

```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 1.0f - nt)
    {
        nt = nt / nc; ddn = ddn * nc;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        Tr) R = (D * nnt - N * (ddn > 0 ? 1 : -1));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, N, align );
    e.x + radiance.y + radiance.z );
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```

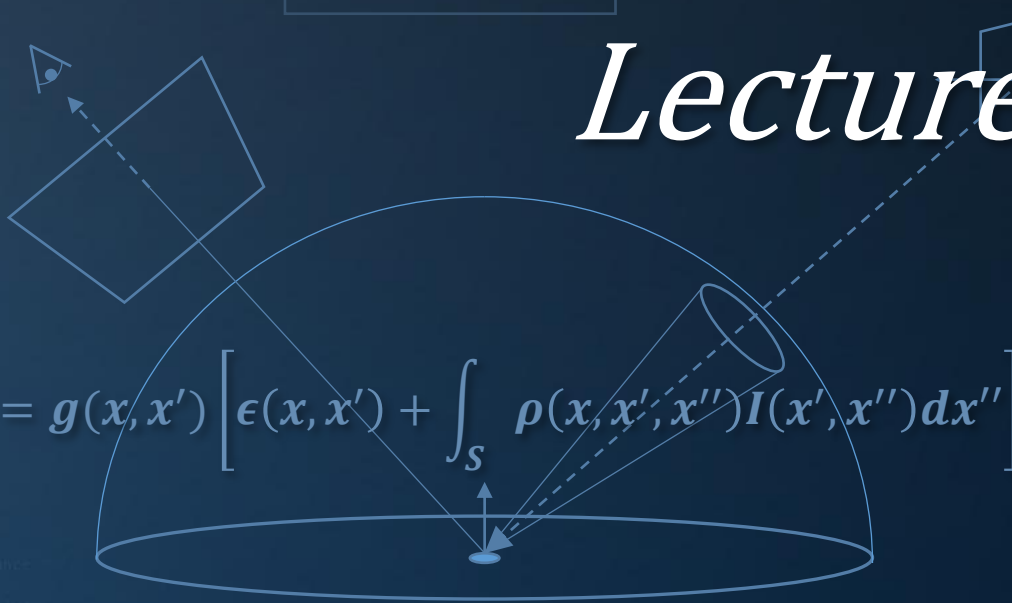


INFOMAGR – Advanced Graphics

Jacco Bikker - November 2021 - February 2022

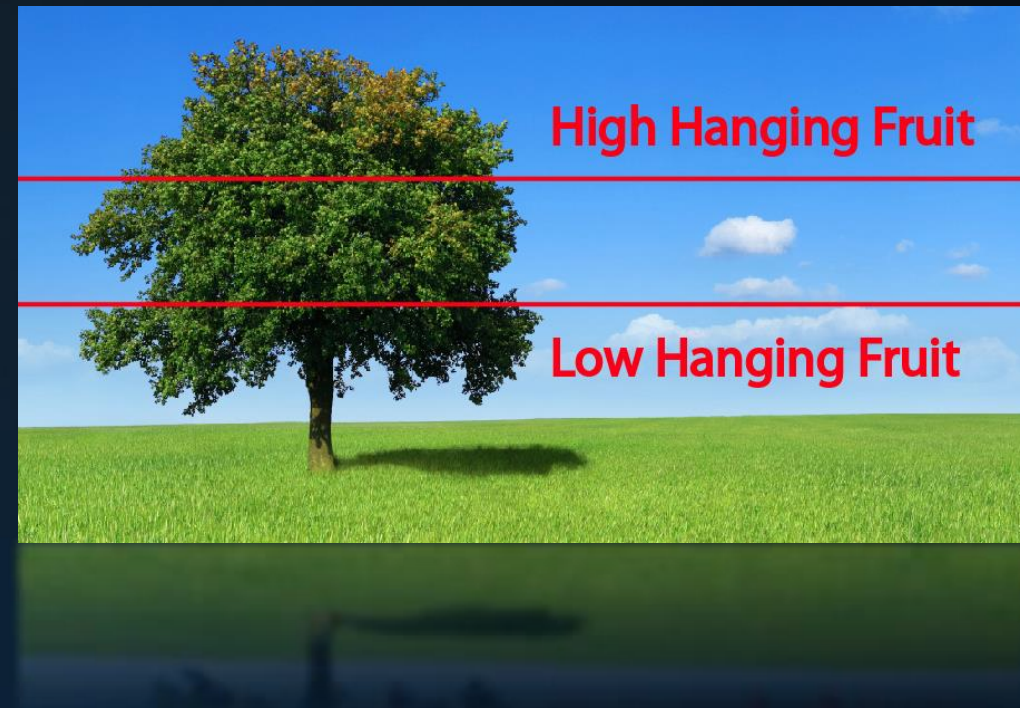
Lecture 11 - “Various”

Welcome!



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox
- Spots, IES Profiles
- Microfacets



Gamma Correction

Human Eye

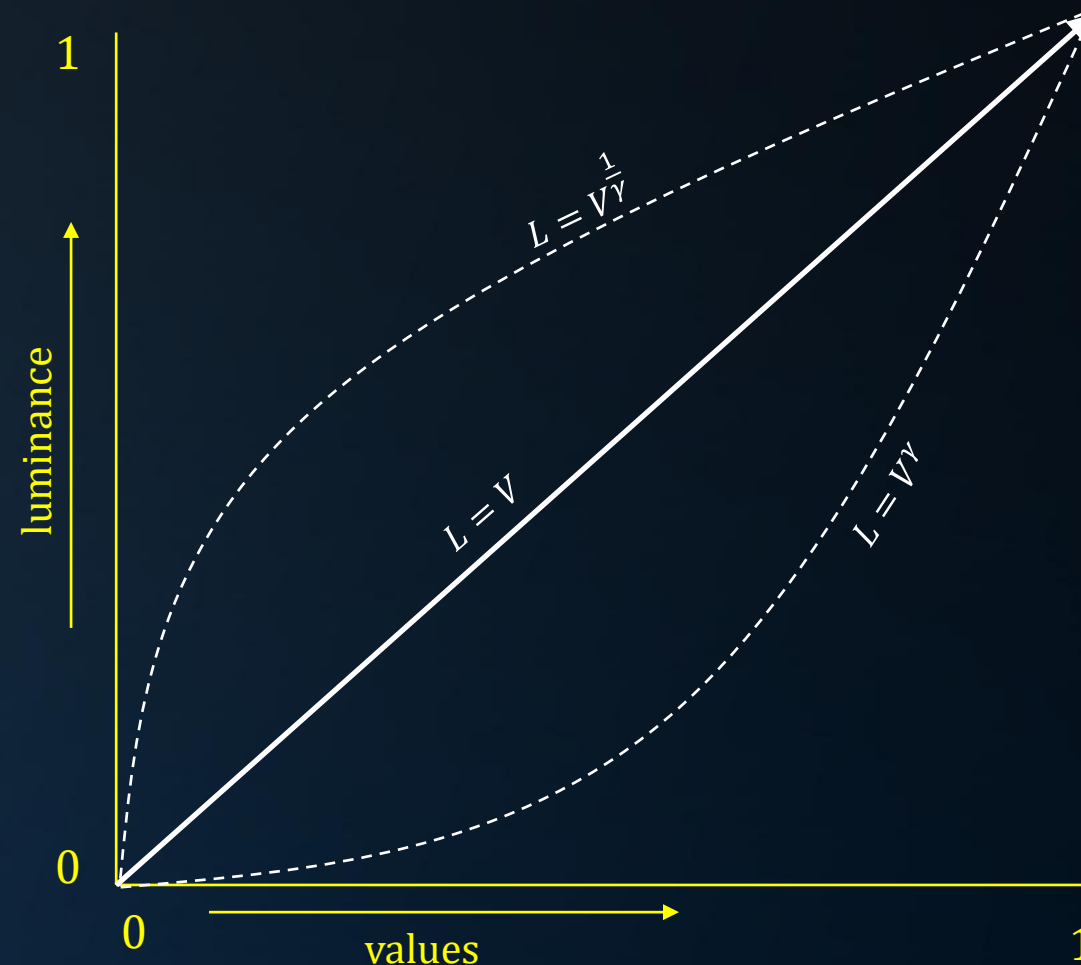
Digital representation of intensities is discrete: for ARGB32, we have 256 levels for red, green and blue.

The human eye is more sensitive to differences in luminance for dark shades. When encoding luminance, it is advantageous to have more detail in the lower regions, e.g.:

$$L = V^\gamma \Rightarrow V = L^{\frac{1}{\gamma}}$$

For the human eye, $\gamma = 2.33$ is optimal*.

*: Ebner & Fairchild, Development and testing of a color space (IPT) with improved hue uniformity, 1998.



Gamma Correction

CRT Power Response

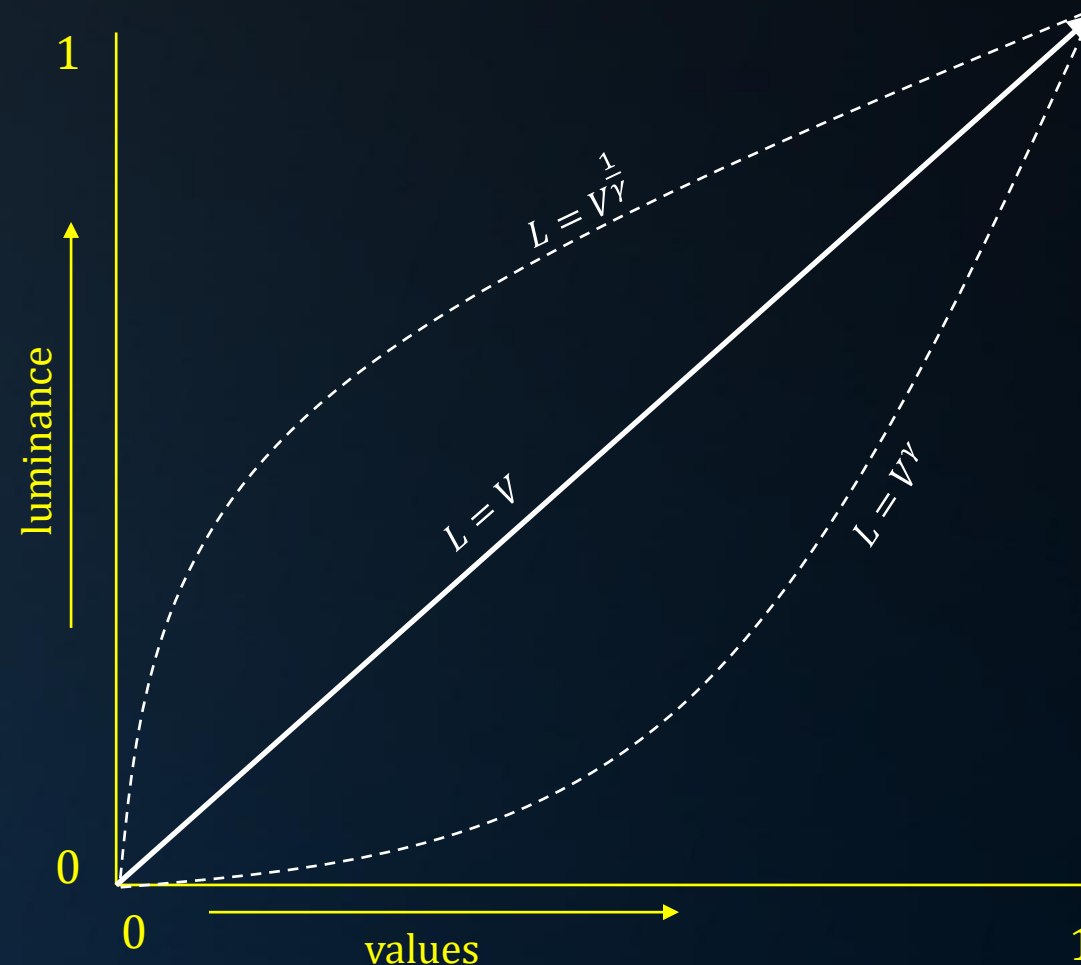
A classic CRT display converts incoming data to luminance in a non-linear way.

$$L = V^\gamma \Rightarrow V = L^{\frac{1}{\gamma}}$$

For a typical monitor, $\gamma = 2.2$.

In other words:

- If we encode our luminance using $V = L^{\frac{1}{\gamma}}$, it will be linear on the monitor.
- At the same time, this yields a distribution that has more detail for darker shades, which suits the human eye.



Gamma Correction

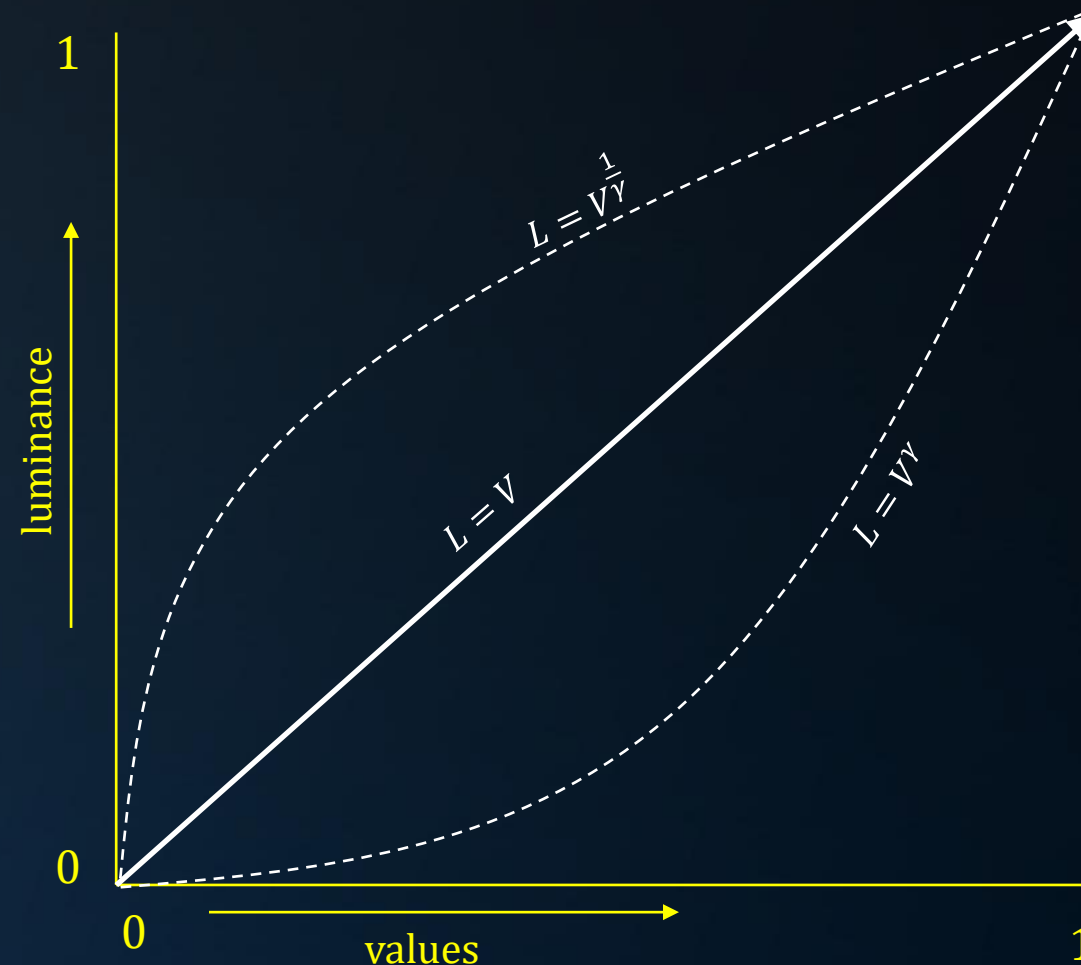
Practical Gamma Correction

To ensure linear response of the monitor to our synthesized images, we feed the monitor adjusted data:

$$V = L^{1/2.2} \approx \sqrt{L}$$

What happens if we don't do this?

1. L will be $V^{2.2}$; the image will be too dark.
2. A linear gradient will become a quadratic gradient; a quadratic gradient will become a cubic gradient → your lights will appear to have a very small area of influence.

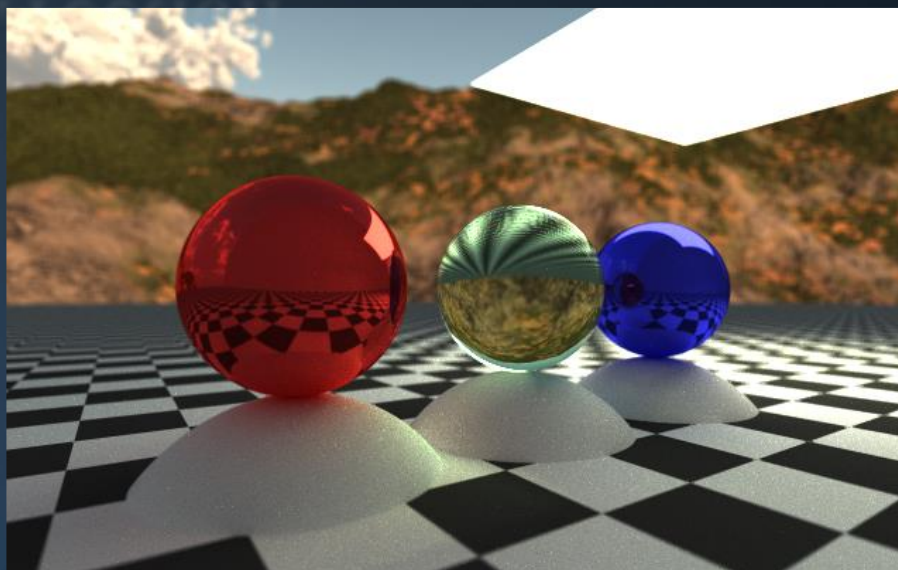


Gamma Correction

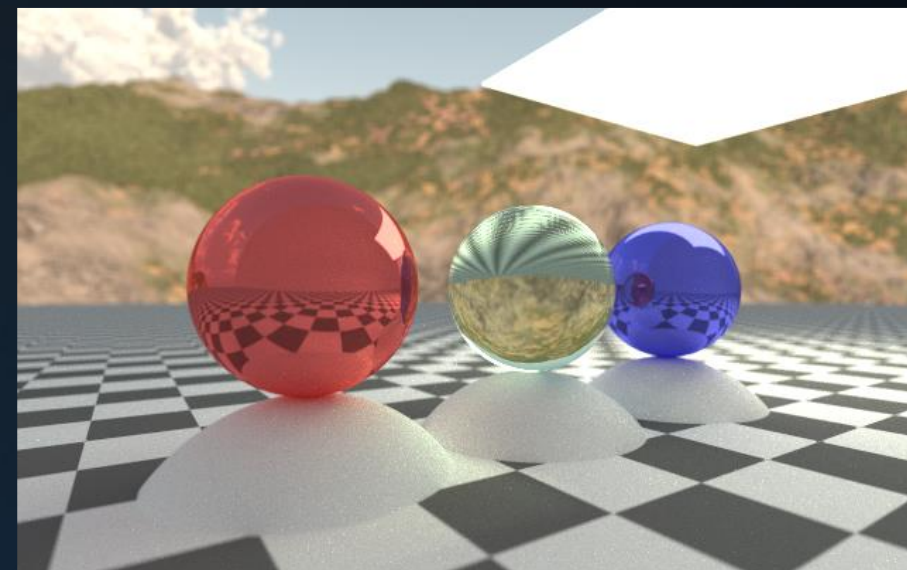
```

ics
& (depth < MAXDEPTH)
{
    nt = inside ? 1.0 : 0.0;
    nt = nt / nc; ddn = dot(N, L);
    cos2t = 1.0f - nnt * nnt;
    D, N );
    0);
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    df;
    radiance = SampleLight( &rand, I, &L, &light
    e.x + radiance.y + radiance.z ) > 0) && (depth
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (r
    random walk - done properly, closely following
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2,
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

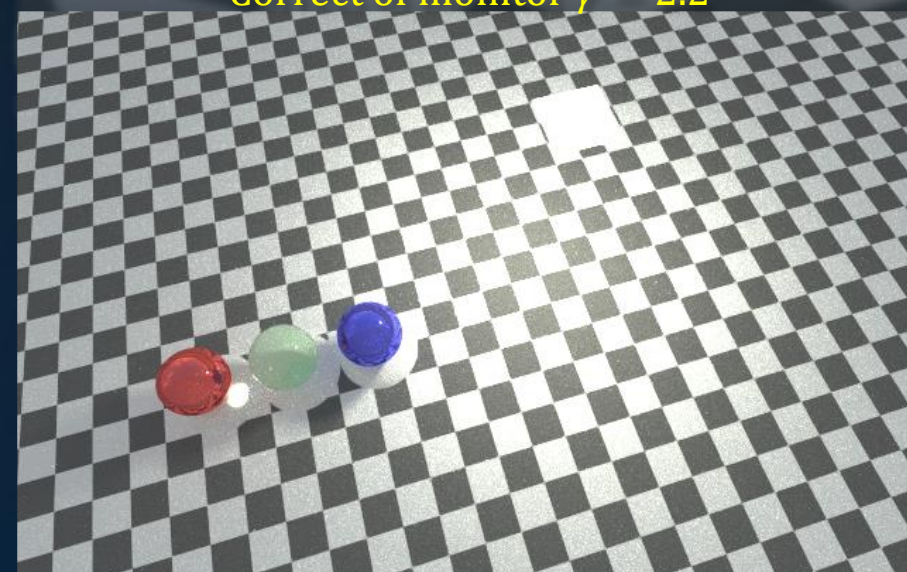
```



Correct of monitor $\gamma = 1.0$



Correct of monitor $\gamma = 2.2$



Gamma Correction

Legacy

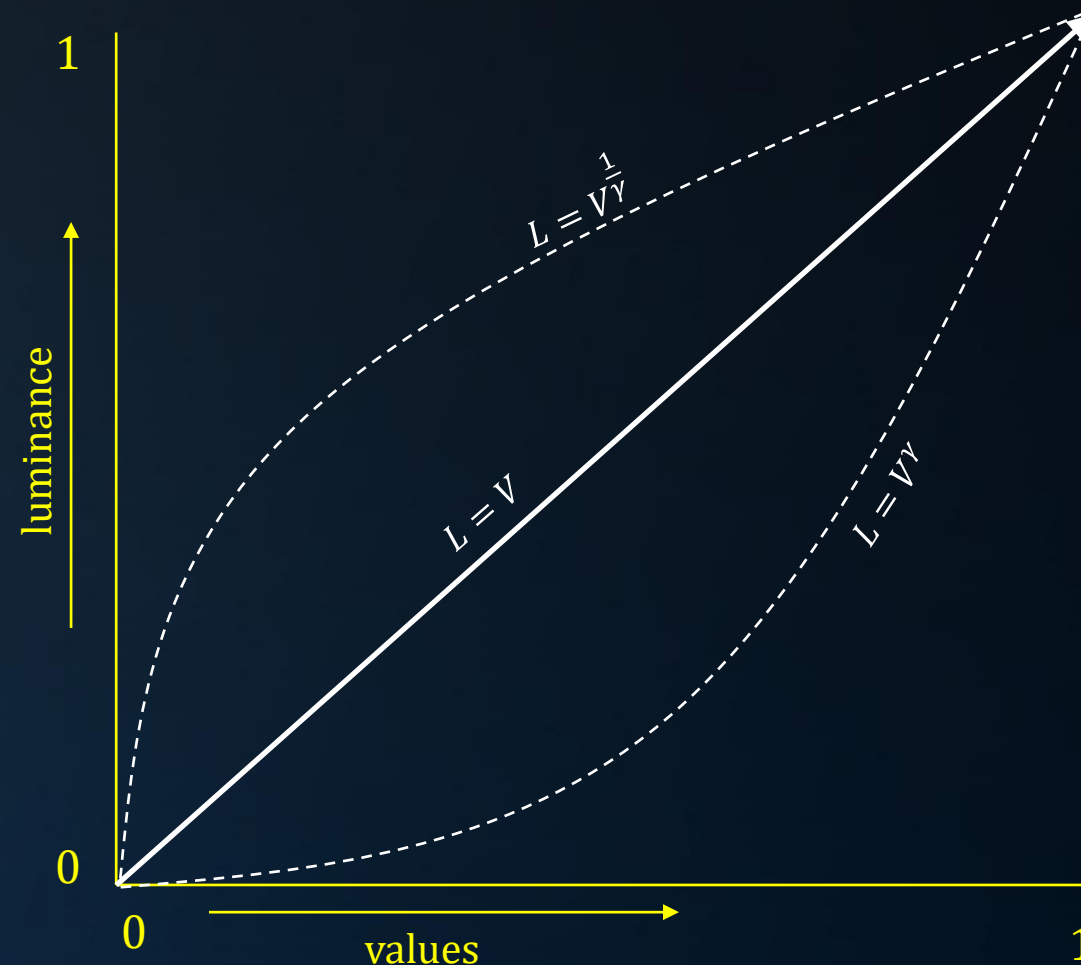
The response of a CRT is $L = V^{2.2}$; what about modern screens?

Typical laptop / desktop screens have a linear response, but expect applications to provide \sqrt{L} data... So V is modified (in hardware, or by the driver): $V = V^2$.

$$L \Rightarrow \sqrt{L} \Rightarrow L^2$$

Not all screens take this legacy into account; especially beamers will often use $\gamma = 1$.

Gamma correct only if the hardware or video driver expects it!

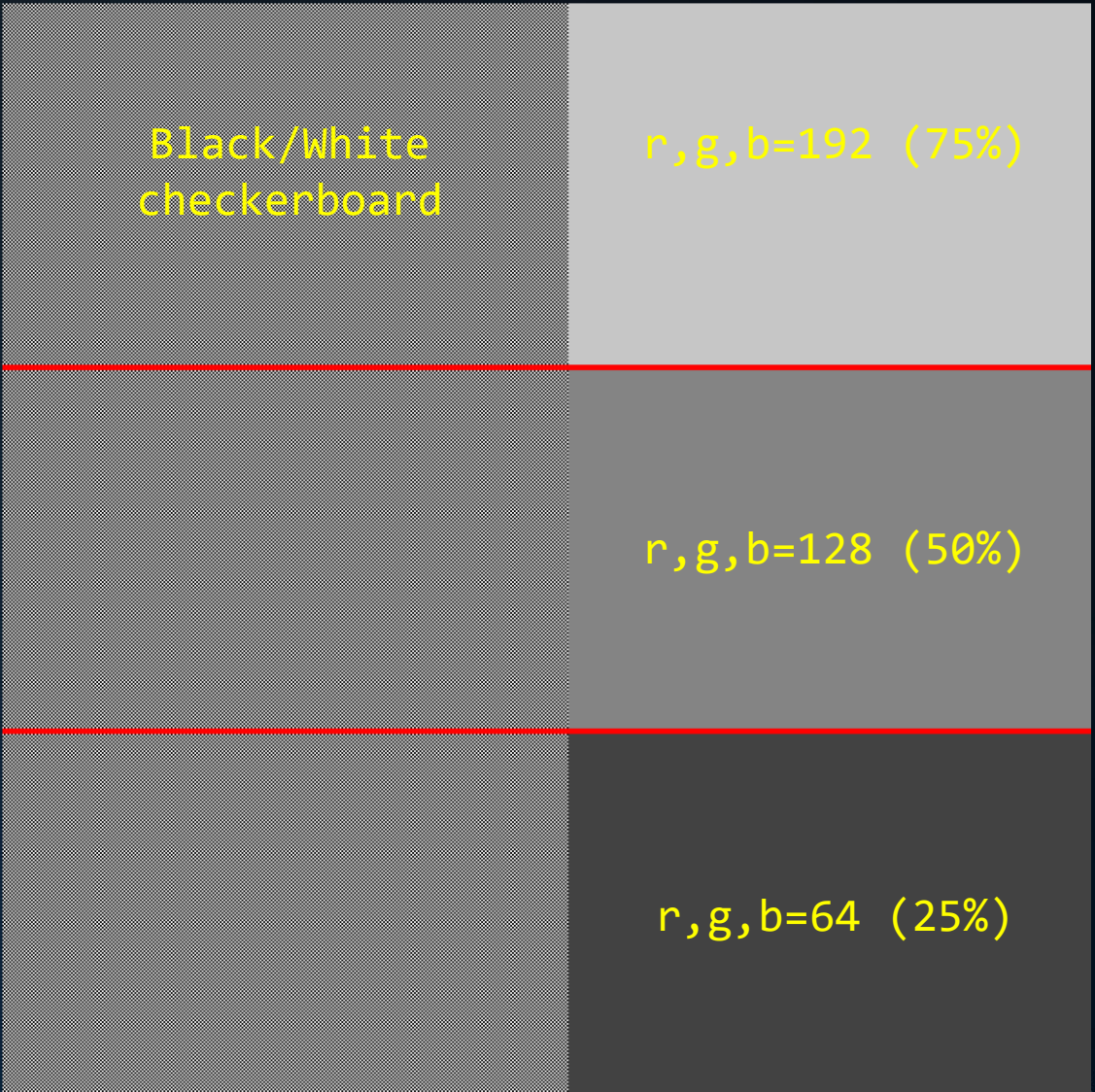


Gamma Correction

Gamma Corrected Or Not?

Open gamma.gif using the windows image previewer, and zoom to the smallest level (1:1). Which bar in the right column is most similar in brightness to the right column?

	$\gamma=1$	$\gamma=2$
75%	0.75	0.56
50%	0.50	0.25
25%	0.25	0.06



Gamma Correction

Consequences

How are your digital photos / DVD movies stored?

1. With gamma correction, ready to be sent to a display device that expects \sqrt{L}
2. Without gamma correction, expecting the image viewer to apply \sqrt{L}

For jpegs and mpeg video, the answer is 1: these images are already gamma corrected.

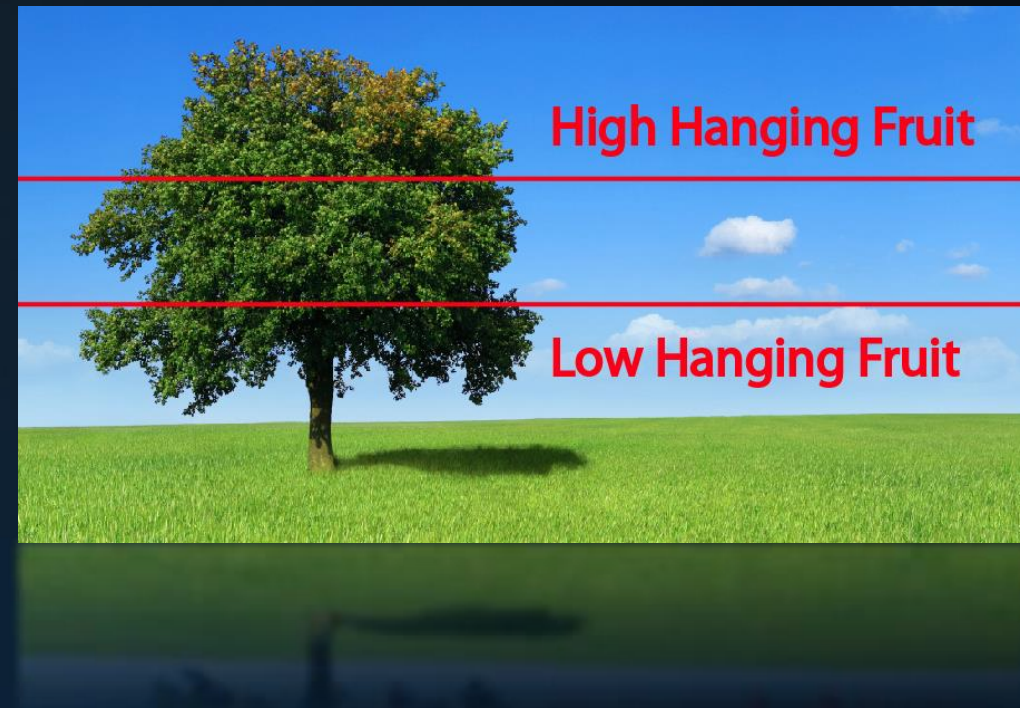
➔ Your textures may require conversion to linear space:

$$L = V^2$$



Today's Agenda:

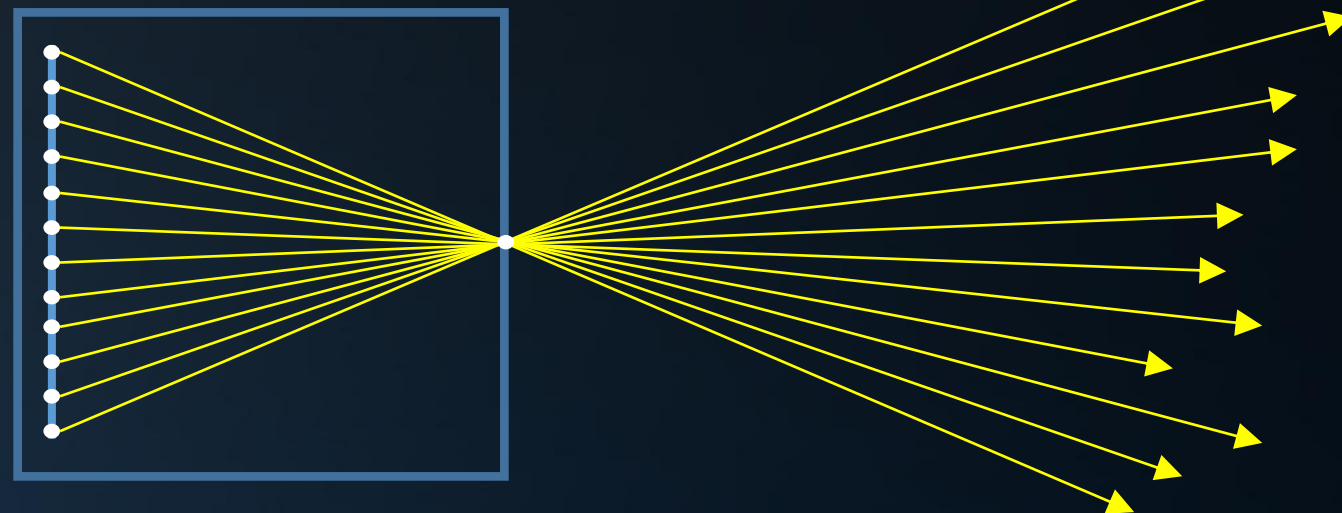
- Gamma Correction
- Depth of Field
- Skybox
- Spots, IES Profiles
- Microfacets



Depth of Field

Focus

A pinhole camera ensures that each pixel receives light from a single direction.



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = dot(N, N);
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * f);
        Tr) R = (D * nnt - N * (ddn * cos2t));
    }
    E * diffuse;
    = true;
}

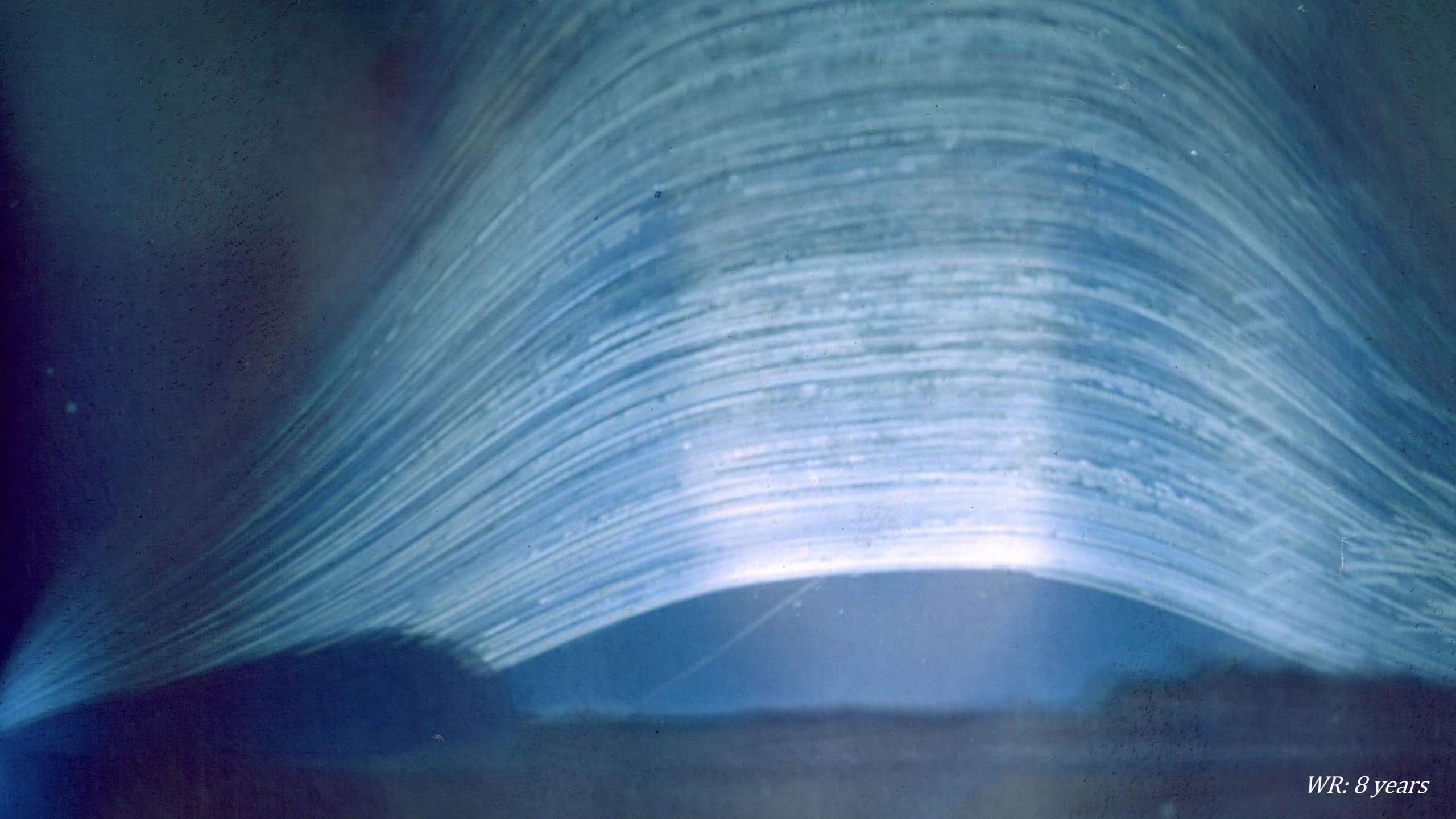
efl + refr) && (depth < MAXDEPTH)
{
    D, N );
    refl * E * diffuse;
    = true;
}

MAXDEPTH)

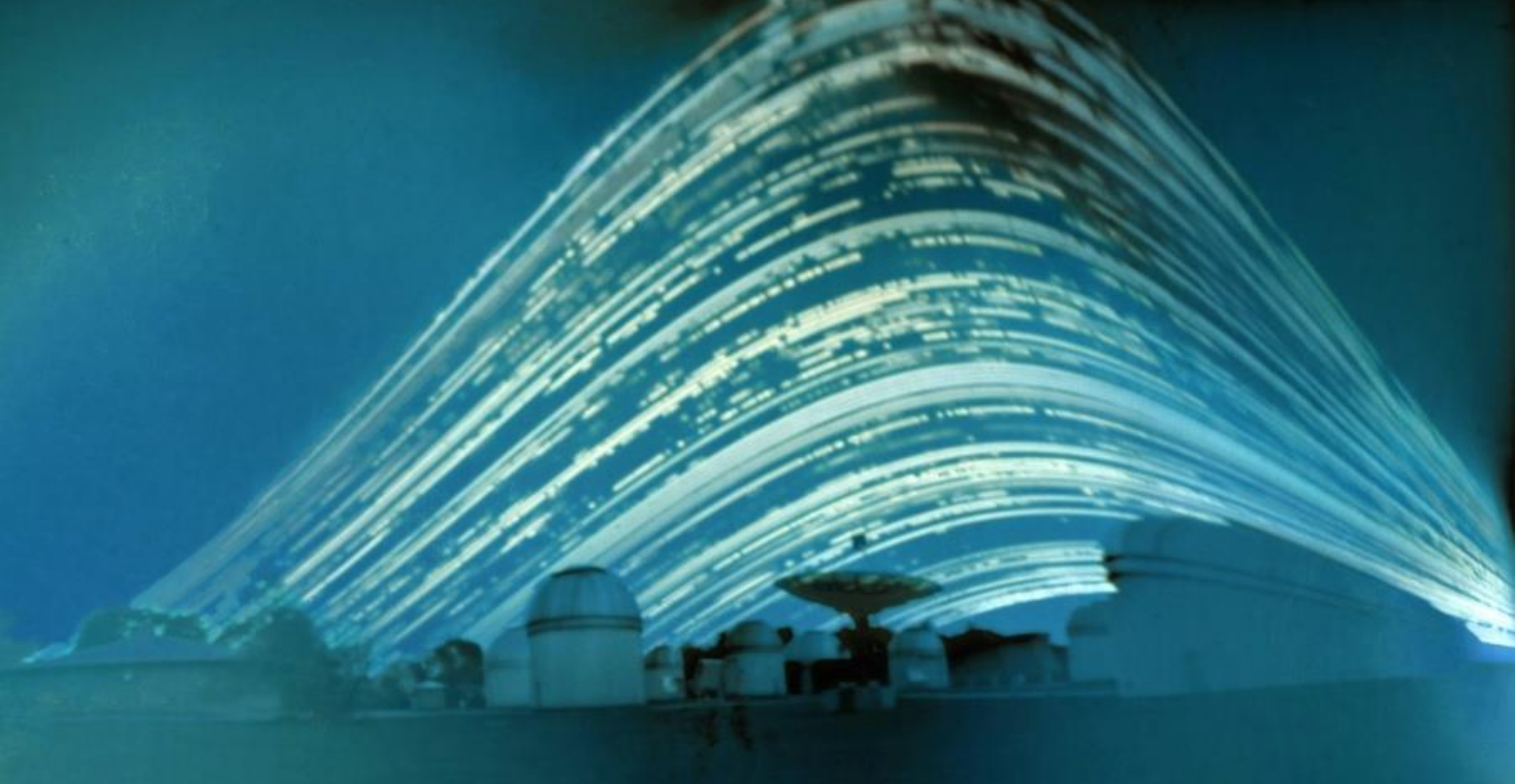
survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light );
e.x + radiance.y + radiance.z) > 0) && (depth <
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Small's
vive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```





WR: 8 years



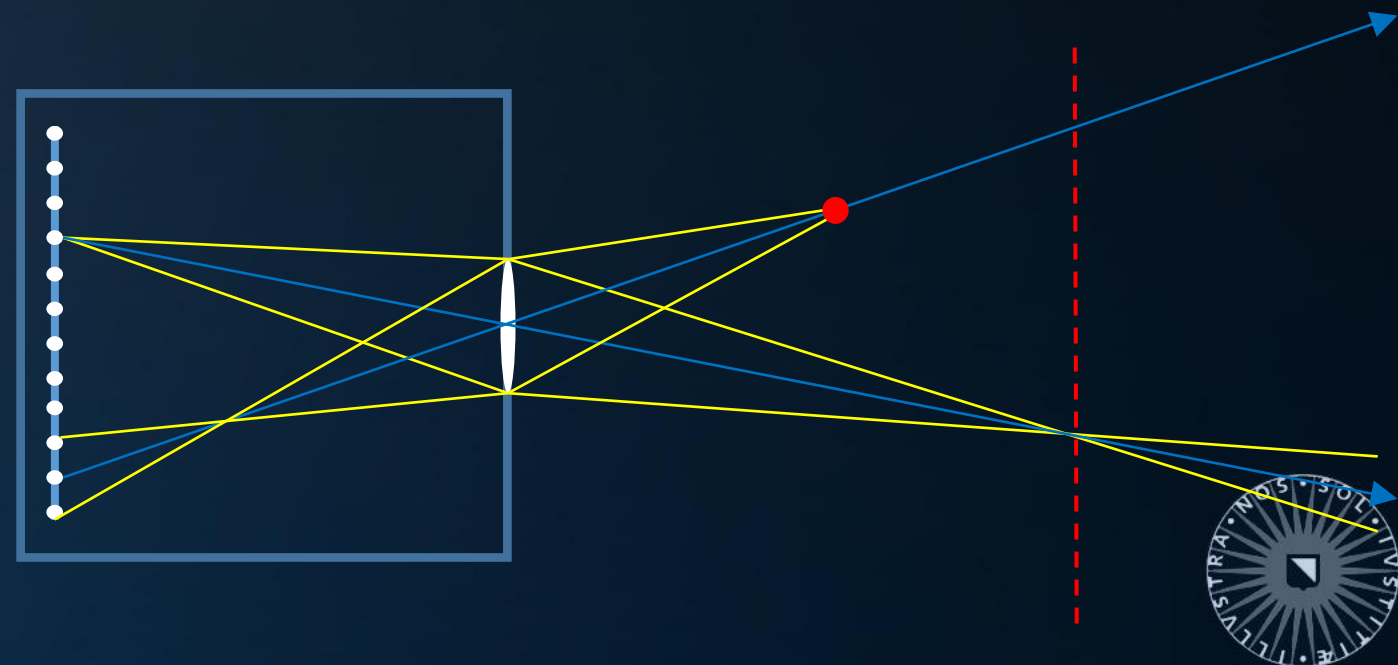
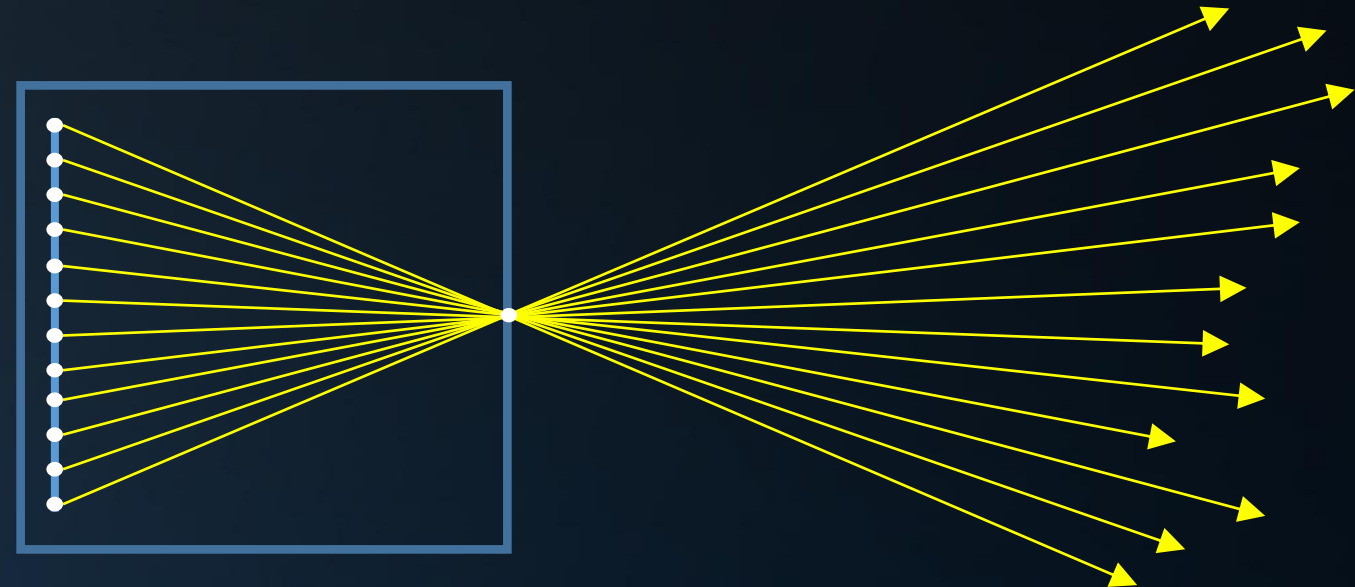
Depth of Field

Focus

A pinhole camera ensures that each pixel receives light from a single direction.

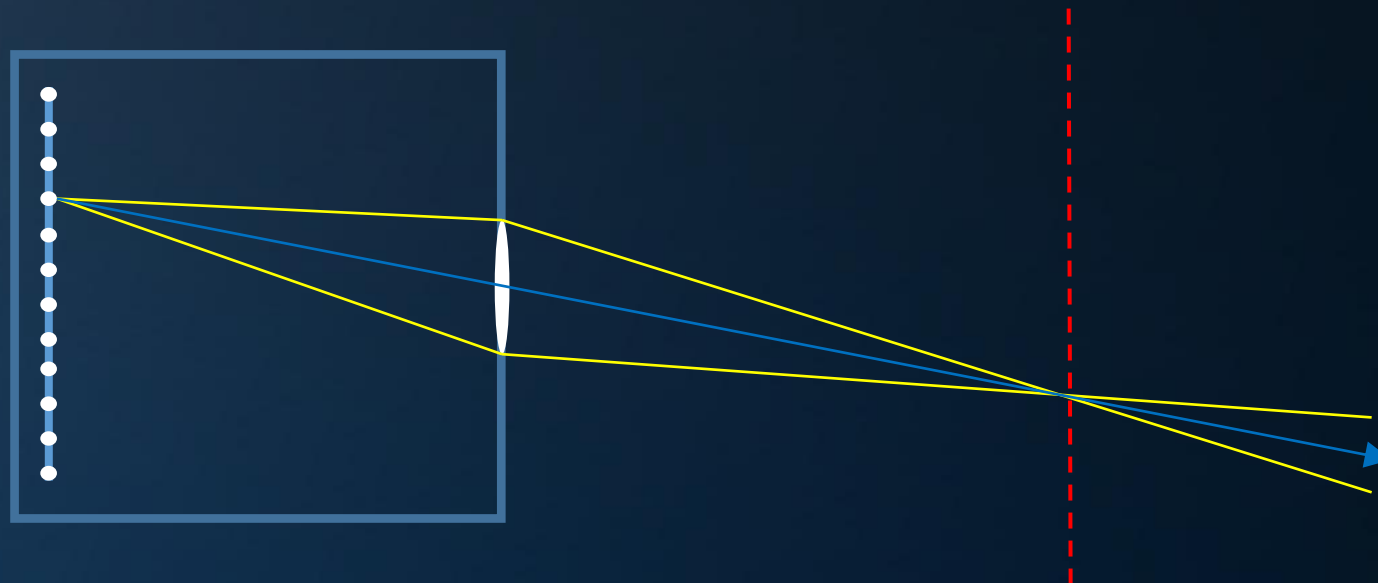
For a true pinhole, the amount of light is zero.

Actual cameras use a lens system to direct a limited set of directions to each pixel.



Focus

Light reflected from these objects to the lens end up on a single pixel on the film.

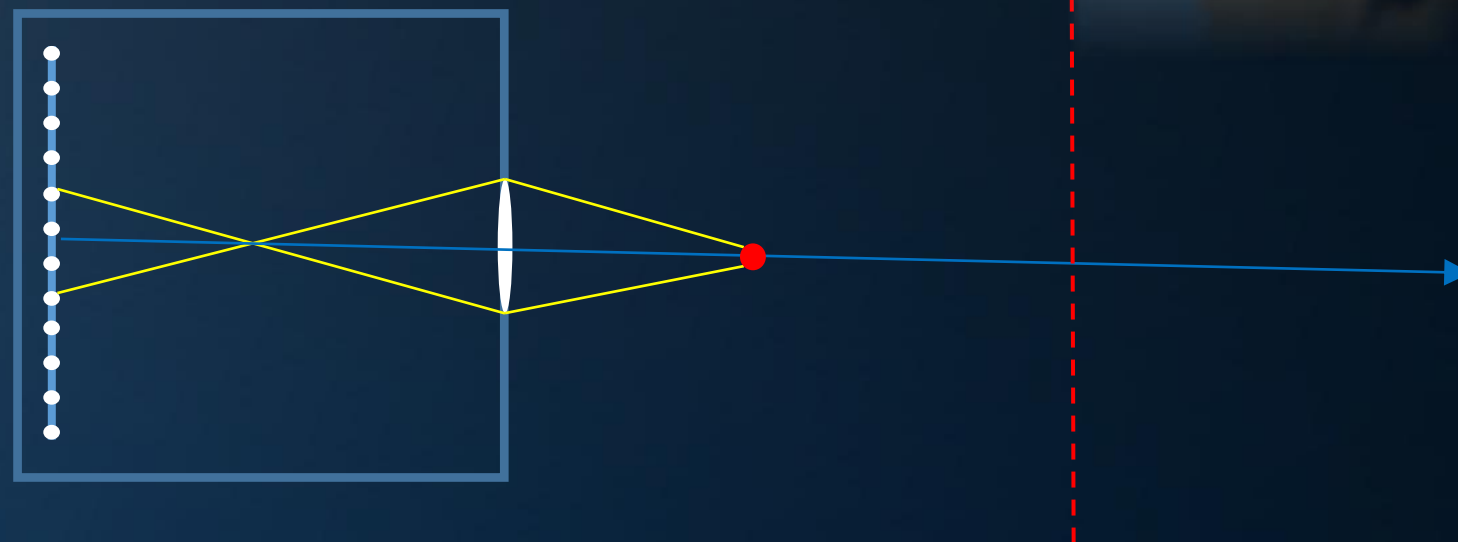


Depth of Field

Focus

Objects before the focal plane appear out of focus:

Light reflected from these objects is spread out over several pixels on the film (the 'circle of confusion').

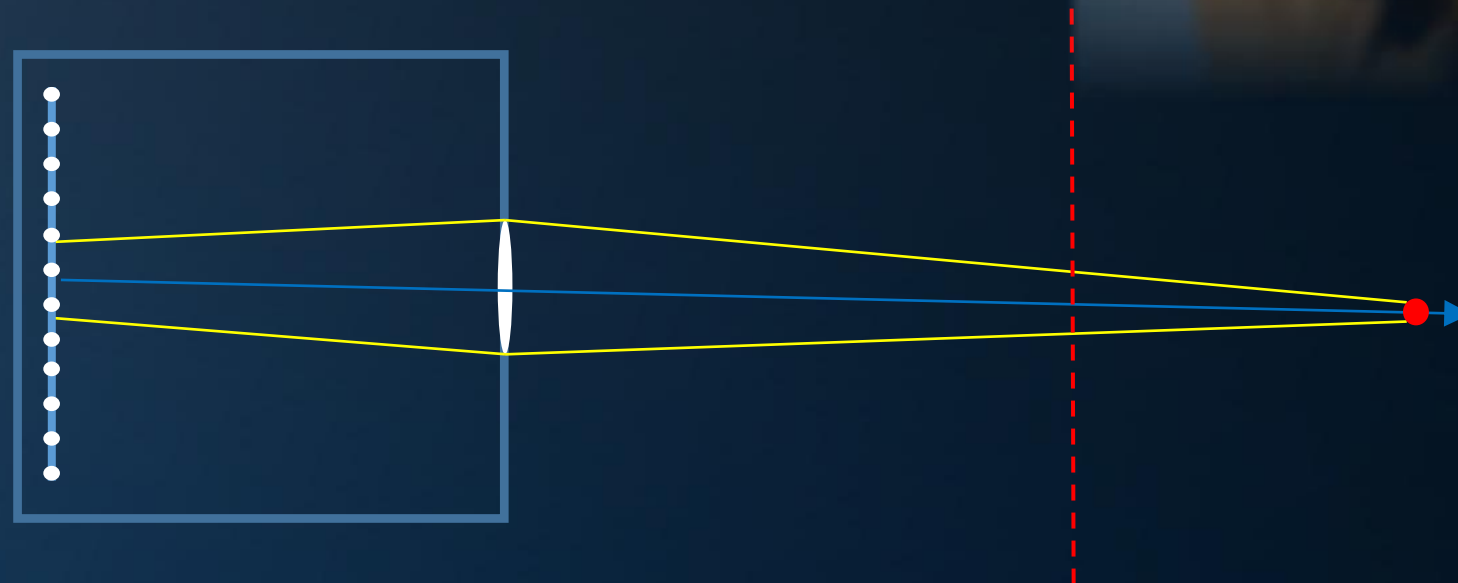
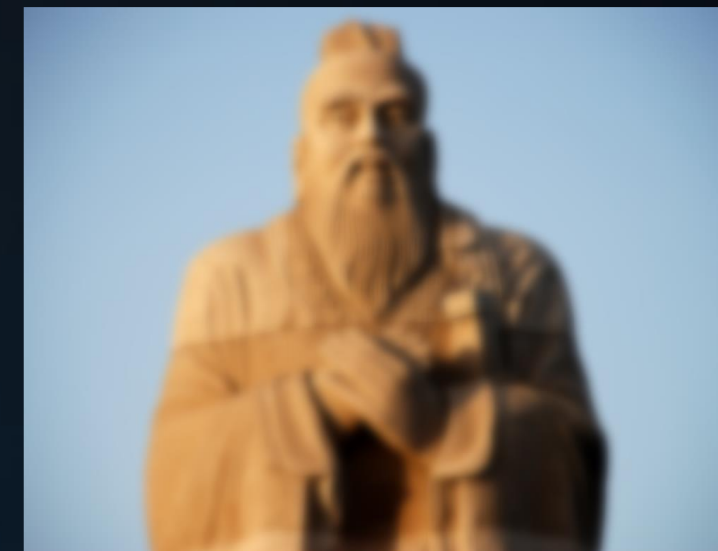


Depth of Field

Focus

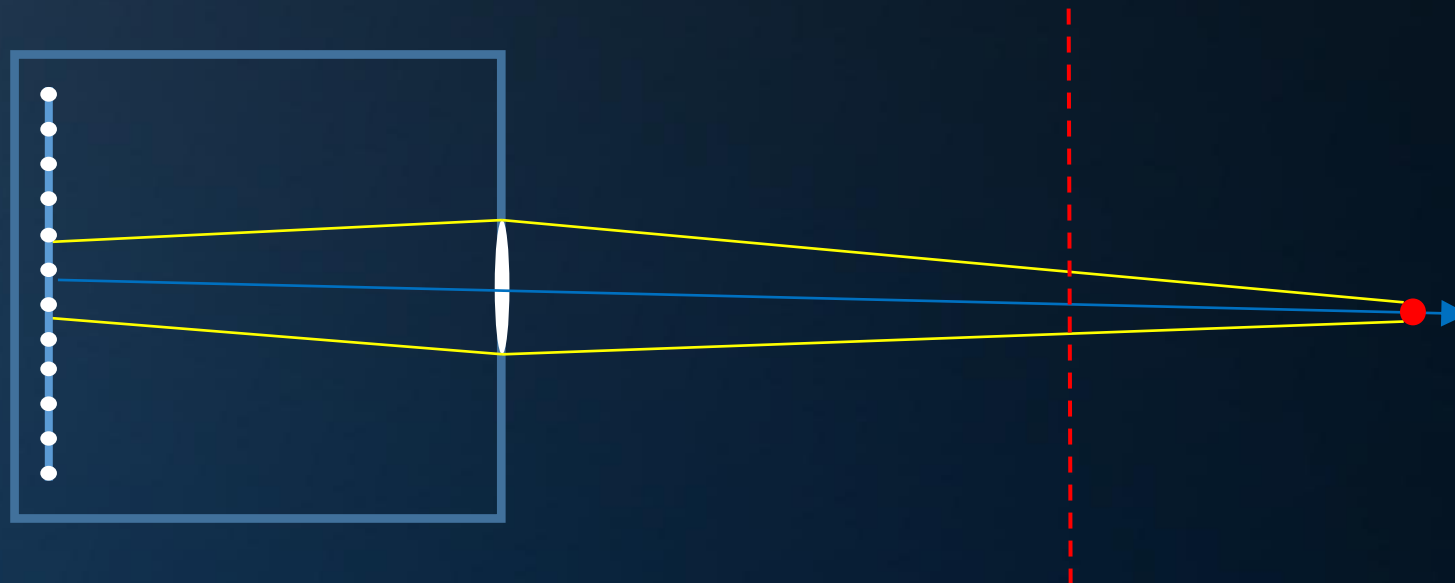
Objects beyond the focal plane also appear out of focus:

Light reflected from these objects is again spread out over several pixels on the film.



Circle of Confusion

Spreading out the energy returned by a single ray over multiple pixels within the circle of confusion.



Depth of Field

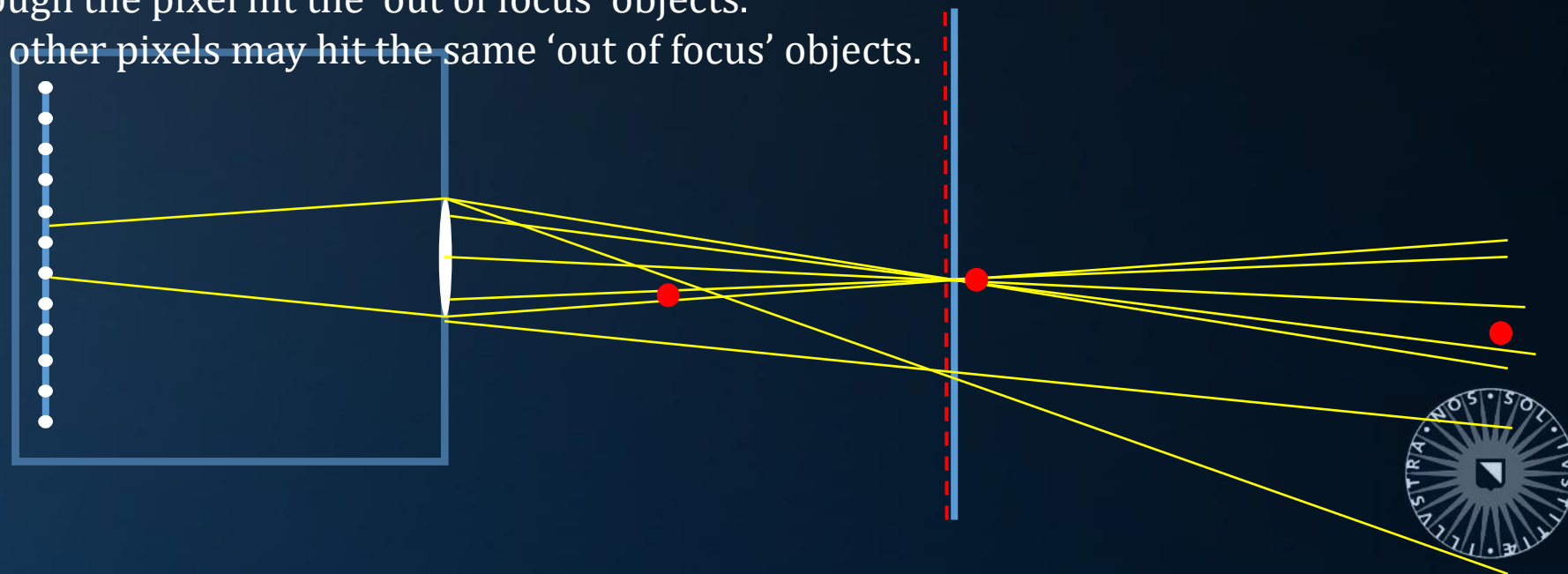
Circle of Confusion

Efficient depth of field:

We place the virtual screen plane at the focal distance (from the lens).

Rays are generated on the lens, and extend through each pixel.

- All rays through the pixel will hit the object near the focal plane;
- Few rays through the pixel hit the ‘out of focus’ objects.
- Rays through other pixels may hit the same ‘out of focus’ objects.



Depth of Field

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse,
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &light;
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psum;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Smith's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```

Generating Primary Rays

Placing the virtual screen plane at the focal distance:

Recall that a 2×2 square at distance d yielded a FOV that could be adjusted by changing d .

We can adjust d without changing FOV by scaling the square and d by the same factor.

Random point on the lens: generate an (ideally uniform) random point on a disc. This is non-trivial; see Global Illumination Compendium, 19a or b. Alternatively, you can use rejection sampling.

Also nice: replace the disc with a regular n-gon.

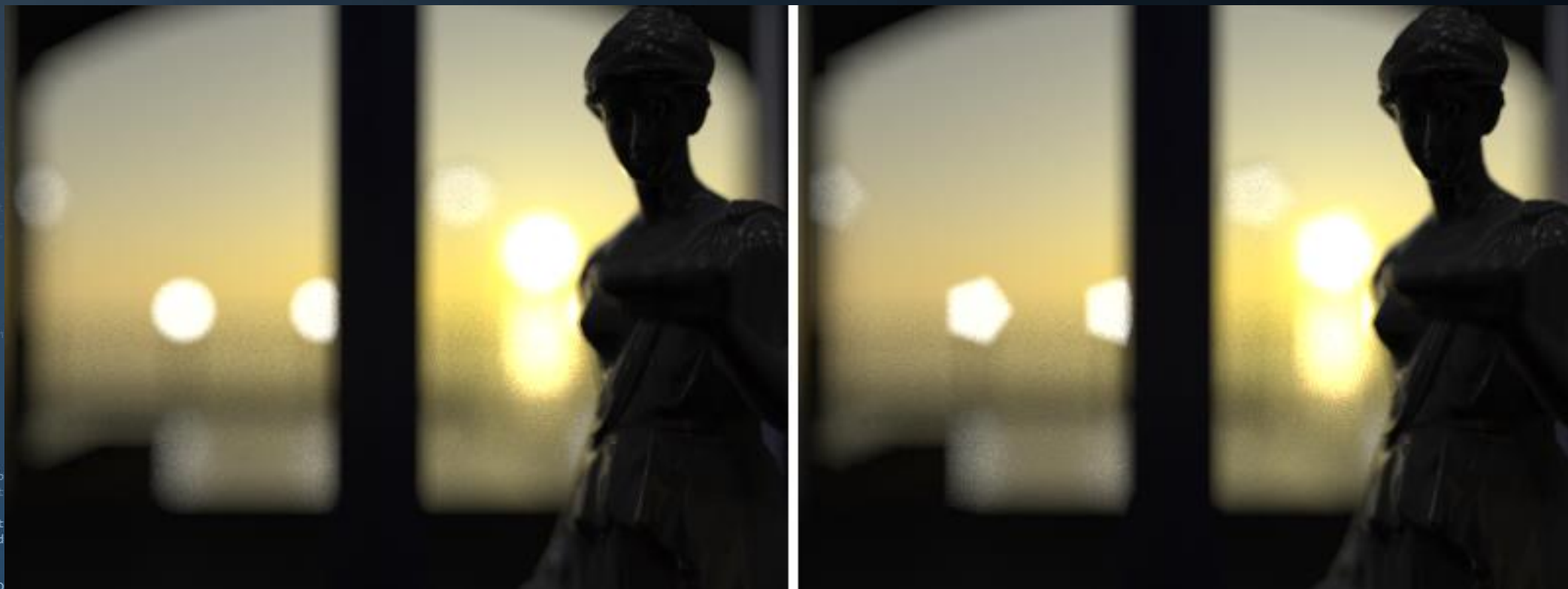


Depth of Field

```

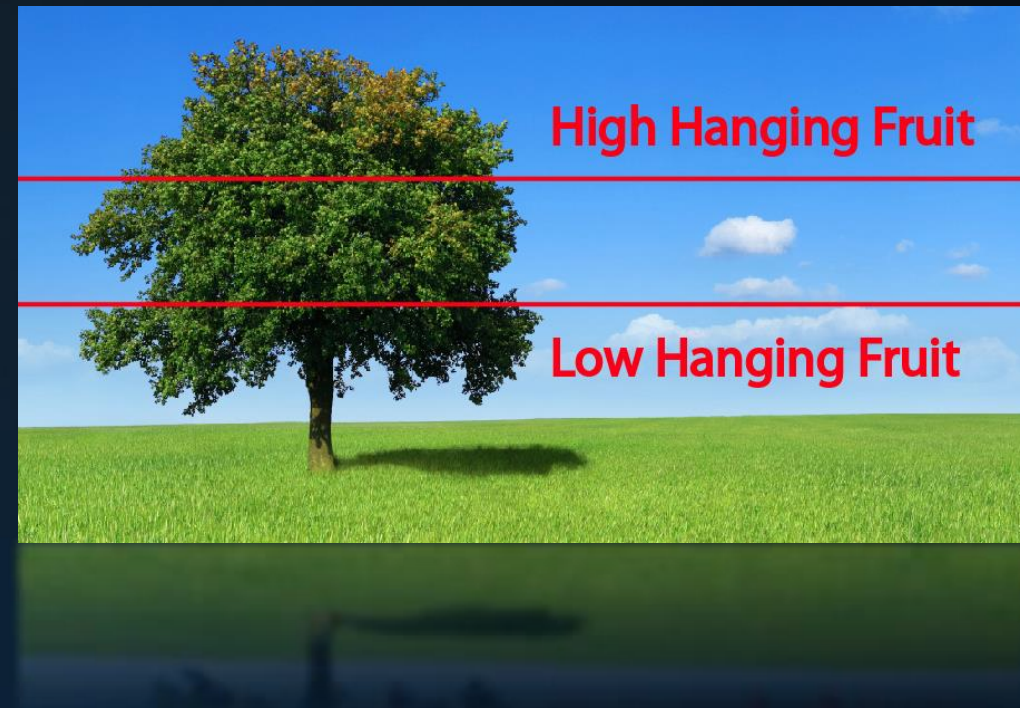
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt;
    at Tr = 1 - (R0 + (1 - R0) * cos2t);
    R = (D * nnt - N * a);
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability - doing it
    if;
    radiance = SampleLightSource(x, radiance.y + radiance.z);
    w = true;
    at brdfPdf = EvaluateDf;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance.x + radiance.y + radiance.z);
    random walk - done properly, closely following the path of light
    (live)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox
- Spots, IES Profiles
- Microfacets



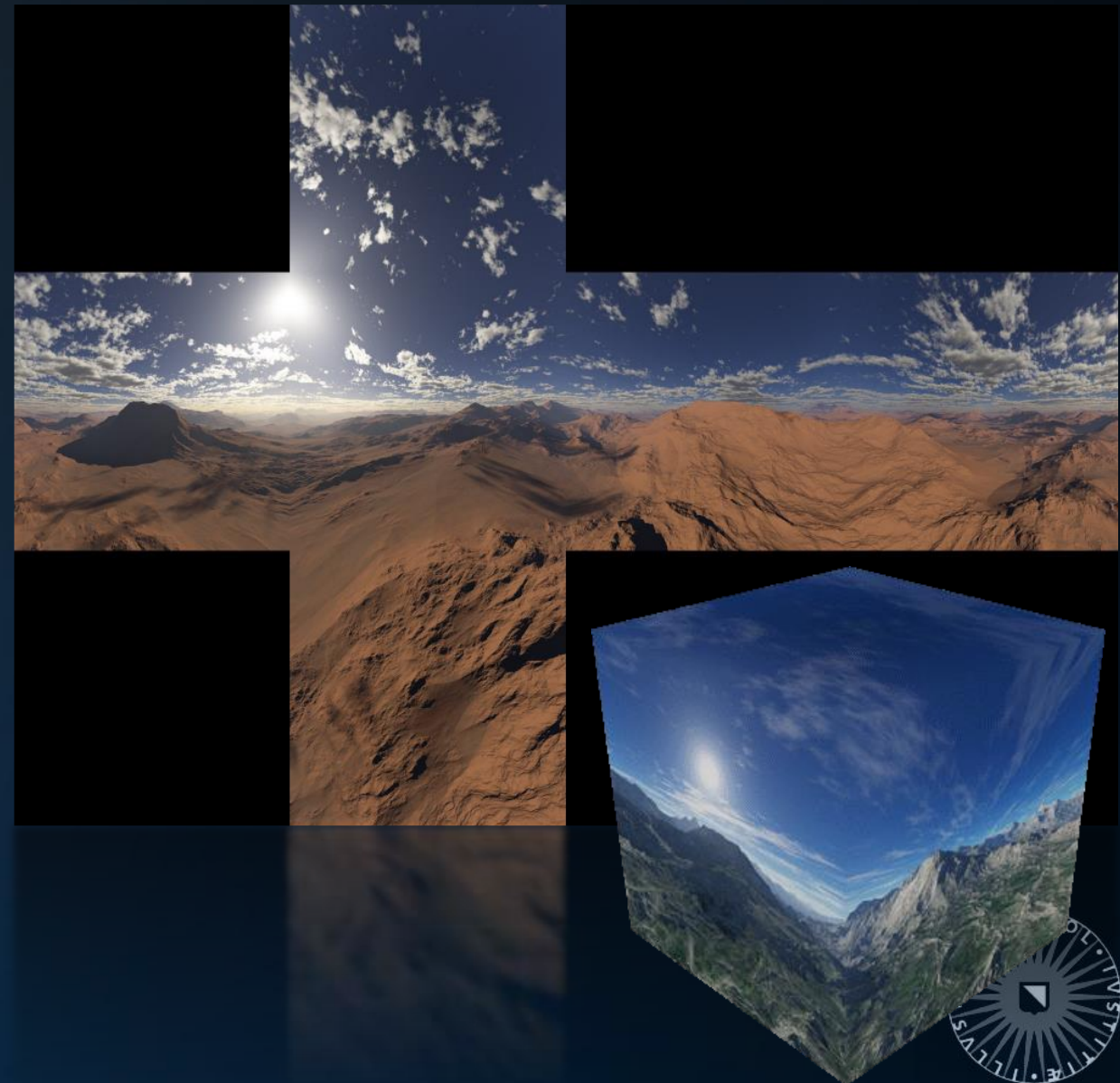
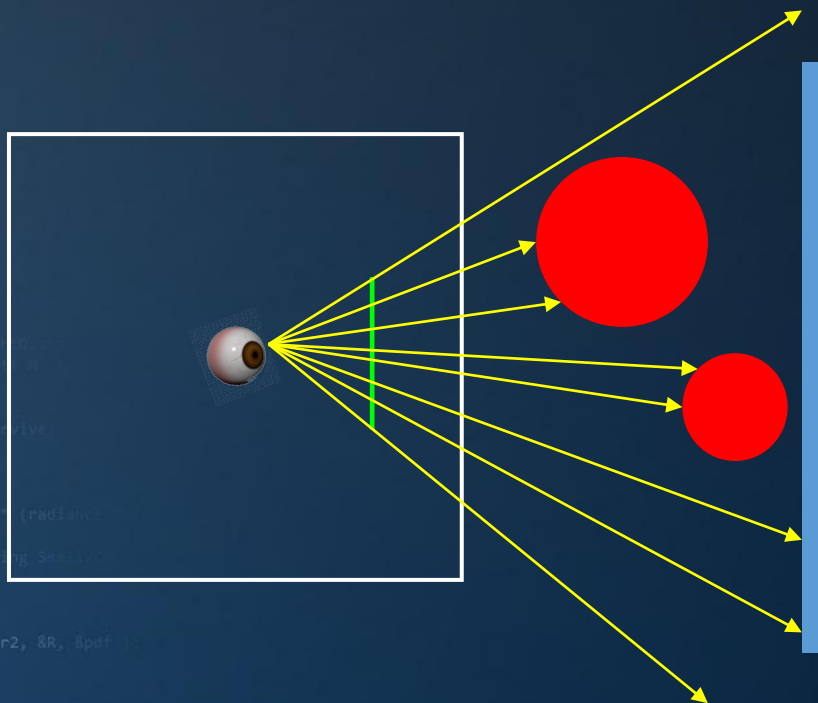
Skybox

Environment Imposter

Many games use a skybox to simulate distant geometry without actually storing this geometry.

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * cos2t);
    Tr) R = (D * nnt - N * (ddn * cos2t));
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse,
    estimation - doing it properly, closely
    df;
    radiance = SampleLight( &rand, I, &L, &light,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Sample
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
    
```



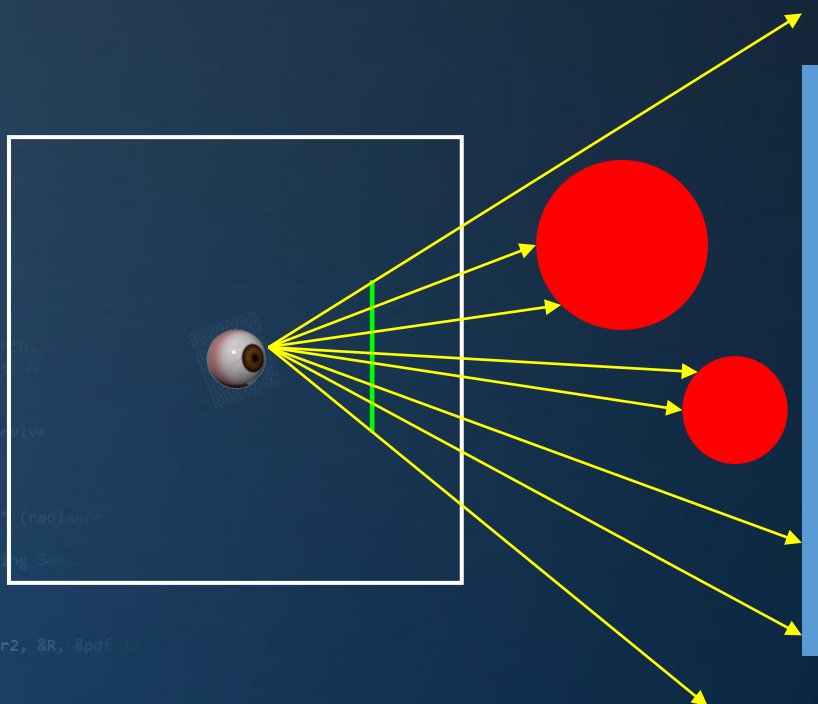
Skybox

Environment Imposter

Many games use a skybox to simulate distant geometry without actually storing this geometry.

The skybox is a $1 \times 1 \times 1$ box centered around the camera: assuming the sky is at an ‘infinite’ distance, the location of the camera inside this box is irrelevant.

Which face of the cubemap we need to use, and where it is hit by a ray is determined on ray direction alone.



Skybox

High Dynamic Range

Instead of using a skybox, we can also use an equirectangular mapping, which maps azimuth to u and elevation to v :

$$\theta = \pi(u - 1), \varphi = \pi v; \quad u = [0,2], \quad v = [0,1].$$

Converting polar coordinates to a unit vector:

$$\vec{D} = \begin{pmatrix} \sin(\varphi)\sin(\theta) \\ \cos(\varphi) \\ -\sin(\varphi)\cos(\theta) \end{pmatrix}$$

Reverse:

$$u, v = \begin{pmatrix} 1 + \text{atan2}(D_x, -D_z) / \pi \\ \text{acos}(D_y) / \pi \end{pmatrix}$$



Skybox

High Dynamic Range

You can find HDR panoramas on Paul Debevec's page:

<http://gl.ict.usc.edu/Data/HighResProbes>

Note:

A HDR skydome can be used as a light source.



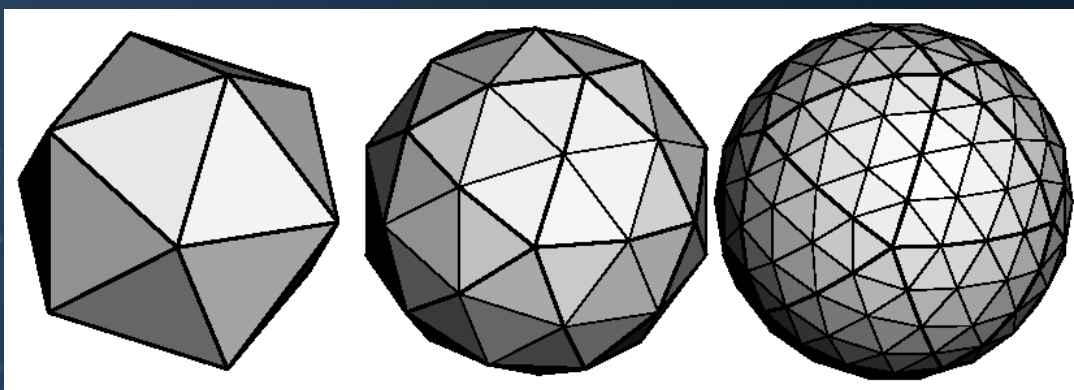
Skybox

Next Event Estimation for Skydomes

Useful trick:

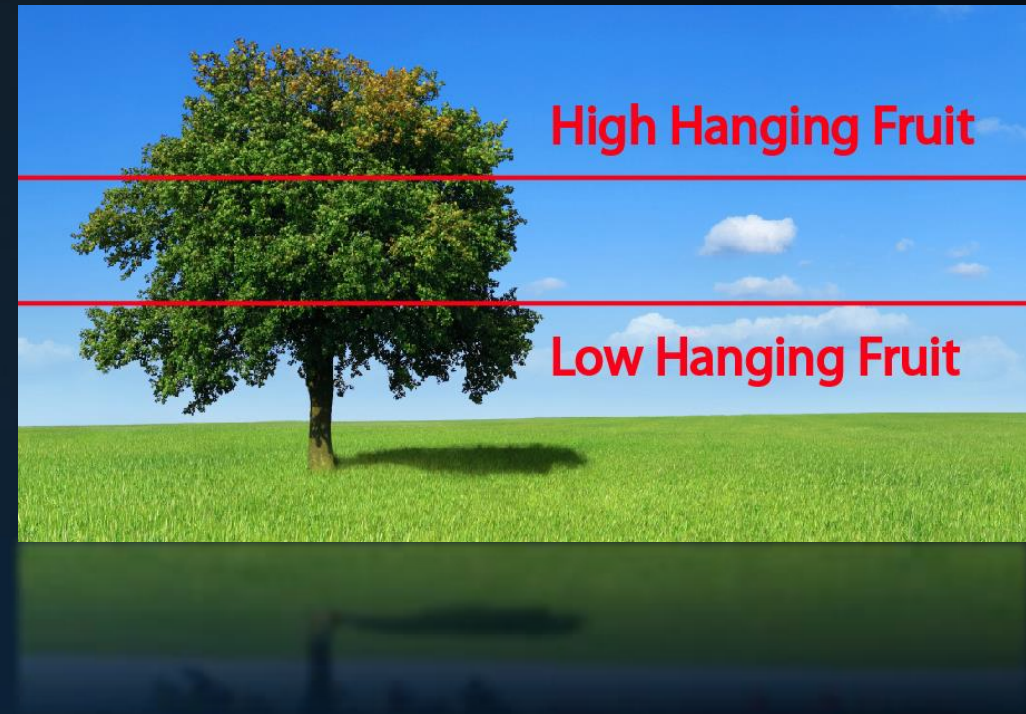
Use the original skydome only for rays that stumble upon it.

For next event estimation, use a tessellated (hemi)sphere; assign to each triangle the average skydome color for the directions it covers.



Today's Agenda:

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- Microfacets

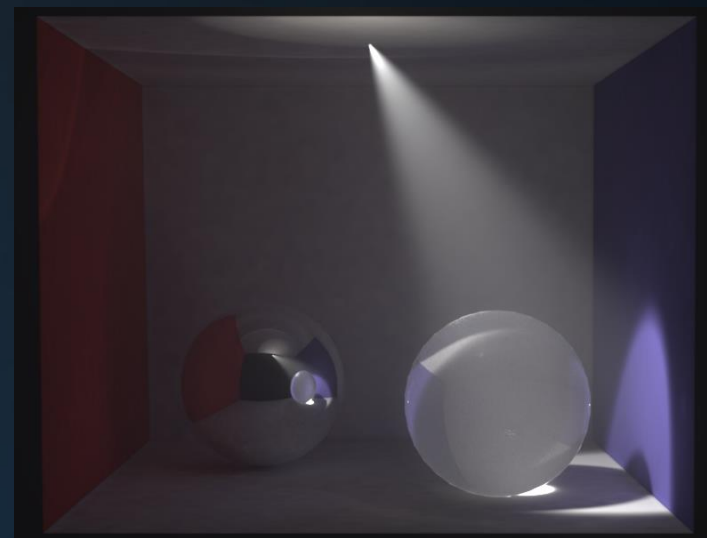


Spots & IES

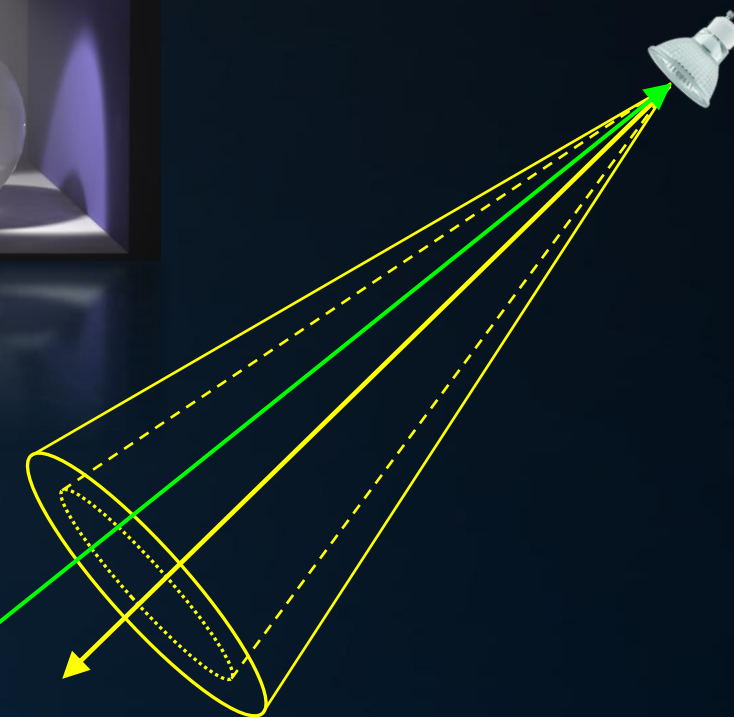
Ray Tracing Spotlights

Spotlight parameters:

- Brightness
- Position, direction
- Inner angle, outer angle



We can use importance sampling for spotlights, taking into account potential contribution based on these parameters.

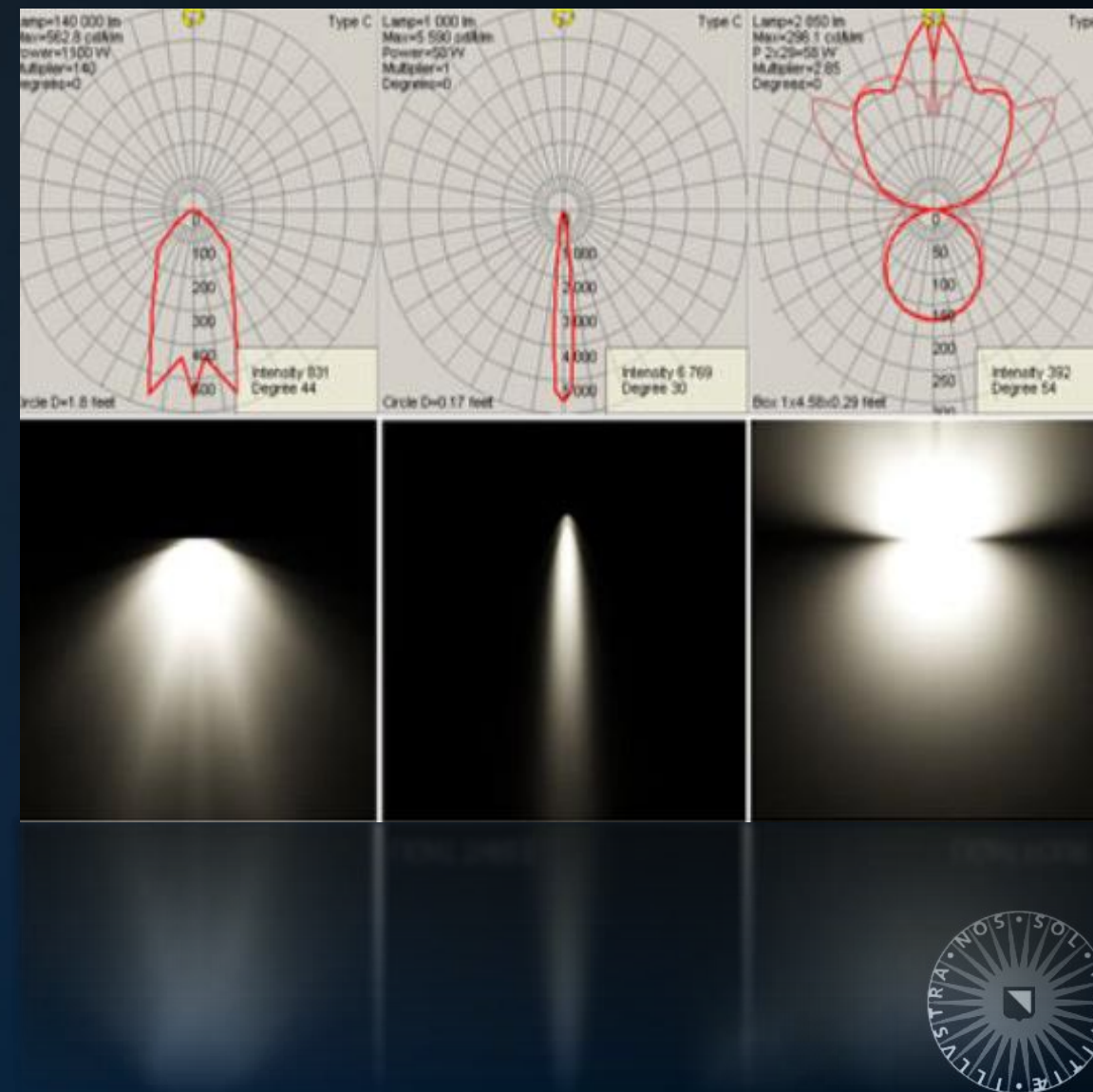


Spots & IES

IES Profiles

Photometric data for light sources:
Measurement of the distribution of light intensity.

Can be used in e.g. 3DS Max to model lights in virtual scenes.



Spots & IES

IESNA:LM-63-1995
[TEST] 21307
[MANUFAC]ECLIPSE LIGHTING - PENDANT LUMINAIRE
[LUMCAT]ME-XL1-QL165-277VOLT
[LUMINAIRE]WHITE PLASTIC TUBE WITH TOP AND BOTTOM OPEN
[LAMP]ONE PHILIPS 165 WATT INDUCTION LAMP
[LAMPCAT]QL165W/840. LUMEN RATING = 8289 LMS.
[OTHER]ONE PHILIPS QL165W S/1 GENERATOR OPERATING AT 277 VAC AND 147 WATTS
TILT=NONE

Format specification:
<http://lumen.iee.put.poznan.pl/kw/iesna.txt>

Lumens

1	8289	1	73	1	1	1	-1.00	0.00	1.92	1	1
147.0000											
0	2.5	5	7.5	10	12.5	15	17.5	20	22.5	25	27.5
30	32.5	35	37.5	40	42.5	45	47.5	50	52.5	55	57.5
60	62.5	65	67.5	70	72.5	75	77.5	80	82.5	85	87.5
90	92.5	95	97.5	100	102.5	105	107.5	110	112.5	115	117.5
120	122.5	125	127.5	130	132.5	135	137.5	140	142.5	145	147.5
150	152.5	155	157.5	160	162.5	165	167.5	170	172.5	175	177.5
180											
0	879.2	897.2	941.6	1001.1	1060.8	1116.3	1165.3	1171.1	1131.6	1064.3	
	986.6	910.8	845.1	792.7	760.3	745.7	735.6	724.5	714.6	703.8	
	693.0	683.0	675.6	672.1	672.0	673.9	675.9	677.6	679.3	680.9	
	682.3	682.9	682.7	681.2	678.5	676.6	680.7	684.8	683.3	680.9	
	676.9	671.2	664.1	655.9	646.6	636.3	625.0	612.7	599.6	586.1	
	572.3	558.1	544.0	530.5	517.8	506.6	496.4	486.5	477.0	469.6	
	470.0	482.8	502.2	520.6	526.0	496.0	414.4	315.6	235.7	169.7	
	108.4	59.4	35.8								

- Horizontal angles
- Vertical angle
- Candela values





Spots & IES

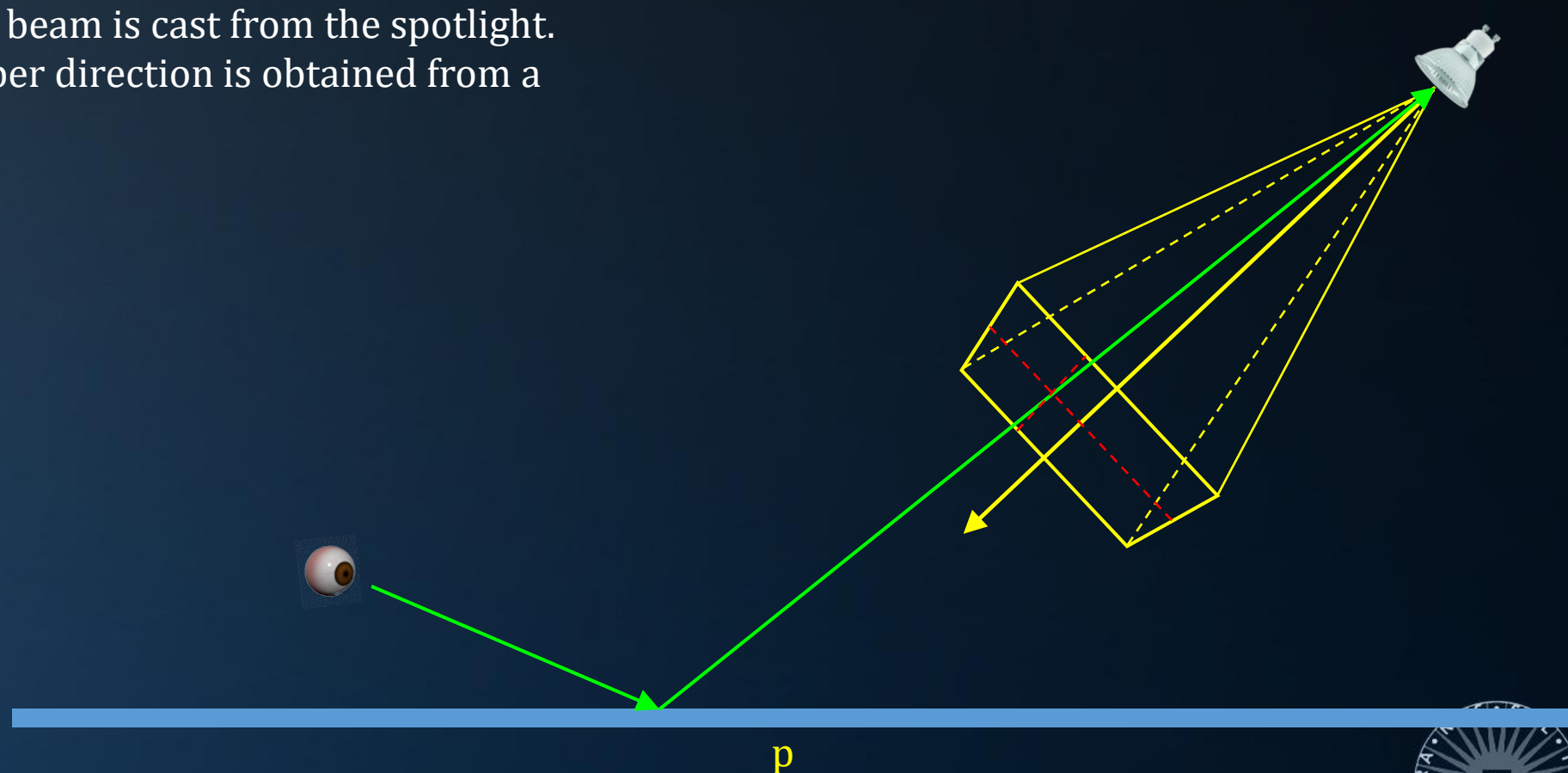
Projective Spotlight

A rectangular beam is cast from the spotlight.
Illumination per direction is obtained from a
bitmap.

$u, v = ?$

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nt;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;
    -
    efl + refr)) && (depth < MAXDEPTH)
    D, N );
    efl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &light,
    e.x + radiance.y + radiance.z > 0) && (dot(N,
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
    
```

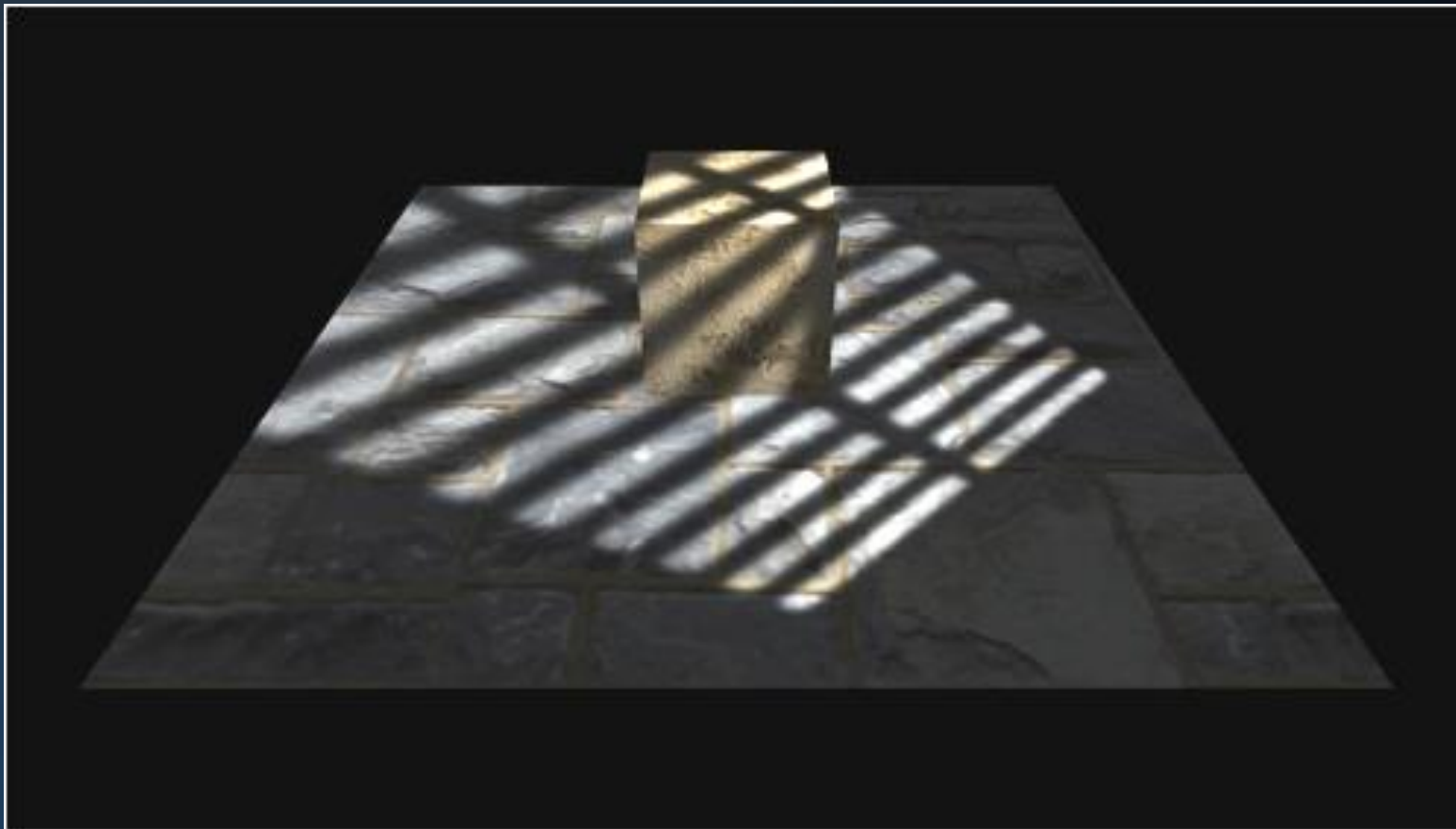


Spots & IES

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 1.0f - 0.5f * nnt)
    {
        nt = nt / nc, ddn = ddn * nc;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        Tr) R = (D * nnt - N * (ddn > 0 ? 1 : -1));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lightPos );
    e.x + radiance.y + radiance.z > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```



Spots & IES

```

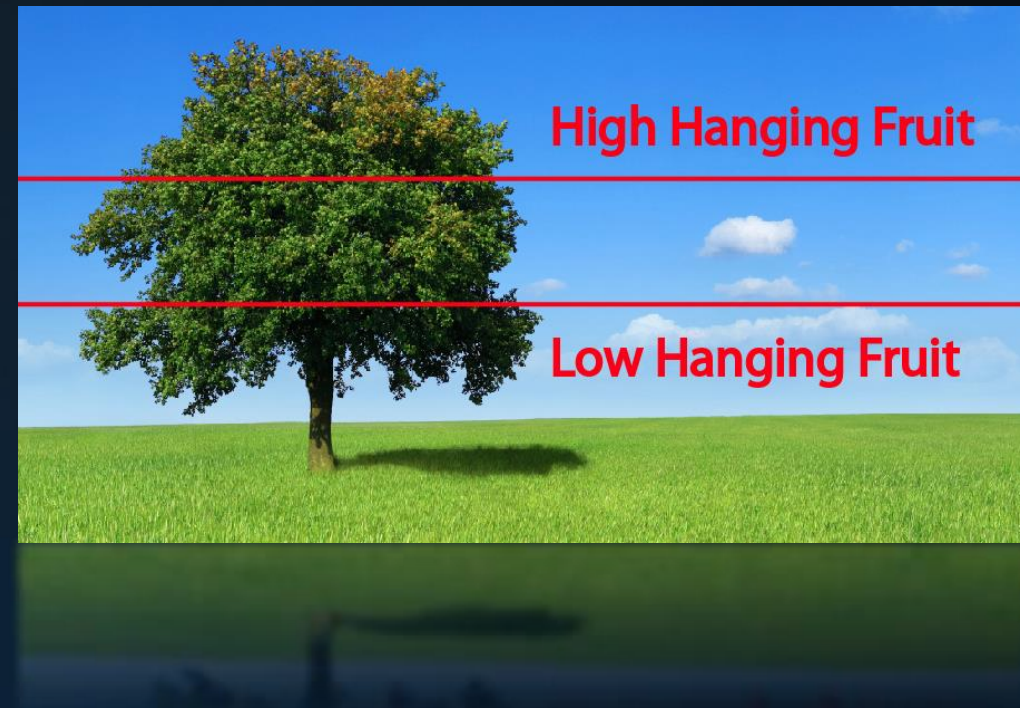
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = max(0, ddn);
        r2s2t = 1.0f - nnt * nnt;
        D, N );
    }
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * r2s2t);
        (Tr) R = (D * nnt - N * (ddn < 0 ? 1 : -1));
        E * diffuse;
        = true;
    }
    {
        refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse, 1);
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &align,
        e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radia
    random walk - done properly, closely following S
    ve)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R,
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}

```



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox
- Spots, IES Profiles
- Microfacets



Microfacet

BRDFs Without Issues

We have two BRDFs without problems:

1. The Lambertian BRDF
2. The pure specular BRDF

These are physically plausible and can be sampled. The PDF is also clear.



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0.25)
    {
        nt = nt / nc; ddn = dot(N, L);
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
}

```

```

at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) * ddn);
Tr) R = (D * nnt - N * (ddn *

```

```

E * diffuse;
= true;

```

```

efl + refr)) && (depth < MAXDEPTH)

```

```

D, N );
refl * E * diffuse;
= true;

```

```

MAXDEPTH)

```

```

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following
df;

```

```

radiance = SampleLight( &rand, I, &L, &lightPos );
e.x + radiance.y + radiance.z) > 0) && (depth <

```

```

w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance

```

```

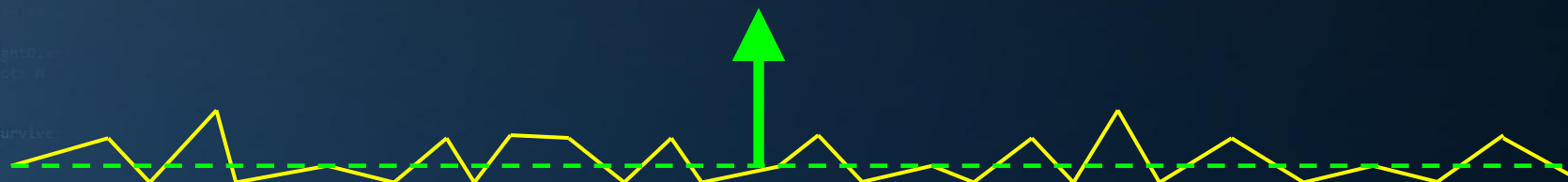
random walk - done properly, closely following Small's
vive)

```

```

;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



Microfacet

Microfacet BRDFs*

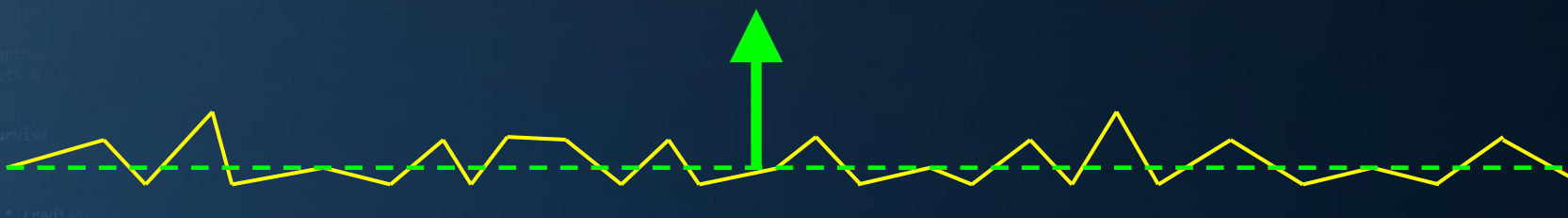
We can simulate a broad range of materials if we assume:
at a microscopic level, the material consists of tiny specular fragments.

- If the fragment orientations are chaotic, the material appears diffuse.
- If the fragment orientations are all the same, the material appears specular.
- Different but similar orientations yield glossy materials.



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = dot(N, N);
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Tr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse,
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &light;
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following SampleLight
    vive)
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2);
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
  
```



*: Torrance & Sparrow, Theory for Off-Specular Reflection from Roughened Surfaces. 1967.



Microfacet BRDFs*

The Microfacet BRDF:

$$f_r(\vec{L}, \vec{V}) = \frac{F(\vec{L}, \vec{V})G(\vec{L}, \vec{V}, \vec{H})D(\vec{H})}{4(\vec{N} \cdot \vec{L})(\vec{N} \cdot \vec{V})}$$

Ingredients:

1. Normal distribution D
2. Geometry term G
3. Fresnel term F
4. Normalization



Microfacet

Normal Distribution

$$f_r(x, \theta_i, \theta_o) = \frac{L_o(x, \theta_o)}{L_i(x, \theta_i) \cos \theta_i}$$

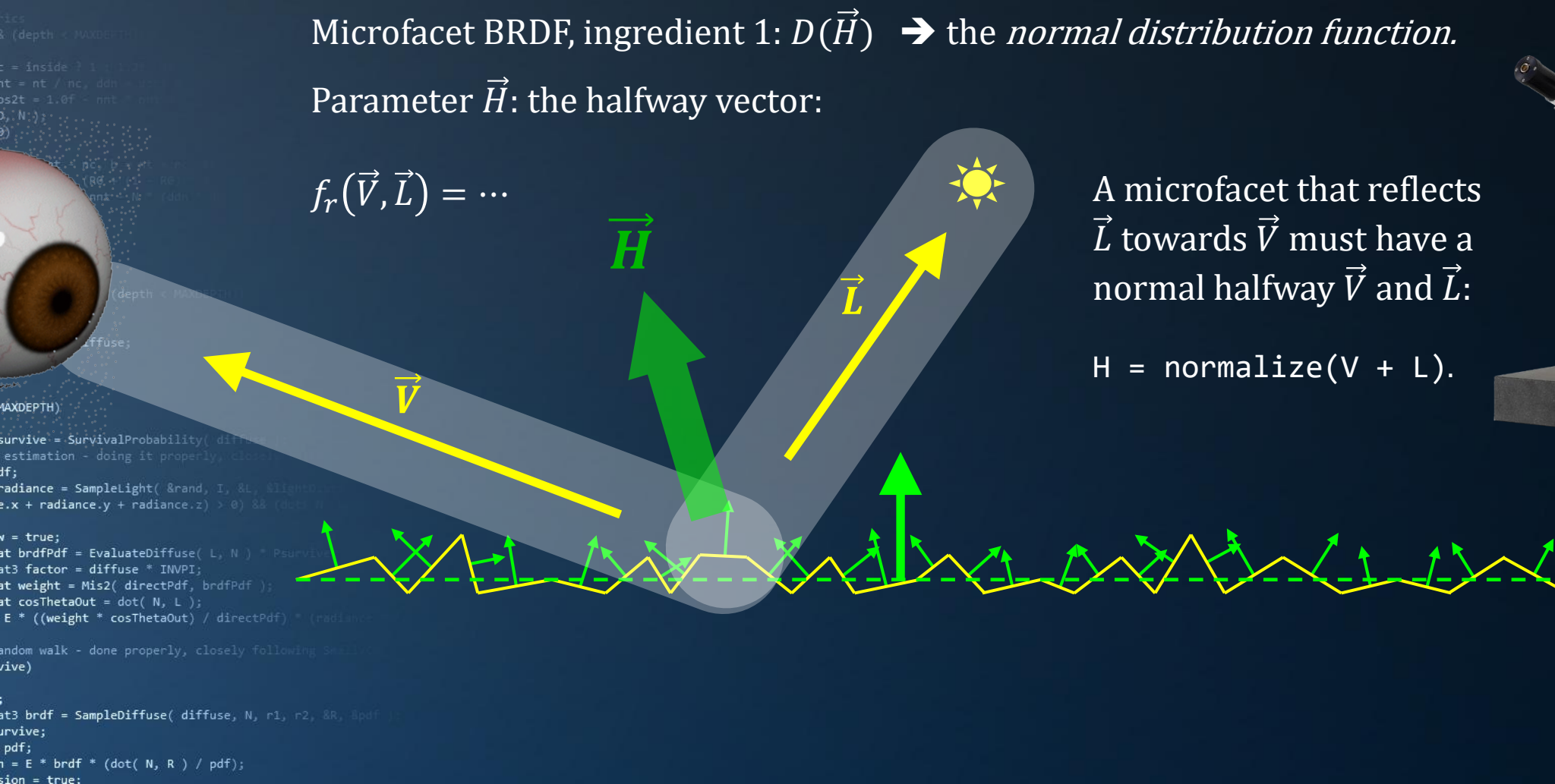
Microfacet BRDF, ingredient 1: $D(\vec{H}) \rightarrow$ the *normal distribution function*.

Parameter \vec{H} : the halfway vector:

$$f_r(\vec{V}, \vec{L}) = \dots$$

A microfacet that reflects \vec{L} towards \vec{V} must have a normal halfway \vec{V} and \vec{L} :

$$\vec{H} = \text{normalize}(\vec{V} + \vec{L}).$$



Intuitive choices for D:

$$D(\vec{H}) = \begin{cases} \infty, & \text{for } \vec{H} = (0,0,1) \\ 0, & \text{otherwise} \end{cases} : \text{all microfacet normals are } (0,0,1) \rightarrow \text{pure specular.}$$

Good practical choice for D : the Blinn-Phong distribution;

$$D(\vec{H}) = \frac{\alpha + 2}{2\pi} (\vec{N} \cdot \vec{H})^\alpha$$



Microfacet

Geometry Term

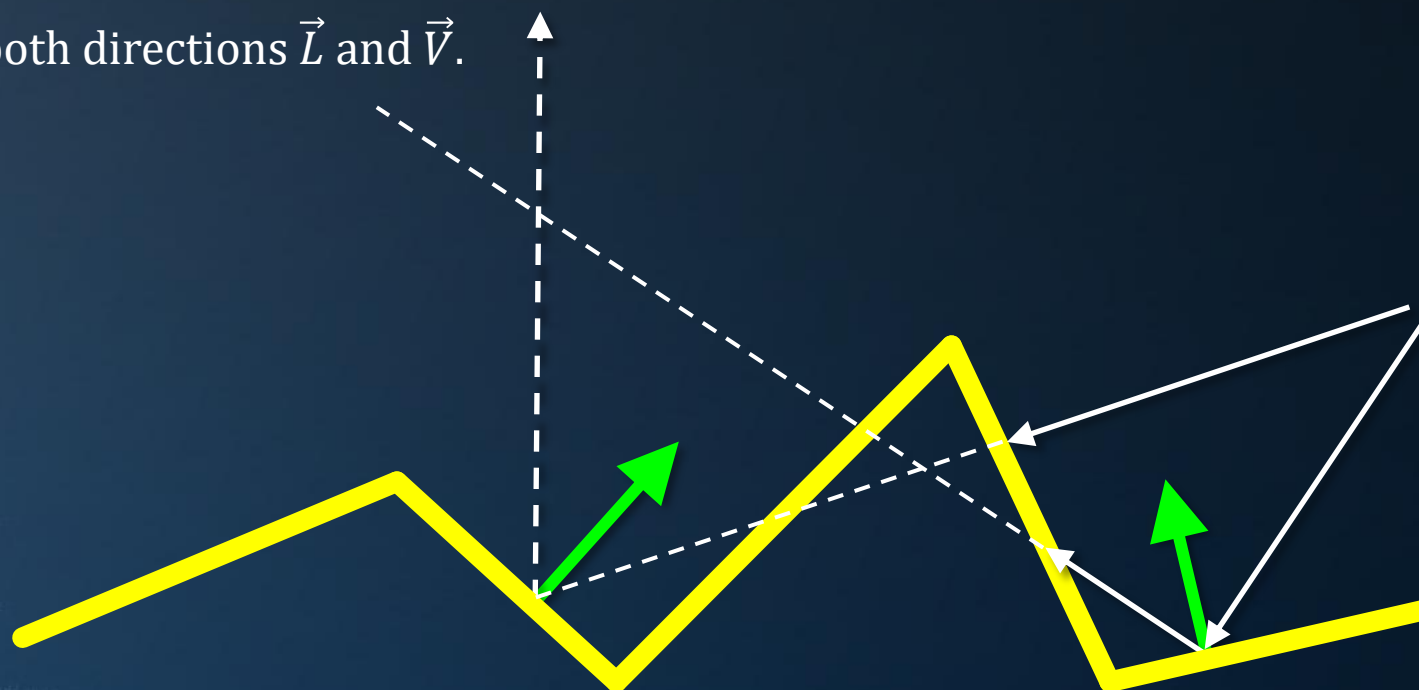
Microfacet BRDF, ingredient 2: $G(\vec{V}, \vec{L}, \vec{H}) \rightarrow$ the *geometry term*.

It describes what fraction of a microsurface with normal \vec{H} is visible in both directions \vec{L} and \vec{V} .

Geometry Term

Microfacet BRDF, ingredient 2: $G(\vec{V}, \vec{L}, \vec{H}) \rightarrow$ the *geometry term*.

It describes what fraction of a microsurface with normal \vec{H} is visible in both directions \vec{L} and \vec{V} .



Microfacet

Geometry Term

Intuitive choice for G:

$G(\vec{V}, \vec{L}, \vec{H}) = 1$: no occlusion.

Good practical choice for G*:

$$G(\vec{V}, \vec{L}, \vec{H}) = \min(1, \min\left(\frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{V})}{\vec{V} \cdot \vec{H}}, \frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{L})}{\vec{V} \cdot \vec{H}}\right))$$

*: Physically Based Rendering, page 455



Microfacet

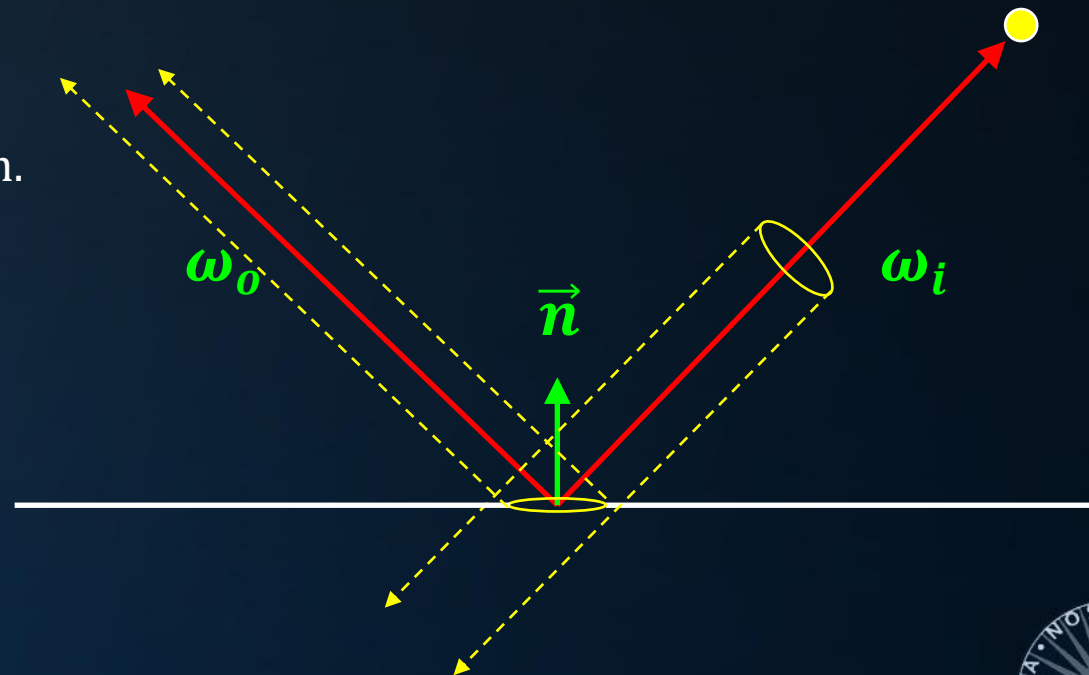
Fresnel Term

Microfacet BRDF, ingredient 3: $F(\vec{L}, \vec{H}) \rightarrow$ the *Fresnel term*.

So far, we assumed that the light reflected by a specular surface is only modulated by the material color.

This is not true for dielectrics: here we use the Fresnel equations to determine reflection.

In nature, Fresnel does not just apply to dielectrics.



Microfacet

Fresnel Term

Iron is specular, but reflectivity differs depending on incident angle.

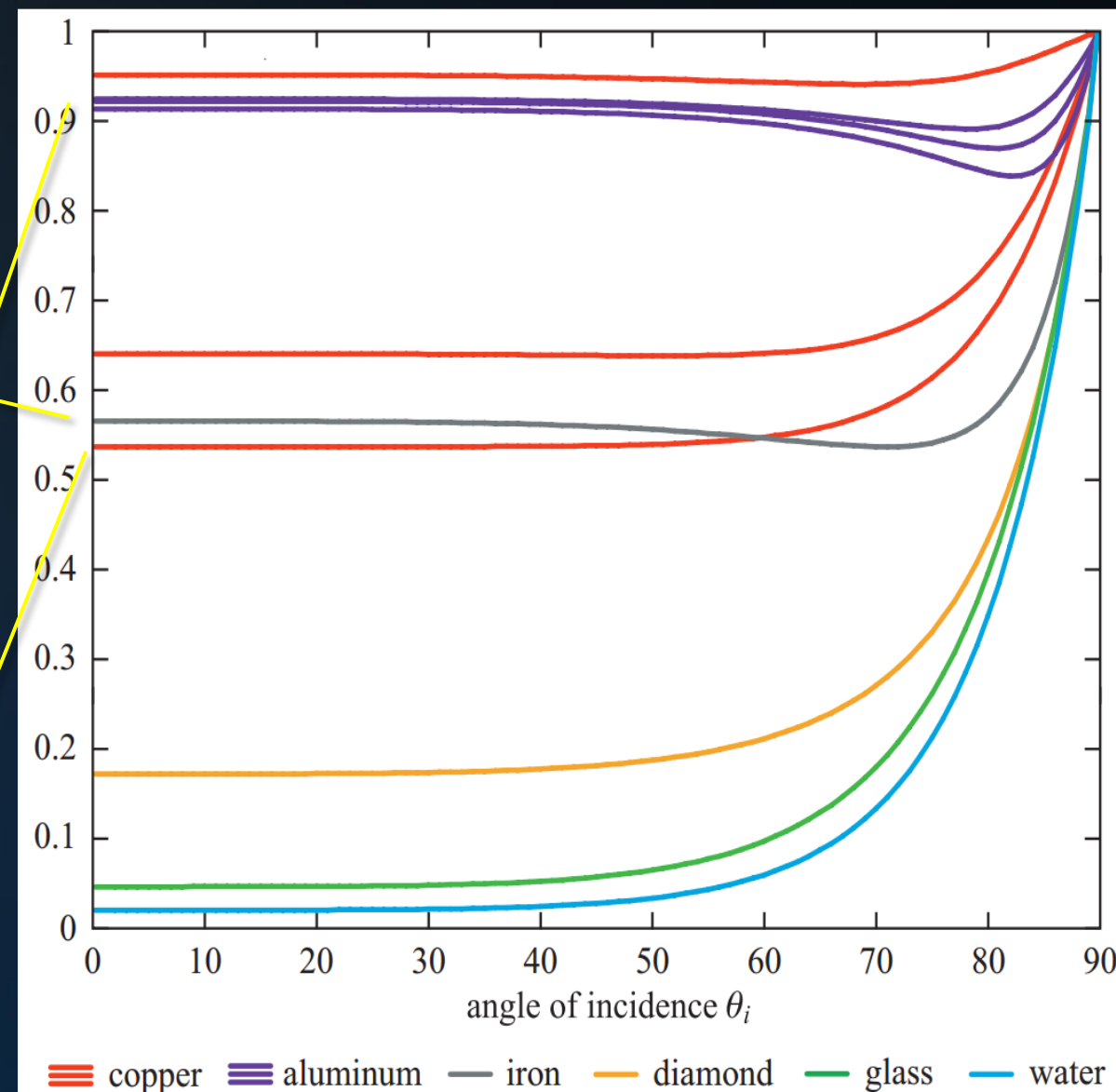
Aluminum is even more interesting: reflectivity depends on wavelength. The three lines in the graph:

Top: blue, middle: green, bottom: red.

Copper takes this to extremes: at grazing angles, it appears white. The lines in the graph:

Top: red, middle: green, bottom: blue.

(hence its reddish appearance)



From "Real-time Rendering, 3rd edition, A. K. Peters.

Microfacet

Fresnel Term

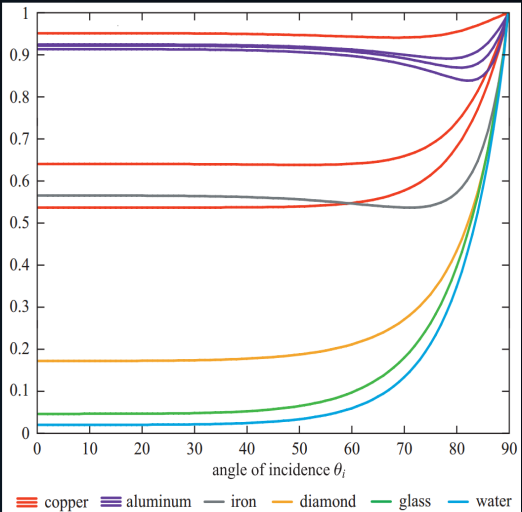
For Fresnel, we use Schlick's approximation:

$$F_r = k_{specular} + (1 - k_{specular})(1 - (\vec{L} \cdot \vec{H}))^5$$

Note that this is calculated per color channel ($k_{specular}$ is an rgb triplet).

Values for $k_{specular}$ for various materials:

Iron	0.56, 0.57, 0.58
Copper	0.95, 0.64, 0.54
Gold	1.00, 0.71, 0.29
Aluminum	0.91, 0.92, 0.92
Silver	0.95, 0.93, 0.88



Microfacet

Bringing it All Together

The Microfacet BRDF:

$$f_r(\vec{L}, \vec{V}) = \frac{F(\vec{L}, \vec{V})G(\vec{L}, \vec{V}, \vec{H})D(\vec{H})}{4(\vec{N} \cdot \vec{L})(\vec{N} \cdot \vec{V})}$$

$$D(\vec{H}) = \frac{\alpha + 2}{2\pi} (\vec{N} \cdot \vec{H})^\alpha$$

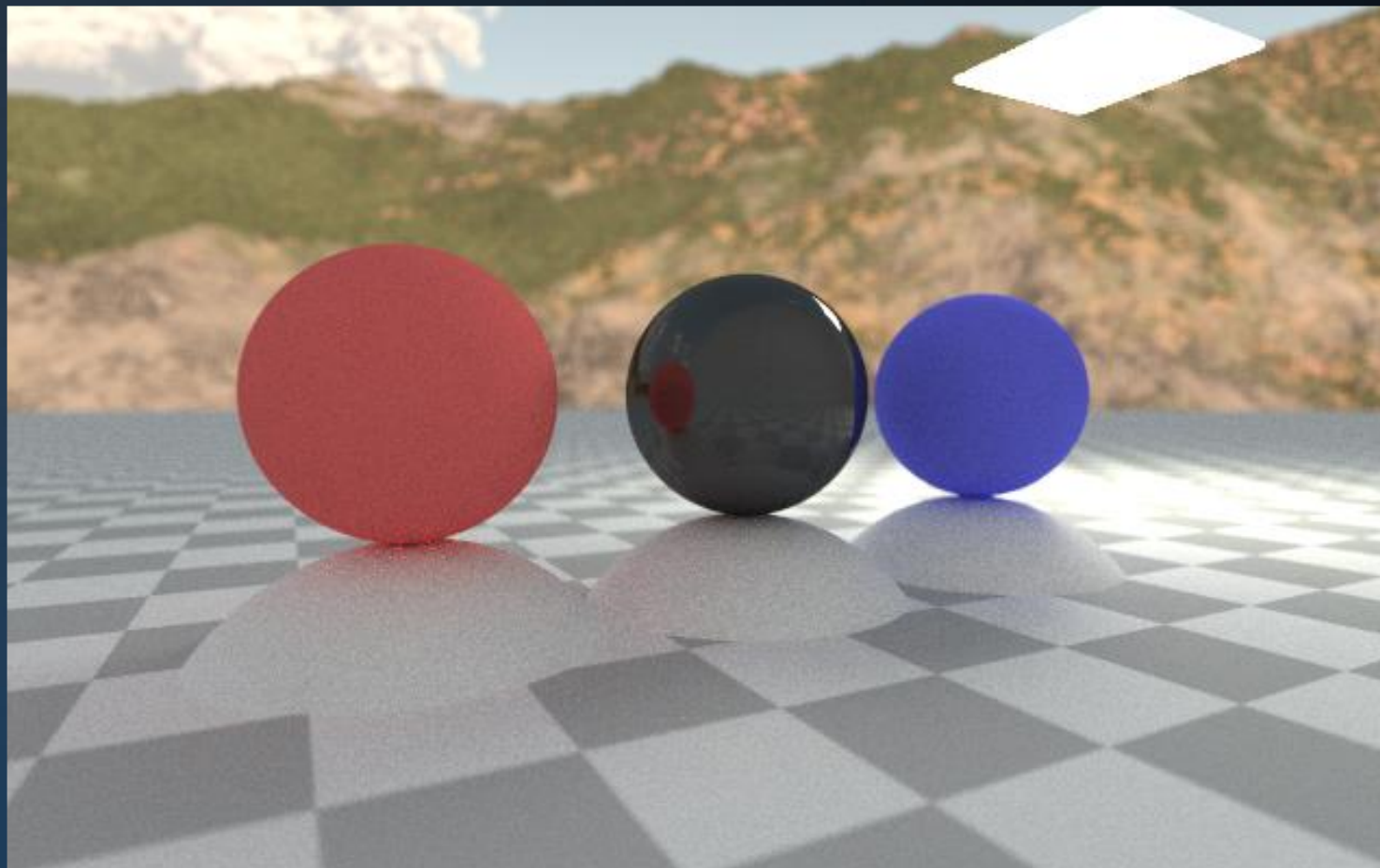
$$G(\vec{V}, \vec{L}, \vec{H}) = \min(1, \min\left(\frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{V})}{\vec{V} \cdot \vec{H}}, \frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{L})}{\vec{V} \cdot \vec{H}}\right))$$

For a full derivation of the denominator of the BRDF, see Physically Based Rendering, section 8.4.2.

$$F_r = k_{specular} + (1 - k_{specular})(1 - (\vec{L} \cdot \vec{H}))^5$$



Microfacet



Lambertian BRDF

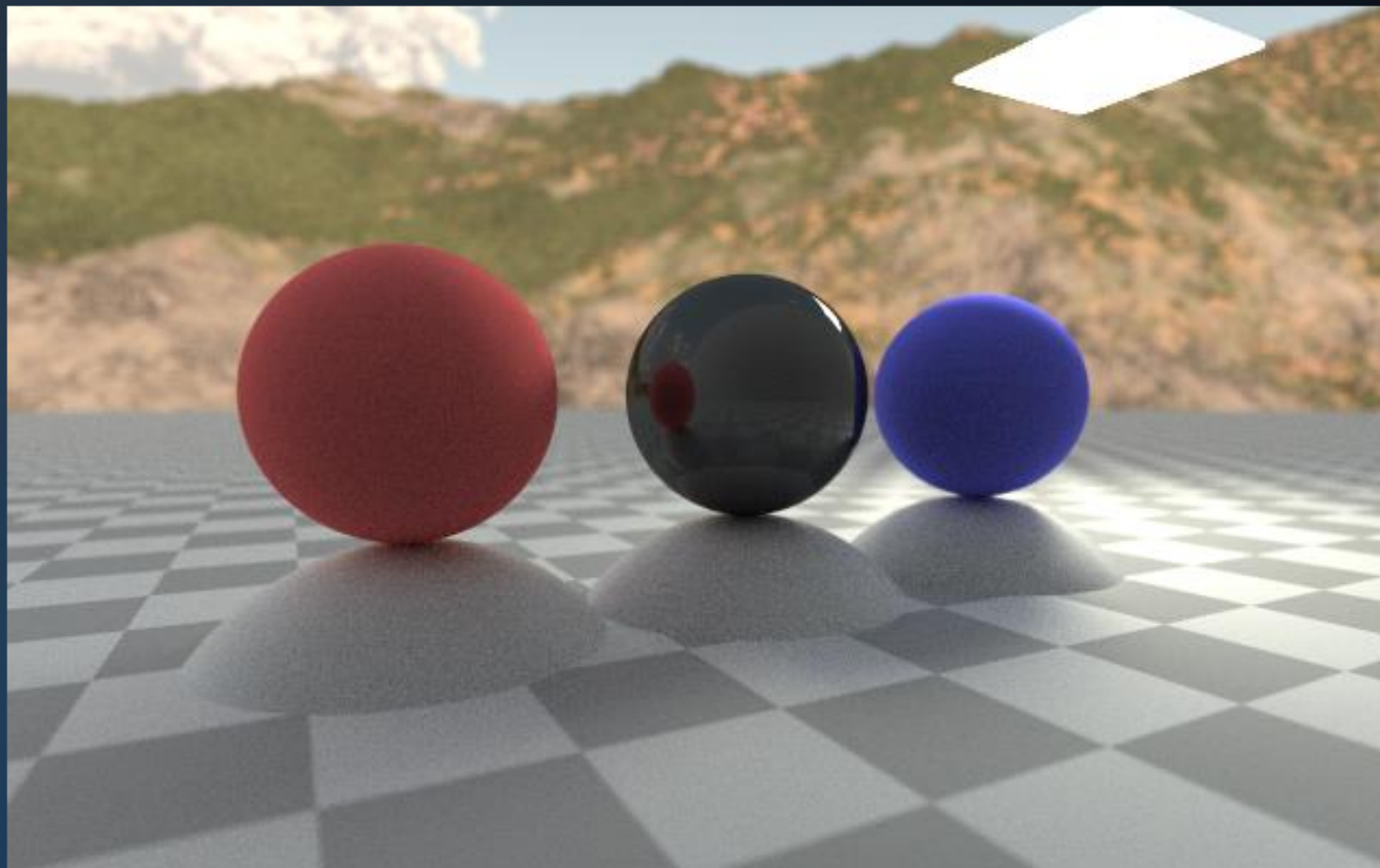


Microfacet

```

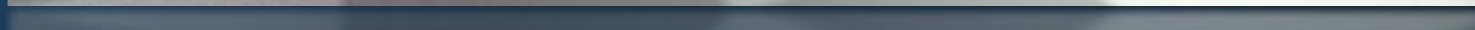
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0.5)
    {
        nt = nt / nc; ddn = dot(N, D);
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        (Tr) R = (D * nnt - N * (ddn < 0 ? 1 : -1));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &align, &pdf );
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;

```



Blinn-Phong Microfacet BRDF, $\alpha=1$



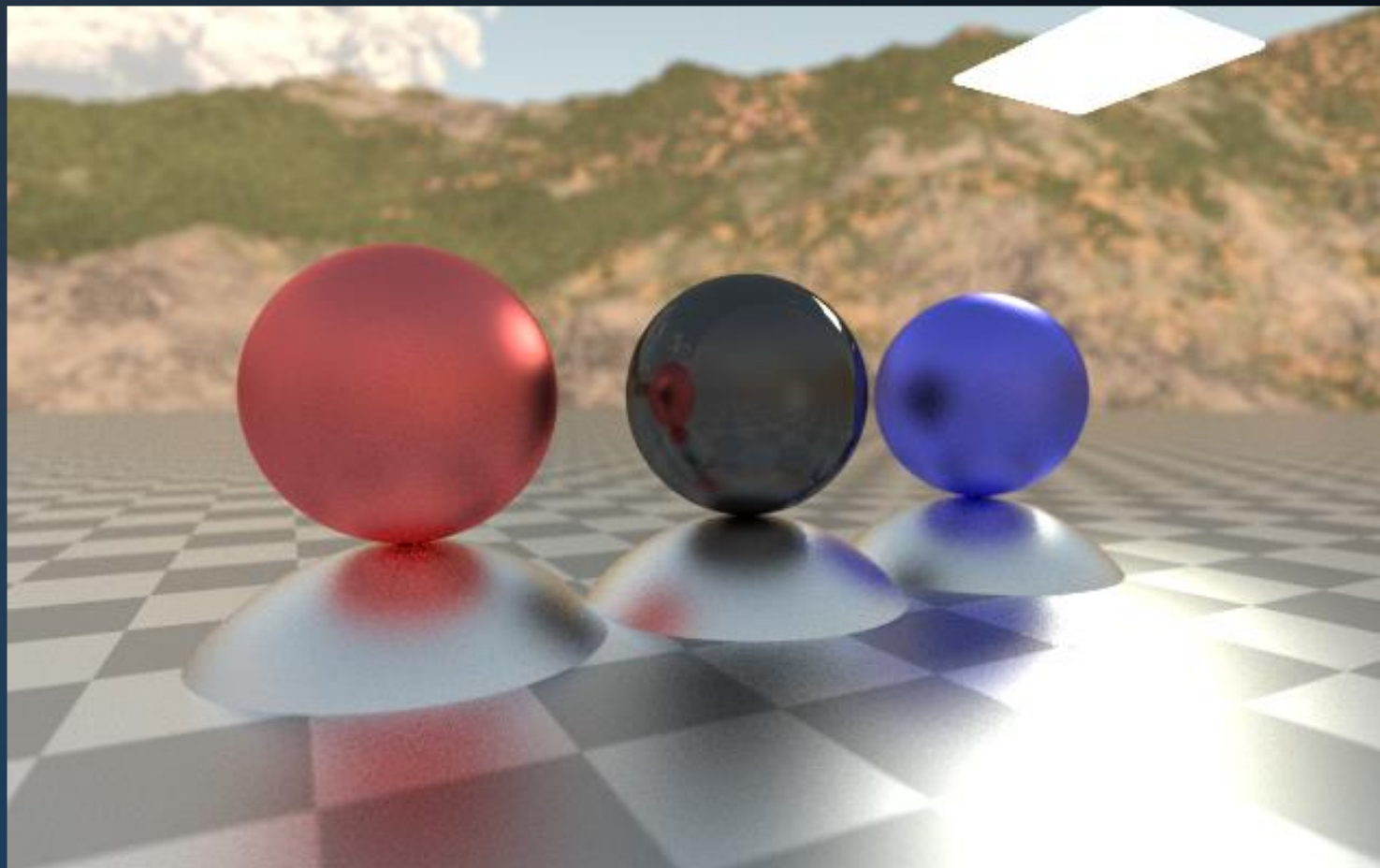


Microfacet

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nt;
        rnt = 1.0f - nnt * nnt;
        D, N );
    }
    {
        at a = nt - nc; b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * rnt);
        (Tr) R = (D * nnt - N * (ddn * rnt));
    }
    E * diffuse;
    = true;
}
{
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &align, &pdf );
    e.x + radiance.y + radiance.z > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following Small's
    (survive)
    {
        at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
        survive;
        pdf;
        n = E * brdf * (dot( N, R ) / pdf);
        sion = true;
    }
}

```



Blinn-Phong Microfacet BRDF, $\alpha=50$

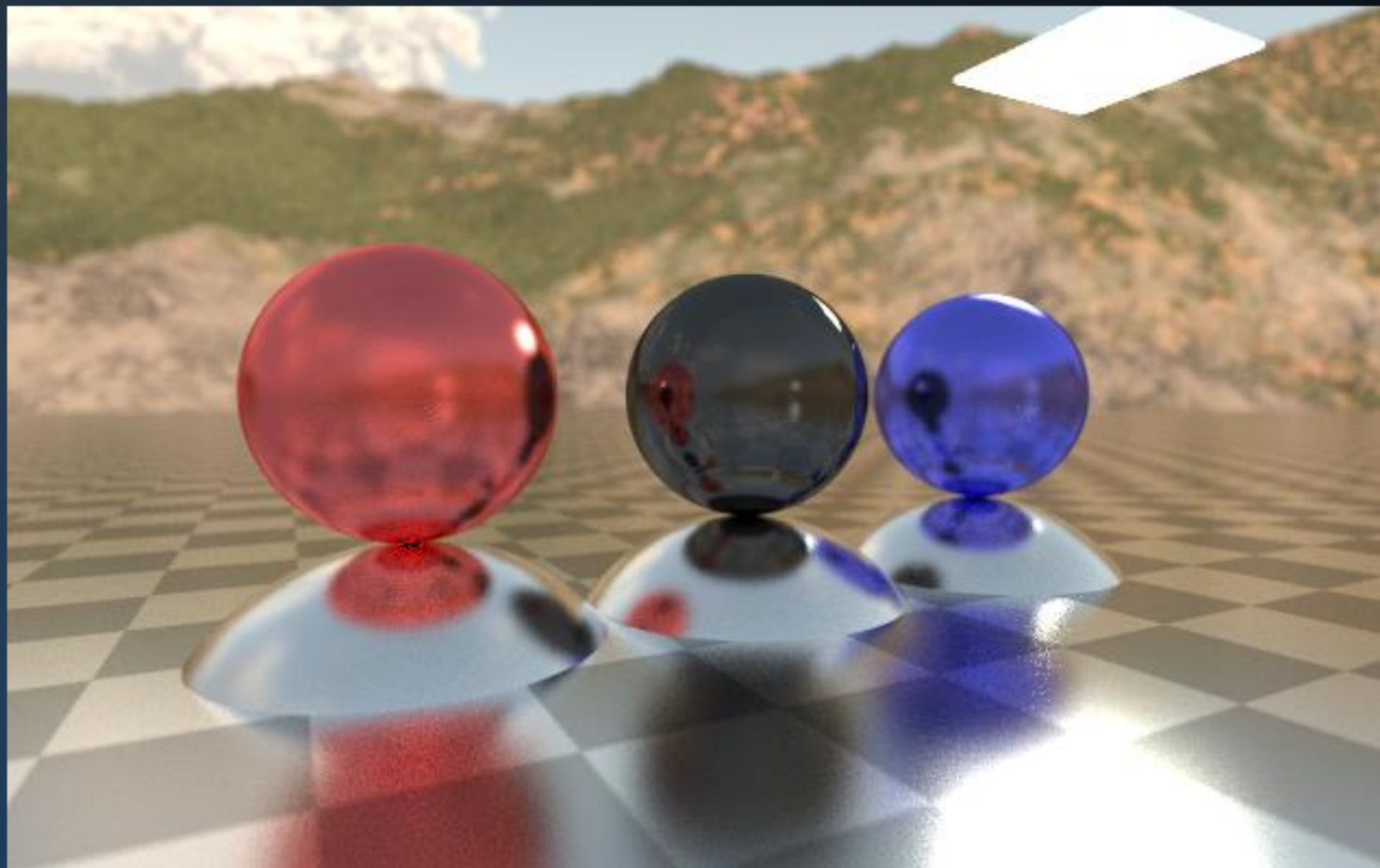


Microfacet

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0.5)
    {
        nt = nt / nc, ddn = ddn * nc;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        Tr) R = (D * nnt - N * (ddn < 0 ? 1 : 0));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &align, &pdf );
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}

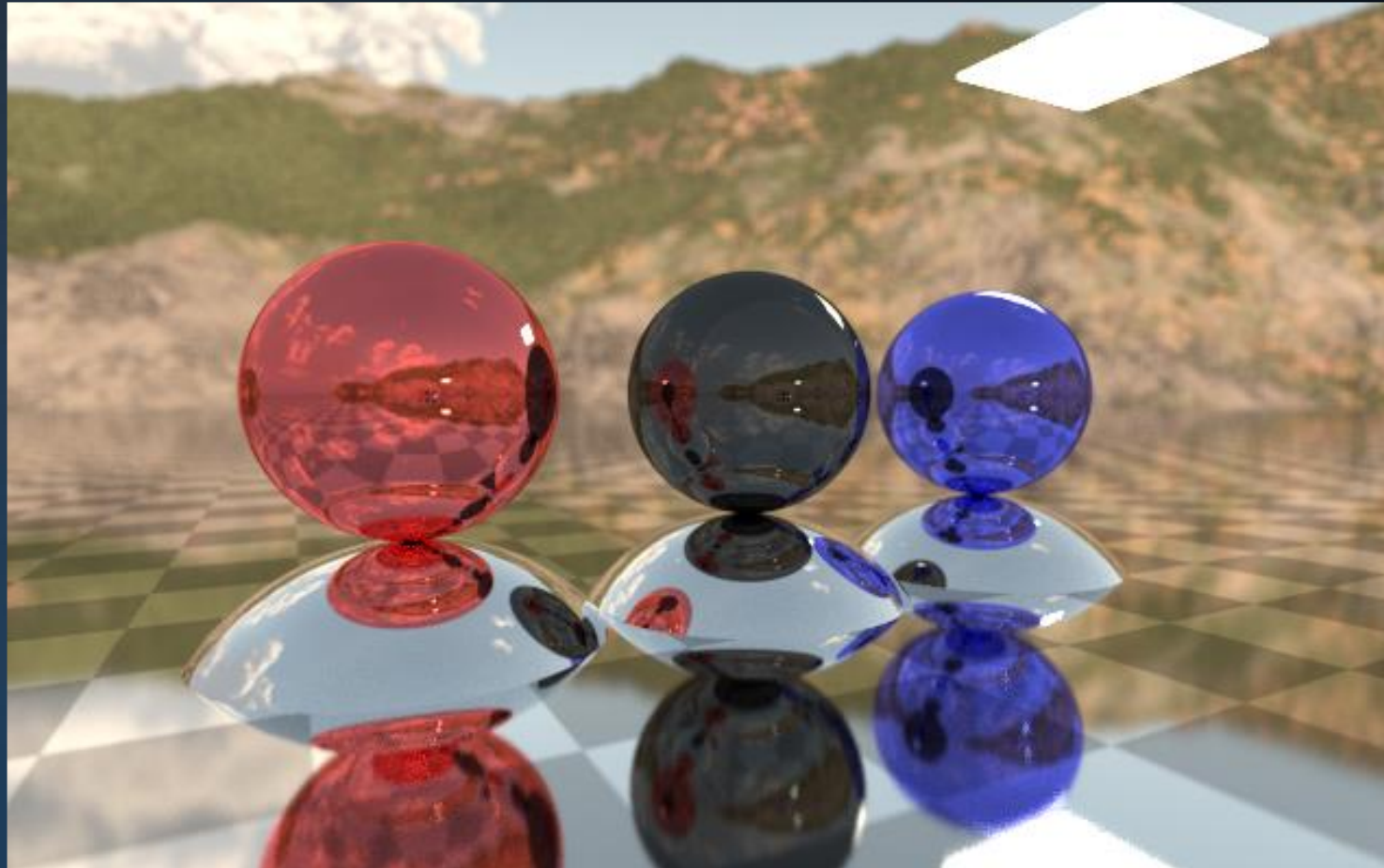
```



Blinn-Phong Microfacet BRDF, $\alpha=500$



Microfacet



Blinn-Phong Microfacet BRDF, $\alpha=50000$

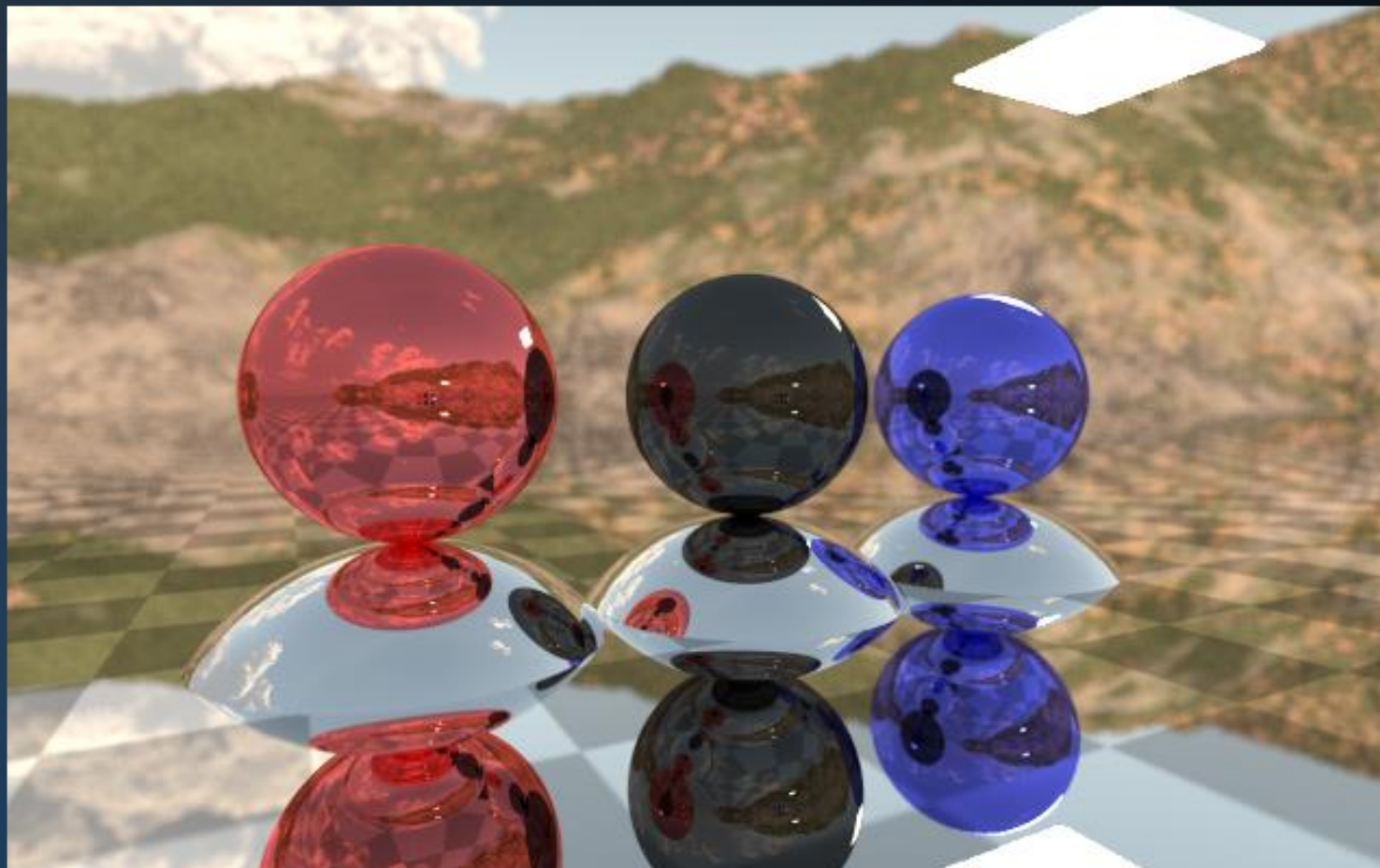


Microfacet

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0.5)
    {
        nt = nt / nc, ddn = ddn * nt;
        r = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        a = nt - nc, b = nt + nc;
        Tr = 1 - (R0 + (1 - R0) * ddn);
        R = (D * nnt + N * (ddn * ddn));
    }
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &light, &N );
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following SurvivalProbability
    (survive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}

```

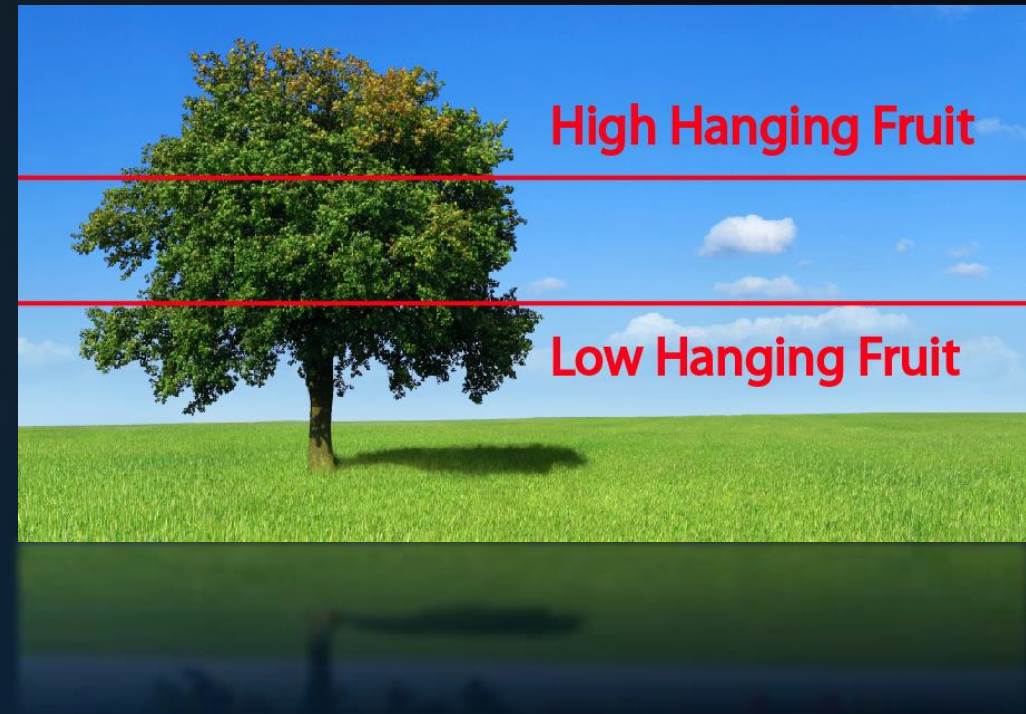


Specular BRDF



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox
- Spots, IES Profiles
- Microfacets



INFOMAGR – Advanced Graphics

Jacco Bikker - November 2021 - February 2022

END of “Various”

next: Assignment 2 deadline, then: Christmas Break

