: exitance (M), in all directions over the hemisphere.



The relation between E and M is linear:
doubling irradiance doubles exitance.

$\frac{M}{E}$ must be in the range 0..1.



Today's Agenda:

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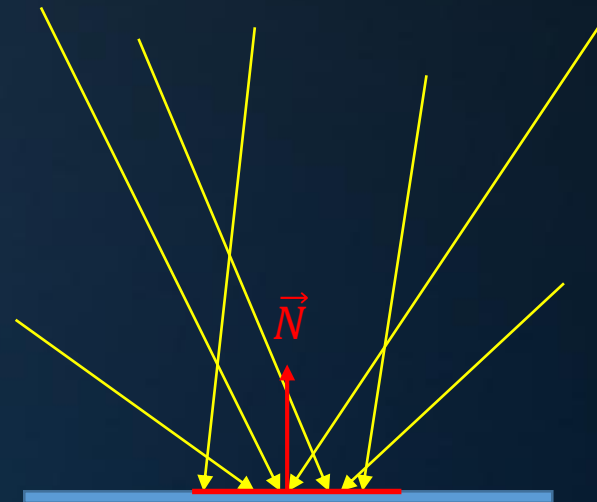
Sensors

Sensors typically consists of many small sensors:

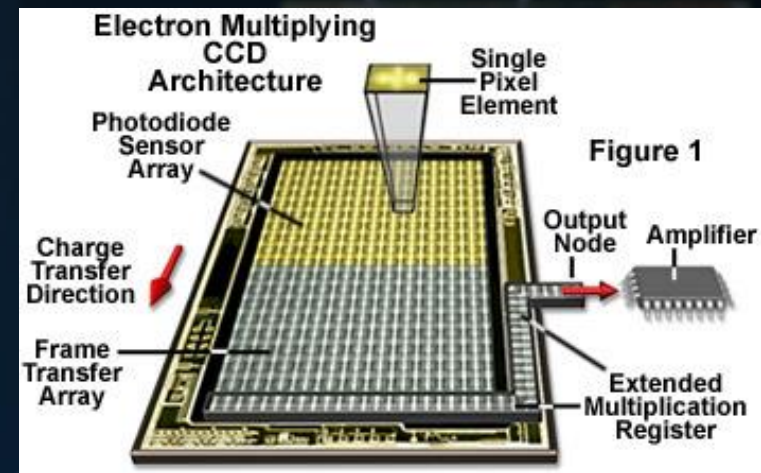
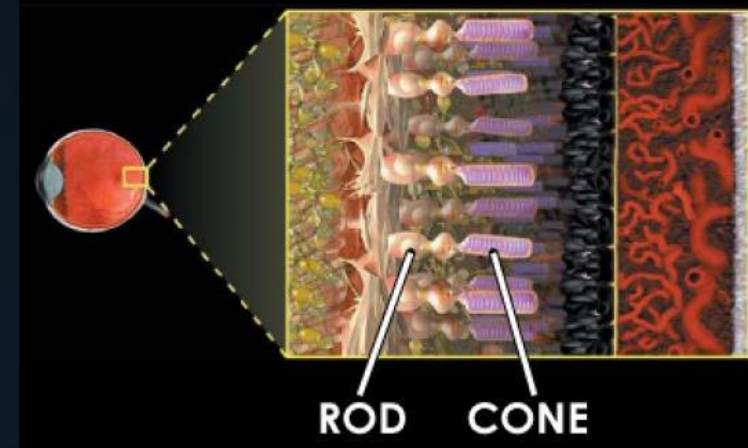
- Rods and cones in the eye
- Dye particles in the film
- Pixel elements in a CCD
- A ray in a ray tracer
- A fragment in a rasterizer

Note that we cannot use irradiance to generate an image:

irradiance is a measure for light arriving from all directions.



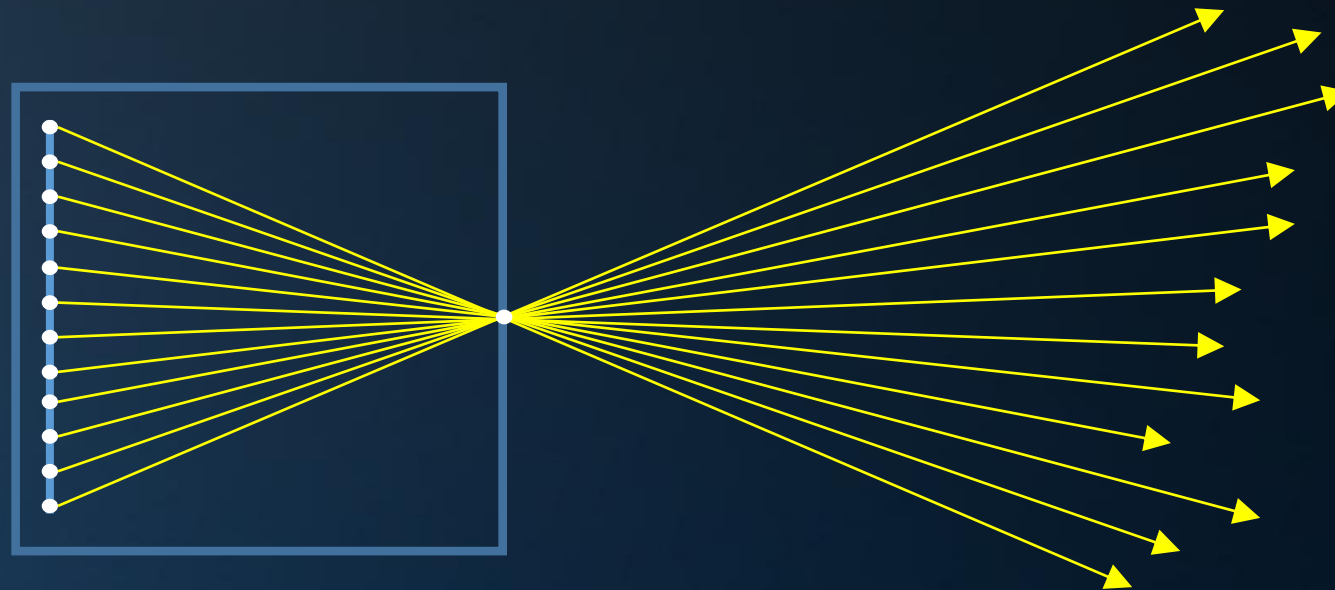
ENLARGED CROSS-SECTION OF RETINA



Sensors

Pinhole camera

To capture light from a specific direction, we use a camera with a small opening (the aperture), so that each sensor can ‘see’ a small set of incoming directions.



Sensors

Radiance

Using a pinhole camera, the sensors become directionally specific:

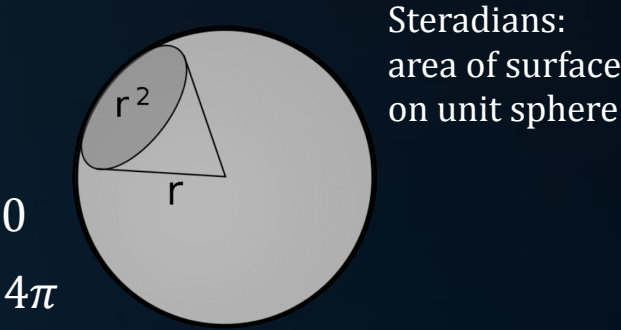
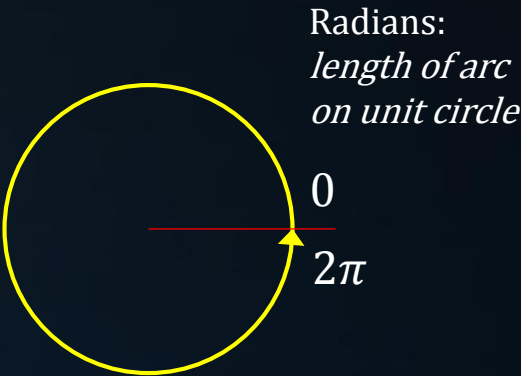
they average light over a small area, and a small set of incoming directions.

This is referred to as *radiance* :

The density of light flow per area per incoming direction.

Units: $W\ m^{-2}\ sr^{-1}\ s^{-1}$.

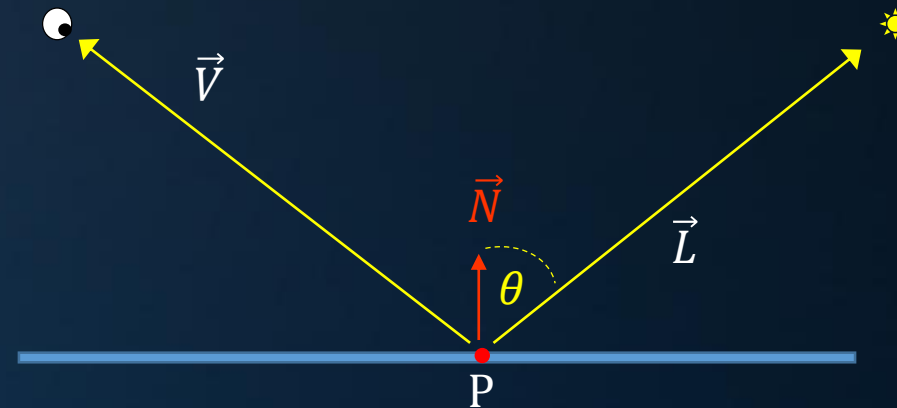
Symbol: L



Sensors

Summing it up:

- Light arrives from all light sources on point P ;
- The energy flow per unit area, perpendicular to $\vec{L}$ is projected on a surface perpendicular to $\vec{N}$. This is *irradiance*, or: E .
- Exitant light M is scattered over all directions on the hemisphere.
- Light scattered towards the eye arrives at a sensor.
- The sensor detects radiance: light from a specific set of directions.



Today's Agenda:

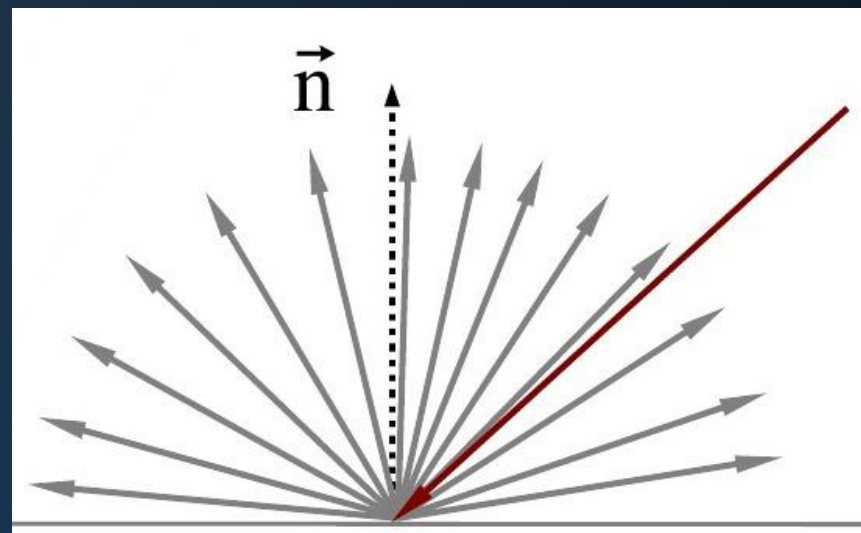
- Introduction
- Light Sources
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- Shading



Shading

Definition

Shading: the process of using an equation to compute the outgoing radiance L_o along the view ray $\vec{V}$, based on material properties and light sources.



Diffuse or Lambert BRDF, also called “N dot L shading”



Shading

Lambert shading model

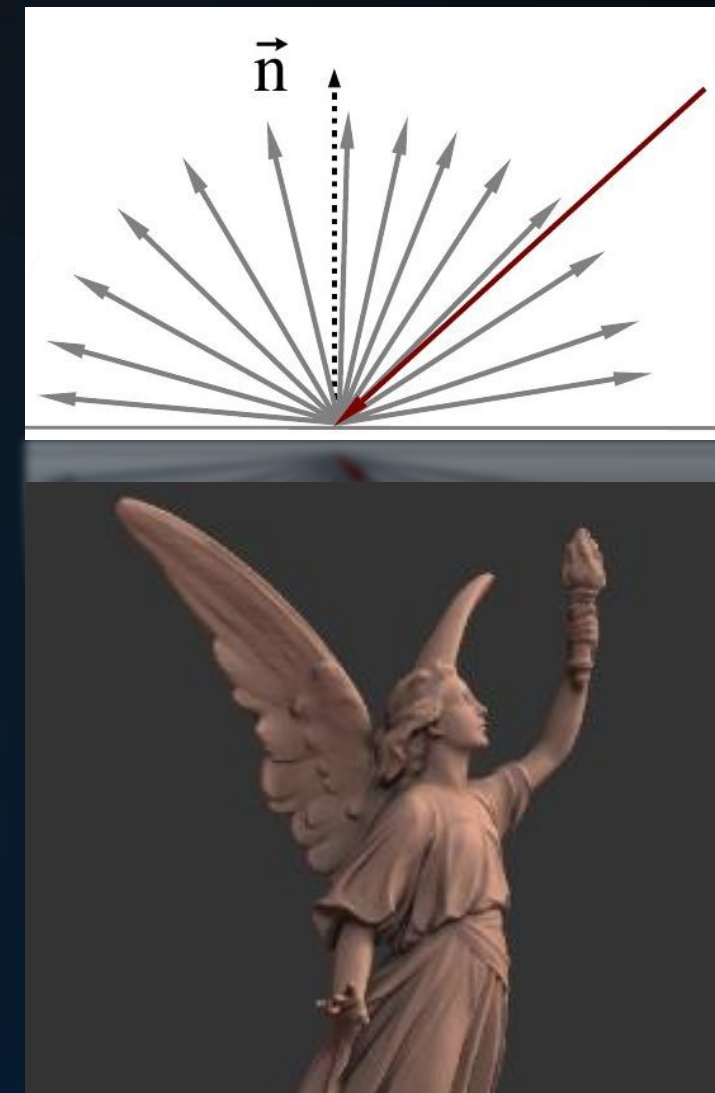
The diffuse shading model is:

$$M_{diff} = \frac{c_{diff}}{\pi} E_{Li} \overline{\cos\theta_i}$$

This takes into account:

- Projection of the directional light on the normal;
- Absorption due to material color c_{diff} .

Distance attenuation is represented in E_{Li}
(for directional lights, this is not applicable)



Shading

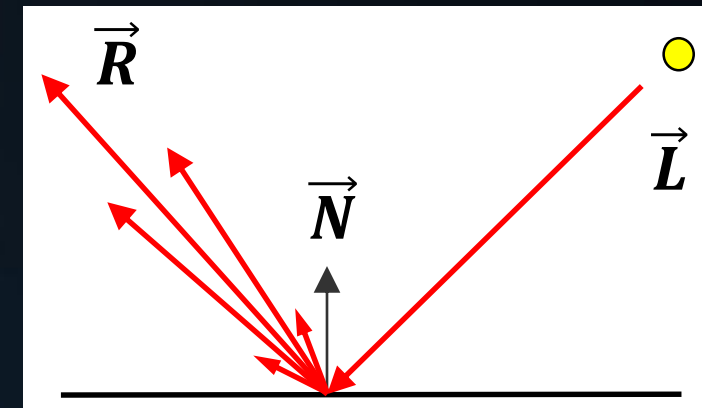
Phong shading model

The Phong shading model combines a diffuse reflection with a glossy one, and adds an ambient factor.

$$M_{\text{phong}} = c_{\text{ambient}} + c_{\text{diff}}(\vec{N} \cdot \vec{L})L_{\text{diff}} + c_{\text{spec}}(\vec{V} \cdot \vec{R})^s L_{\text{spec}}$$

The Phong shading model is an ‘empirical model’, and has many problems:

- It doesn’t guarantee that $M \leq E$;
- It doesn’t take irradiance as input;
- It requires many (unnatural) parameters;
- That ambient factor...



Shading

BRDF – Bidirectional Reflectance Distribution Function

Defines the relation between *irradiance* and *radiance*.

Or, more accurately:

The BRDF represents the ratio of reflected radiance exiting along $\vec{V}$, to the irradiance incident on the surface from direction $\vec{L}$.

Note that the BRDF takes two parameters: an incoming and an outgoing direction.

$$f_r(\vec{L}, \vec{V}) = \frac{dL_r(\vec{V})}{dE_i(\vec{L})}$$



Shading

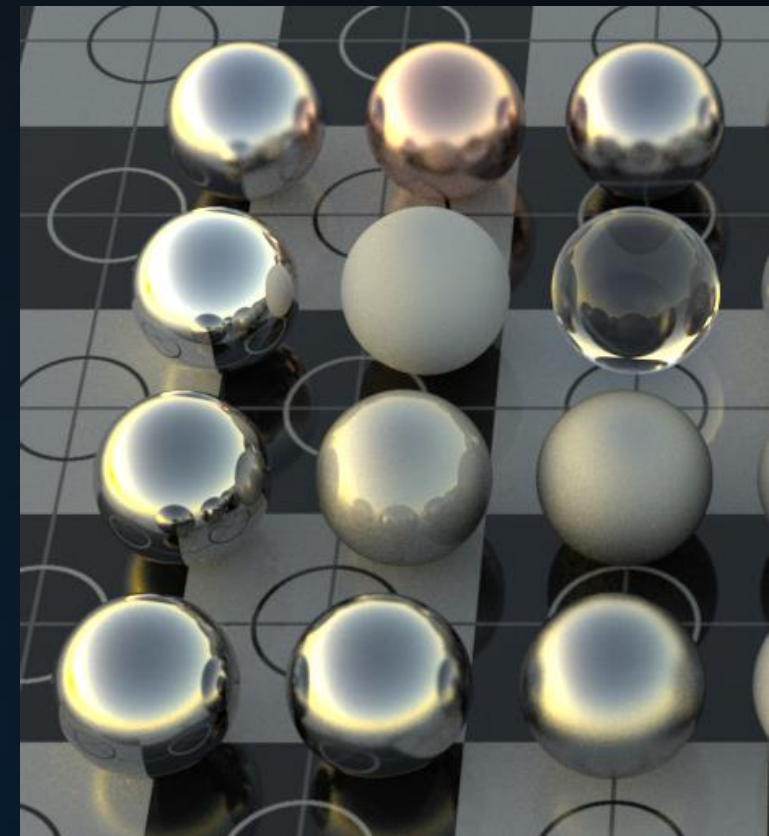
BRDF – Bidirectional Reflectance Distribution Function

BRDFs formalize the interaction of light / surface interaction, and allow us to do so in a physically correct way.

Games are switching to physically based models rapidly:

- To increase realism;
- To reduce the number of parameters in shaders;
- To have uniform shaders for varying lighting conditions.

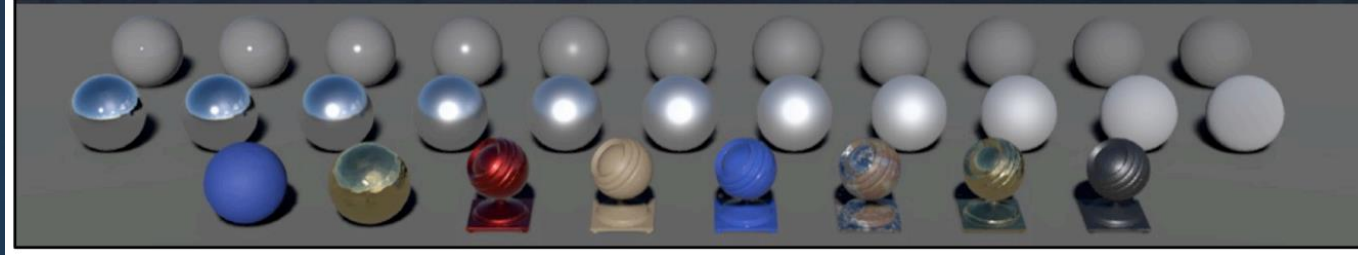
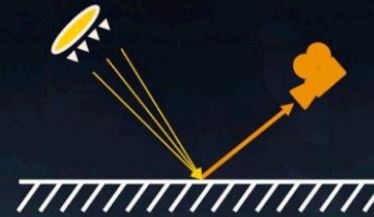
More on this in Advanced Graphics!



Shading

Lighting – Analytical Lights

- **Sun** light
 - **Units:** Illuminance (lux)
 - Facing disk with non-null solid angle



“Moving Frostbite to PBR”

http://www.frostbite.com/wp-content/uploads/2014/11/s2014_pbs_frostbite_slides.pdf



```

100
    (depth < MAXDEPTH)
    {
        int = inside / 1.5 * 1.5;
        int = nt / nc; ddx = dot(N, dir);
        double r2 = 1.0f - nnt * nnt;
        double D, N );
        0);
    }

    int a = nt - nc, b = nt - nc;
    int Tr = 1 - (RR + (1 - RR) * a);
    (Tr) R = (D * nnt - N * (ddx
    )

    E * diffuse;
    = true;

    .

    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;

    MAXDEPTH)

    survive = SurvivalProbability( diffuse,
    estimation - doing it properly, clearly
    if;
    radiance = SampleLight( &rand, I, &t, &light;
    e.x + radiance.y + radiance.z) > 0) && (env
    w = true;
    int brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    int3 factor = diffuse * INVPI;
    int weight = Mix2( directPdf, brdfPdf );
    int cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following well
    vive)

    ;
    int3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```

Michal Drobot
Senior Tech Programmer

Guerrilla Games



Shading



Lighting Conditions

Want same content to look good

“Physically Based Shading in Unity”

http://aras-p.info/texts/files/201403-GDC_UnityPhysicallyBasedShading_notes.pdf



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J. Bikker - April-July 2015 - Lecture 9: “Shading Models”

END of “Shading Models”

next lecture: “Ground Truth”

