

```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Tr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &light);
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following
    (survive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```

/INFOMOV/

Optimization & Vectorization

J. Bikker - Sep-Nov 2019 - Lecture 2: "Low Level"

Welcome!





Home



↻ 11

♥ 43



↻ Jonathan Adamczewski Retweeted



Mike Conley @mconley@mastodon.social @mike_conley · 13h



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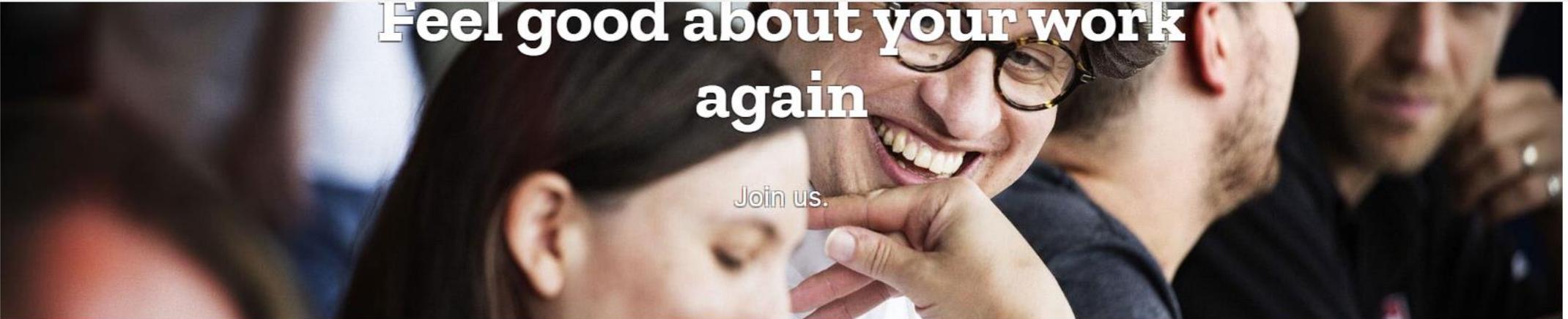
careers.mozilla.org/position/gh/17...

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```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Fr) R = (D * nnt - N * (ddn *
E * diffuse;
= true;
efl + refr)) && (depth < MAXDEPTH)
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refl * E * diffuse;
= true;
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estimation - doing it properly, closely following
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radiance = SampleLight( &rand, I, &L, &light);
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at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
```

/INFOMOV/

Optimization & Vectorization

J. Bikker - Sep-Nov 2019 - Lecture 2: "Low Level"

Welcome!



Previously in INFOMOV...

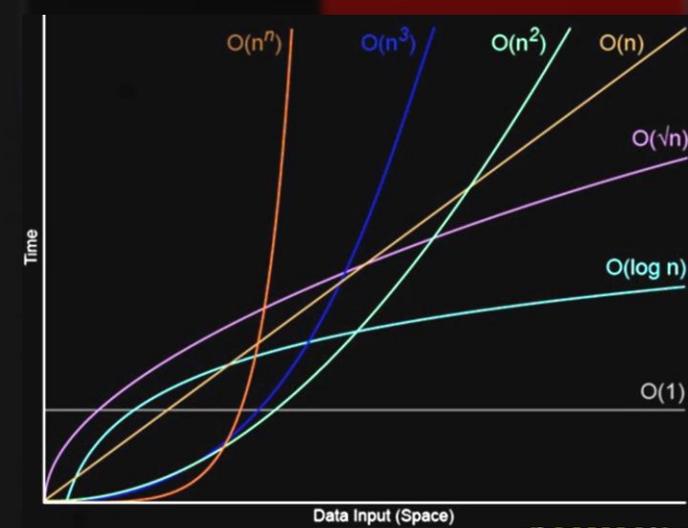
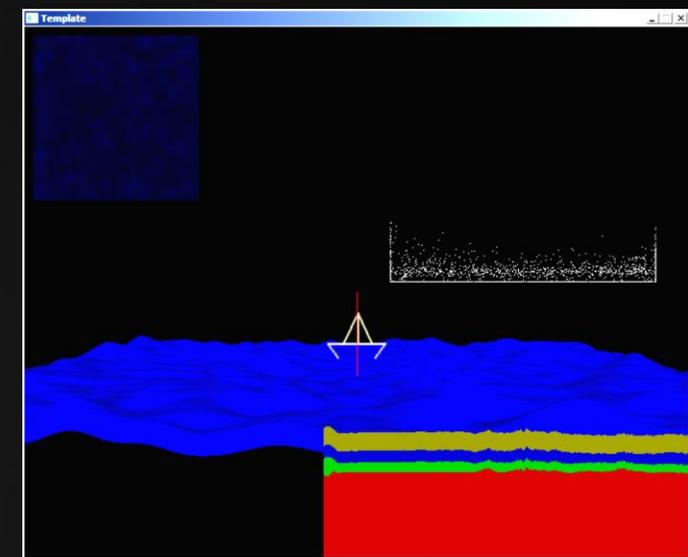
Consistent Approach

(0.) Determine optimization requirements

1. Profile: determine hotspots
2. Analyze hotspots: determine scalability
3. Apply high level optimizations to hotspots
4. Profile again.
5. Parallelize
6. Use GPGPU
7. Profile again.
8. Apply low level optimizations to hotspots
9. Repeat steps 7 and 8 until time runs out
10. Report.

```

...ics
& (depth < MAXDEPTH)
...
c = inside ? 1 : 0;
nt = nt / nc; ddn = ddn * ddn;
cos2t = 1.0f - nnt; rnt = nnt;
D, N );
...
at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) * rnt);
Tr) R = (D * nnt - N * (ddn *
...
E * diffuse;
= true;
...
efl + refr)) && (depth < MAXDEPTH)
D, N );
-refl * E * diffuse;
= true;
MAXDEPTH)
survive = SurvivalProbability( diffuse, r1, r2, &R, Spdf );
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light );
e.x + radiance.y + radiance.z) > 0) && (depth <
...
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
...
random walk - done properly, closely following
ive)
...
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, Spdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
    
```



Today's Agenda:

- The Cost of a Line of Code
- CPU Architecture: Instruction Pipeline
- Data Types and Their Cost
- Rules of Engagement



Instruction Cost

What is the ‘cost’ of a multiply?

```
starttimer();
float x = 0;
for( int i = 0; i < 1000000; i++ ) x *= y;
stoptimer();
```

- Actual measured operations:
 - timer operations;
 - initializing ‘x’ and ‘i’;
 - comparing ‘i’ to 1000000 (x 1000000);
 - increasing ‘i’ (x 1000000);
 - jump instruction to start of loop (x 1000000).
- Compiler outsmarts us!
 - No work at all unless we use x
 - $x += 1000000 * y$

Better solution:

- Create an arbitrary loop
- Measure time with and without the instruction we want to time



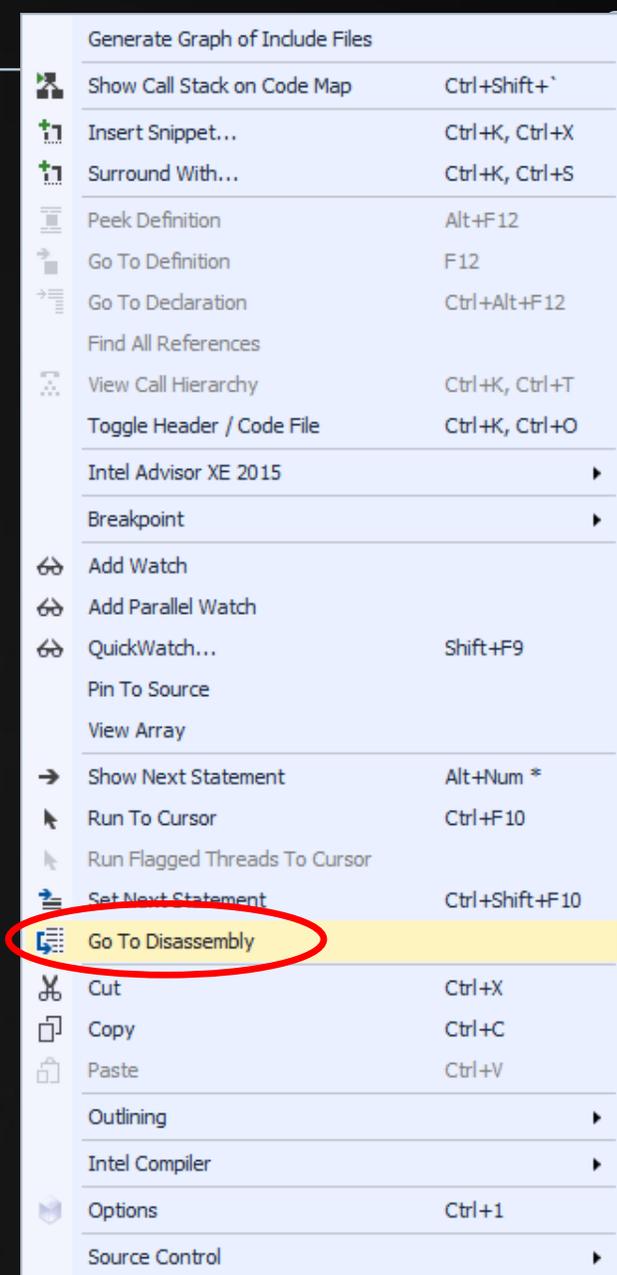
Instruction Cost

What is the ‘cost’ of a multiply?

```

float x = 0, y = 0.1f;
unsigned int i = 0, j = 0x28929227;
for( int k = 0; k < ITERATIONS; k++ )
{
    // ensure we feed our line with fresh data
    x += y, y *= 1.01f;
    // integer operations to free up fp execution units
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
    // operation to be timed
    if (with) x *= y;
    // integer operations to free up fp execution units
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
}
dummy = x + (float)i;

```



Instruction Cost

x86 assembly in 5 minutes

Modern CPUs still run x86 machine code, based on Intel’s 1978 8086 processor. The original processor was 16-bit, and had 8 ‘general purpose’ 16-bit registers*:

AX (‘accumulator register’)	AH, AL (8-bit)	EAX (32-bit)	RAX (64-bit)
BX (‘base register’)	BH, BL	EBX	RBX
CX (‘counter register’)	CH, CL	ECX	RCX
DX (‘data register’)	DH, DL	EDX	RDX
BP (‘base pointer’)		EBP	RBP
SI (‘source index’)		ESI	RSI
DI (‘destination index’)		EDI	RDI
SP (‘stack pointer’)		ESP	RSP
		st0..st7	R8..R15
		XMM0..XMM7	XMM0..XMM15
			YMM0..YMM15
			ZMM0..ZMM31

* More info: <http://www.swansontec.com/sregisters.html>



Instruction Cost

x86 assembly in 5 minutes:

Typical assembler:

loop:

```

mov eax, [0x1008FFA0] // read from address into register
shr eax, 5           // shift eax 5 bits to the right
add eax, edx        // add registers, store in eax
dec ecx             // decrement ecx
jnz loop            // jump if not zero
fld [esi]           // load from address [esi] onto FPU
fld st0             // duplicate top float
faddp               // add top two values, push result

```

More on x86 assembler: <http://www.cs.virginia.edu/~evans/cs216/guides/x86.html>

A bit more on floating point assembler: https://www.cs.uaf.edu/2007/fall/cs301/lecture/11_12_floating_asm.html



Instruction Cost

What is the ‘cost’ of a multiply?

```
float x = 0, y = 0.1f;
unsigned int i = 0, j = 0x28929227;
for( int k = 0; k < ITERATIONS; k++ )
{
    // ...
    x += y, y *= 1.01f;
    // ...
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
    // ...
    if (with) x *= y;
    i += j, j ^= 0x17737352, i >>= 1, j /= 28763;
}
dummy = x + (float)i;
```

```
fldz
xor ecx, ecx
fld dword ptr ds:[405290h]
mov edx, 28929227h
fld dword ptr ds:[40528Ch]
push esi
mov esi, 0C350h = 50000
```

```
add ecx, edx
mov eax, 91D2A969h = 2^46 / 28763 (!!)
```

```
xor edx, 17737352h
shr ecx, 1
mul eax, edx
fld st(1)
faddp st(3), st

mov eax, 91D2A969h
shr edx, 0Eh
add ecx, edx
fmul st(1), st
xor edx, 17737352h
shr ecx, 1
mul eax, edx
shr edx, 0Eh
dec esi
jne tobetimed<0>+1Fh
```



Instruction Cost

What is the ‘cost’ of a multiply?

Observations:

- Compiler reorganizes code
- Compiler cleverly evades division
- Loop counter *decreases*
- Presence of integer instructions affects timing
(to the point where the mul is free)

But also:

- It is really hard to measure the cost of a line of code.

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * 2;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    at a = nt - nc; b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse, i);
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &light);
    e.x + radiance.y + radiance.z) > 0) && (cosThetaOut
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Section 5.4.1
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
    
```



Instruction Cost

What is the ‘cost’ of a single instruction?

Cost is highly dependent on the surrounding instructions, and many other factors. However, there is a ‘cost ranking’:

- << >> *bit shifts*
- + - & | ^ *simple arithmetic, logical operands*
- * *multiplication*
- / *division*
- sqrt
- sin, cos, tan, pow, exp

This ranking is generally true for any processor (including GPUs).

```

ics
& (depth < MAXDEPTH)
= inside ? 1.0f : 0.0f;
nt = nt / nc; ddn = ddn * ddn;
s2t = 1.0f - nnt * nnt;
D, N );
)
at a = nt - nc, b = nt * nc;
at Tr = 1 - (R0 + (1 - R0) * R);
Tr) R = (D * nnt - N * (ddn *
E * diffuse;
= true;
efl + refr)) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;
MAXDEPTH)
survive = SurvivalProbability( diffuse, l
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &light
e.x + radiance.y + radiance.z) > 0) && (survive)
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Section 3.1.2
vive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
    
```



Instruction Cost

AMD Jaguar 2013

Instruction	Operands	Ops	Latency	Reciprocal throughput	Execution pipe	Notes
Arithmetic instructions						
ADD, SUB	r,r/i	1	1	0.5	10/1	
ADD, SUB	r,m	1		1		
ADD, SUB	m,r	1	6	1		
ADC, SRR	r,r/i	1	1	1	10/1	
ADC, S						
ADC, S	Math					
ADC, S	FSQRT		1	35	35	FP1
CMP	FLDPI, etc.		1		1	FP0
CMP	FSIN		4-44	30-139	30-151	FP0, FP1
INC, D	FCOS		11-51	38-93		FP0, FP1
INC, D	FSINCOS		11-76	55-122	55-180	FP0, FP1
AAA	FPTAN		11-45	55-177	55-177	FP0, FP1
AAS	FPATAN		9-75	44-167	44-167	FP0, FP1
DAA	FSCALE		5	27		FP0, FP1
DAS	FEXTRACT		7	9	6	FP0, FP1
AAD	F2XM1		8	32-37		FP0, FP1
AAM	FYL2X		8-51	30-120	30-120	FP0, FP1
MUL, I	FYL2XP1		61	~160	~160	FP0, FP1
MUL, IMUL	r16/m16	3	3	3	10	
MUL, IMUL	r32/m32	2	3	2	10	
MUL, IMUL	r64/m64	2	6	5	10	
IMUL	r16,r16/m16	1	3	1	10	
IMUL	r32,r32/m32	1	3	1	10	
IMUL	r64,r64/m64	1	6	4	10	
IMUL	r16,(r16),i	2	4	1	10	
IMUL	r32,(r32),i	1	3	1	10	
IMUL	r64,(r64),i	1	6	4	10	
DIV	r8/m8	1	11-14	11-14	10	
DIV	r16/m16	2	12-19	12-19	10	
DIV	r32/m32	2	12-27	12-27	10	
DIV	r64/m64	2	12-43	12-43	10	
IDIV	r8/m8	1	11-14	11-14	10	
IDIV	r16/m16	2	12-19	12-19	10	
IDIV	r32/m32	2	12-27	12-27	10	
IDIV	r64/m64	2	12-43	12-43	10	

Note: Two micro-operations can execute simultaneously if they go to different execution pipes



Instruction Cost

```

ics
& (depth < MAXDEPTH)
c = inside ? 1 : 0;
nt = nt / nc; ddn = ddn / ddn;
os2t = 1.0f - nnt * nnt;
D, N );
)
at a = nt - nc; b = nt - nc;
at Tr = 1 - (R0 + (1 - R0) * R);
R = (D * nnt - N * ddn) / (D * nnt - N * ddn);
E * diffuse;
= true;
efl + refr) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;
MAXDEPTH)
survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely follow
if;
radiance = SampleLight( &rand, I, &L, &light;
e.x + radiance.y + radiance.z) > 0) && (depth <
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
andom walk - done properly, closely follow
ive)
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
    
```

Intel Silvermont 2014

Note: This is a low-power processor (ATOM class).

	Operands	μops	Unit	Latency	Reciprocal throughput	Remarks
Arithmetic instructions						
ADD SUB	r,r/i	1	IP0/1	1	1/2	
ADD SUB	r,m	1	IP0/1, Mem		1	
ADD SUB	m,r/i	1	IP0/1, Mem	6	1	
ADC SBB	r,r/i	1	IP0/1	2	2	
ADC SBB	r,m	1			2	
ADC SBB	m,r/i	1		6	2	
CMP	r,r/i	1	IP0/1	1	1/2	
CMP	m,r/i	1			1	
INC DEC	r	1	IP0/1	1	1/2	latency to flag?
NEG NOT	r	1	IP0/1	1	1/2	
Math						
INC DEC	FSCALE			27		66
AAA	FXTRACT			15	20	20
AAS	FSQRT			1	13-40	13-40
DAA	FSIN FCOS			18	40-170	40-170
DAS	FSINCOS			110	40-170	
AAD	F2XM1			9	39-90	
AAM	FYL2X			34	80-140	
MUL IMUL	FYL2XP1			61	154	
MUL IMUL	FPTAN			101	45-200	
MUL IMUL	FPATAN			63	85-190	
IMUL	r16,r16	2	IP0	4	4	
IMUL	r32,r32	1	IP0	3	1	
IMUL	r64,r64	1	IP0	5	2	
IMUL	r16,r16,i	2	IP0	4	4	
IMUL	r32,r32,i	1	IP0	3	1	
IMUL	r64,r64,i	1	IP0	5	2	
MUL IMUL	m8	3	IP0			
MUL IMUL	m16	5	IP0			
MUL IMUL	m32	4	IP0			
MUL IMUL	m64	4	IP0	14		
DIV	r/m8	9	IP0, FP0	24	19	
DIV	r/m16	12	IP0, FP0	25-29	19-23	
DIV	r/m32	12	IP0, FP0	25-39	19-31	
DIV	r/m 64	23	IP0, FP0	34-94	25-94	
IDIV	r/m8	26	IP0, FP0	24-35	25	
IDIV	r/m16	29	IP0, FP0	37-41	30-32	
IDIV	r/m32	29	IP0, FP0	29-46	29-38	
IDIV	r/m64	44	IP0, FP0	47-107	47-107	



Instruction Cost

What is the ‘cost’ of a single instruction?

The cost of a single instruction depends on a number of factors:

- The arithmetic complexity (sqrt > add);
- Whether the operands are in register or memory;
- The size of the operand (16 / 64 bit is often slightly slower);
- Whether we need the answer immediately or not (latency);
- Whether we work on signed or unsigned integers (DIV/IDIV).

On top of that, certain instructions can be executed simultaneously.



Today's Agenda:

- The Cost of a Line of Code
- CPU Architecture: Instruction Pipeline
- Data Types and Their Cost
- Rules of Engagement



Pipeline

CPU Instruction Pipeline

Instruction execution is typically divided in four phases:

- | | |
|--------------|--|
| 1. Fetch | Get the instruction from RAM |
| 2. Decode | The byte code is decoded |
| 3. Execute | The instruction is executed |
| 4. Writeback | The results are written to RAM/registers |



$CPI = 4$

```

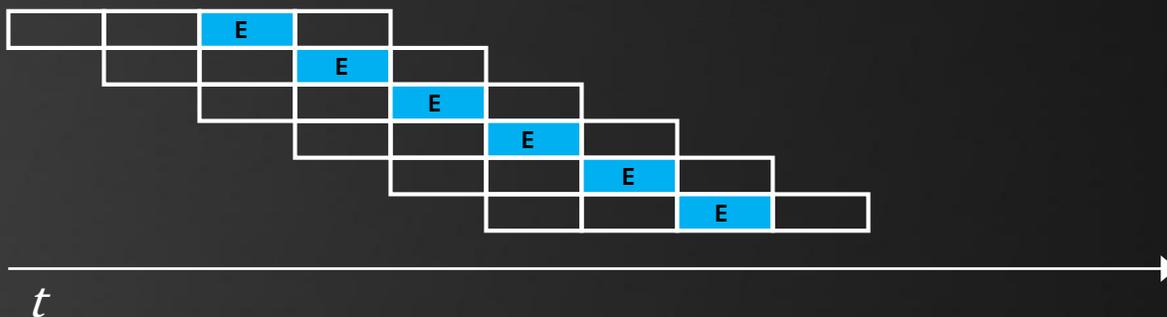
fldz
xor ecx, ecx
fld dword ptr ds:[405290h]
mov edx, 28929227h
fld dword ptr ds:[40528Ch]
push esi
mov esi, 0C350h
add ecx, edx
mov eax, 91D2A969h
xor edx, 17737352h
shr ecx, 1
mul eax, edx
fld st(1)
faddp st(3), st
mov eax, 91D2A969h
shr edx, 0Eh
add ecx, edx
fmul st(1),st
xor edx, 17737352h
shr ecx, 1
mul eax, edx
shr edx, 0Eh
dec esi
jne tobetimed<0>+1Fh
    
```



Pipeline

CPU Instruction Pipeline

For each of the stages, different parts of the CPU are active.
 To use its transistors more efficiently, a modern processor overlaps these phases in a *pipeline*.



At the same clock speed, we get four times the throughput (CPI = IPC = 1).

```

...ics
& (depth < MAXDEPTH)
...
= inside ? 1 : 0;
nt = nt / nc; ddn = ddn / nc;
ps2t = 1.0f - nnt * ddn;
D, N );
...
)
...
at a = nt - nc; b = nt - nc;
at Tr = 1 - (R0 + (1 - R0) * nnt);
Tr) R = (D * nnt - N * (ddn * nnt));
...
E * diffuse;
= true;
...
efl + refr) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;
...
MAXDEPTH)
survive = SurvivalProbability( diffuse, l);
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light);
e.x + radiance.y + radiance.z) > 0) && (survive)
...
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psum;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
...
random walk - done properly, closely following
ive)
...
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
    
```



Pipeline

CPU Instruction Pipeline

Maximum clockspeed is determined by the most complex of the four stages. For higher clockspeeds, it is advantageous to increase the number of stages (thereby reducing the complexity of each individual stage).



Stages

7	PowerPC G4e
8	Cortex-A9
10	Athlon
12	Pentium Pro/II/III, Athlon 64
14	Core 2, Apple A7/A8
14/19	Core i2/i3 Sandy Bridge
16	PowerPC G5, Core i*1 Nehalem
18	Bulldozer, Steamroller
20	Pentium 4
31	Pentium 4E Prescott

Obviously, ‘execution’ of different instructions requires different functionality.

Superpipelining allows higher clockspeeds and thus higher throughput, but it also increases the latency of individual instructions.



Pipeline

CPU Instruction Pipeline

Different execution units for different (classes of) instructions:



Here, one execution unit handles floats;
one handles integer;
one handles memory operations.

Since the execution logic is typically the most complex part, we might just as well duplicate the other parts:



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn / nc;
        ps2t = 1.0f - nnt * ddn;
        D, N );
    }
}

at a = nt - nc; b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
E * diffuse;
= true;
efl + refr)) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;
MAXDEPTH)
survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &light;
e.x + radiance.y + radiance.z) > 0) && (rand
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following &rand;
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
    
```



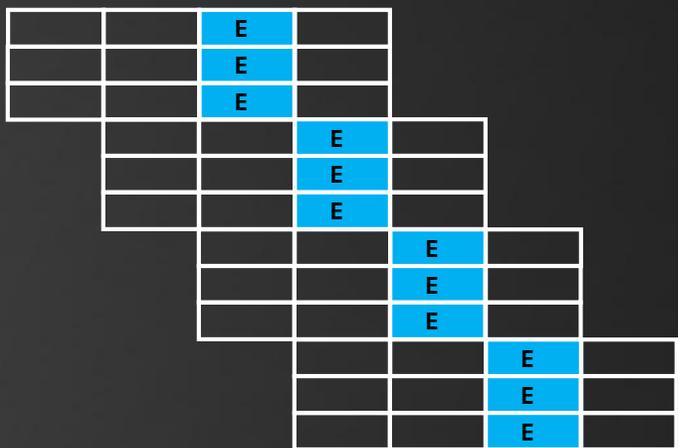
Pipeline

CPU Instruction Pipeline

This leads to the *superscalar* processor, which can execute multiple instructions in the same clock cycle, assuming not all instructions require the same execution logic.

```

ics
& (depth < MAXDEPTH)
c = inside ? 1 : 0;
nt = nt / nc; ddn = ddn + c;
ps2t = 1.0f - nnt * ddn;
D, N );
)
at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) * c);
Tr) R = (D * nnt - N * (ddn * c));
E * diffuse;
= true;
efl + refr) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;
MAXDEPTH)
survive = SurvivalProbability( diffuse, l);
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light);
e.x + radiance.y + radiance.z) > 0) && (depth <
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * radiance;
andom walk - done properly, closely following
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
urvive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
    
```



IPC = 3 (or: ILP = 3)



Pipeline

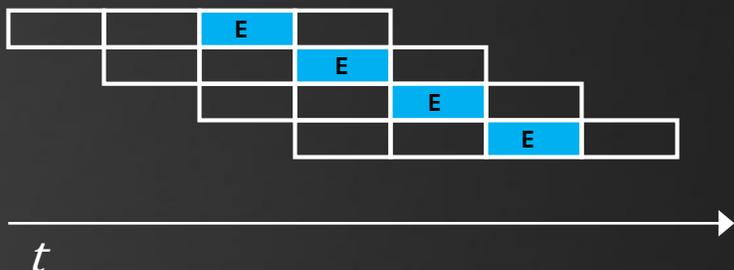
CPU Instruction Pipeline

Using a pipeline has consequences.
Consider the following situation:

```

...
    & (depth < MAXDEPTH)
...
    c = inside ? 1.0f : 0.0f;
    nt = nt / nc; ddn = ddn * ddn;
    cos2t = 1.0f - nnt * ddn;
    D, N );
...
    at a = nt - nc; b = nt * nc;
    at Tr = 1 - (R0 + (1 - R0) * c);
    Tr) R = (D * nnt - N * (ddn *
...
    E * diffuse;
    = true;
...
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
...
MAXDEPTH)
survive = SurvivalProbability( diffuse, r1, r2, &R, $pdf );
estimation - doing it properly, closely following
df;
radiance = SampleLight( &rand, I, &L, &light );
e.x + radiance.y + radiance.z) > 0) && (cosThetaOut > 0)
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
...
random walk - done properly, closely following
(ive)
...
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, $pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



$a = b * c;$
 $d = a + 1;$

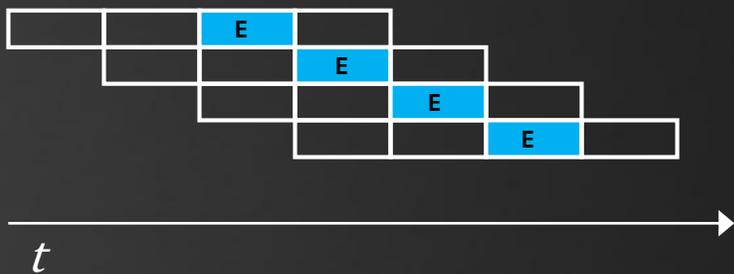
Here, the second instruction needs the result of the first, which is available one clock tick too late. As a consequence, the pipeline stalls briefly.



Pipeline

CPU Instruction Pipeline

Using a pipeline has consequences.
Consider the following situation:



`a = b * c;`
`jump if a is not zero`

In this scenario, a conditional jump makes it hard for the CPU to determine what to feed into the pipeline after the jump.

```

...
    & (depth < MAXDEPTH)
...
    c = inside ? 1.0f : 0.0f;
    nt = nt / nc; ddn = ddn / nd;
    cos2t = 1.0f - nnt * nnt;
    D, N );
...
    at a = nt - nc; b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * c);
    R = (D * nnt - N * (ddn *
...
    E * diffuse;
    = true;
...
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
...
MAXDEPTH)
survive = SurvivalProbability( diffuse, l,
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light
e.x + radiance.y + radiance.z) > 0) && (cos
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
...
random walk - done properly, closely following 3D random walk
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



Pipeline

CPU Instruction Pipeline - Digest

For a more elaborate explanation of the pipeline, see this document:

<http://www.lighterra.com/papers/modernmicroprocessors>

Or check this very detailed study of the Nehalem architecture:

The Architecture of the Nehalem Processor and Nehalem-EP SMP Platforms,
Thomadakis, 2011.

For now:

- A compiler reorganizes code to prevent latencies
- Feeding mixed code provides the compiler with sufficient opportunities for shuffling
- Branching issues need to be prevented manually



Today's Agenda:

- The Cost of a Line of Code
- CPU Architecture: Instruction Pipeline
- Data Types and Their Cost
- Rules of Engagement



Data Types

Data types in C++

int
unsigned int

Red = u4 & (255 << 16);
Green = u4 & (255 << 8);
Blue = u4 & 255;



Size: 32 bit (4 bytes)

Access:

union { unsigned int u4; int s4; char s[4]; };

unsigned char v = 100;

s[1] = v;

u4 = (a4 ^ (255 << 8)) | (v << 8);

u4 ^= 1 << 31;

Altering sign bit of s4:
(note: -1 = 0xffffffff)



Data Types

Data types in C++

float



Size: 32 bit (4 bytes)

Exponent: 8 bit; -127 ... 128

Mantissa: 23 bit; 0 ... $2^{23} - 1$

Value: $\text{sign} * \text{mantissa} * 2^{\text{exponent}}$

Exercise: write a function that replaces array $a = \{ 0.5, 0.25, 0.125, 0.0625, \dots \}$.



Data Types

Data types in C++

double	64 bit (8 bytes)
char, unsigned char	8 bit
short, unsigned short	16 bit
LONG	32 bit (same as int)
LONG LONG, __int64	64 bit
bool	8 bit (!)

Padding*:

```
struct Test
{
    unsigned int u;
    bool flag;
};
// sizeof( Test ) is 8
```

```
struct Test2
{
    double d;
    bool flag;
};
// sizeof( Test2 ) is 16
```

*: More on <http://www.catb.org/esr/structure-packing>



Data Types

Data types in C++ - Conversions

Explicit:

```
float fpi = 3.141593;
int pi = (int)(1024.0f * fpi);
```

Implicit:

```
struct Color { unsigned char a, r, g, b; };
Color bitmap[640 * 480];
for( int i = 0; i < 640 * 480; i++ )
{
    bitmap[i].r *= 0.5f;
    bitmap[i].g *= 0.5f;
    bitmap[i].b *= 0.5f;
}
```

```
// bitmap[i].r *= 0.5f;
movzx    eax,byte ptr [ecx-1]
mov      dword ptr [ebp-4],eax
fild     dword ptr [ebp-4]
fstcw    word ptr [ebp-2]
movzx    eax,word ptr [ebp-2]
or       eax,0C00h
mov      dword ptr [ebp-8],eax
fmul     st,st(1)
fldcw    word ptr [ebp-8]
fistp    dword ptr [ebp-8]
movzx    eax,byte ptr [ebp-8]
mov      byte ptr [ecx-1],al
```



Data Types

Data types in C++ - Conversions

Explicit:

```
float fpi = 3.141593;
int pi = (int)(1024.0f * fpi);
```

Avoiding conversion:

```
struct Color { unsigned char a, r, g, b; };
Color bitmap[640 * 480];
for( int i = 0; i < 640 * 480; i++ )
```

```
    bitmap[i].r >>= 1;
    bitmap[i].g >>= 1;
    bitmap[i].b >>= 1;
```

```
// bitmap[i].r >>= 1;
shr          byte ptr [eax-1],1
// bitmap[i].g >>= 1;
shr          byte ptr [eax],1
// bitmap[i].b >>= 1;
shr          byte ptr [eax+1],1
```



Data Types

Data types in C++ - Conversions

Explicit:

```
float fpi = 3.141593;
int pi = (int)(1024.0f * fpi);
```

Avoiding conversion (2):

```
struct Color { union { struct { unsigned char a, r, g, b; }; int argb; }; };
Color bitmap[640 * 480];
for( int i = 0; i < 640 * 480; i++ )
    bitmap[i].argb = (bitmap[i].argb >> 1) & 0x7f7f7f;
```



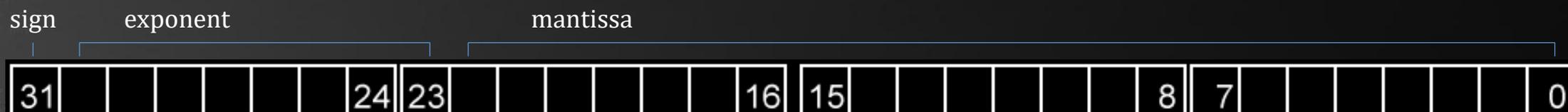
Data Types

Data types in C++ - Free interpretation

Trick: Cheaper float comparison

```

...
    & (depth < MAXDEPTH)
...
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn / nc;
        cos2t = 1.0f - nnt;
        D, N );
    }
...
    at a = nt - nc, b =
    at Tr = 1 - (R0 + 1)
    Tr) R = (D * nnt -
...
    E * diffuse;
    = true;
...
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
...
MAXDEPTH)
survive = SurvivalProbability( diffuse, p
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &light
e.x + radiance.y + radiance.z) > 0) && (cos
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
...
random walk - done properly, closely following S&eacute;e
vive)
...
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, $pdf
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;
    
```



```
union { float v1; unsigned int u1; };
```

```
union { float v2; unsigned int u2; };
```

```
bool smaller = (v1 < v2);
```

```
bool smaller = (u1 < u2); // same result, if signs of v1 and v2 are equal.
```



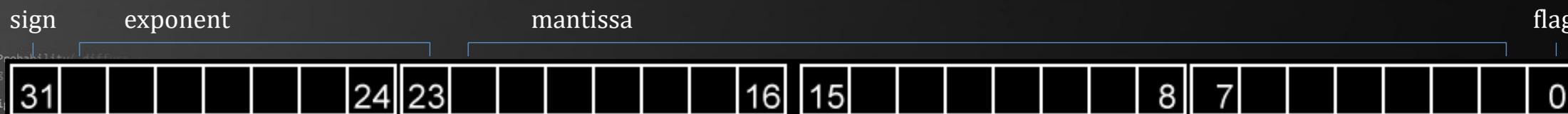
Data Types

Data types in C++ - Rolling your own

HDR color storage



Storing a bit flag in a floating point value



Today's Agenda:

- The Cost of a Line of Code
- CPU Architecture: Instruction Pipeline
- Data Types and Their Cost
- Rules of Engagement



Rules of Engagement

Common Opportunities in Low-level Optimization

RULE 1: Avoid Costly Operations

- Replace multiplications by bitshifts, when possible
- Replace divisions by (reciprocal) multiplications
- Avoid sin, cos, sqrt

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * 2;
        ns2t = 1.0f - nnt * nnt;
        D, N );
    }
}

at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
at R = (D * nnt - N * (ddn
E * diffuse;
= true;

efl + refr)) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;

MAXDEPTH)
survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light;
e.x + radiance.y + radiance.z) > 0) && (cosThetaOut > 0)
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following
vive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



Rules of Engagement

Common Opportunities in Low-level Optimization

RULE 2: Precalculate

- Reuse (partial) results
- Adapt previous results (interpolation, reprojection, ...)
- Loop hoisting
- Lookup tables

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * r);
        (Tr) R = (D * nnt - N * (ddn *
    }
    E * diffuse;
    = true;
    -
    refl + refr) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
}
MAXDEPTH)
{
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &light);
    e.x + radiance.y + radiance.z) > 0) && (cosThetaOut > 0)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
}
random walk - done properly, closely following
(ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



Rules of Engagement

Common Opportunities in Low-level Optimization

RULE 3: Pick the Right Data Type

- Avoid byte, short, double
- Use each data type as a 32/64 bit container that can be used at will
- Avoid conversions, especially to/from float
- Blend integer and float computations
- Combine calculations on small data using larger data

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
}

at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
at R = (D * nnt - N * (ddn
E * diffuse;
= true;

efl + refr)) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;

MAXDEPTH)
survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light;
e.x + radiance.y + radiance.z) > 0) && (cosThetaOut > 0)
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



Rules of Engagement

Common Opportunities in Low-level Optimization

RULE 4: Avoid Conditional Branches

- if, while, ?, MIN/MAX
- Try to split loops with conditional paths into multiple unconditional loops
- Use lookup tables to prevent conditional code
- Use loop unrolling
- If all else fails: make conditional branches predictable

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * 0.5;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
}

at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) * r);
Tr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
}

efl + refr)) && (depth < MAXDEPTH)
{
    D, N );
    refl * E * diffuse;
    = true;
}

MAXDEPTH)
{
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &light);
    e.x + radiance.y + radiance.z) > 0) && (cosThetaOut > 0)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
}

random walk - done properly, closely following
( survive)
{
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}

```



Rules of Engagement

Common Opportunities in Low-level Optimization

RULE 5: Early Out

```

...ics
& (depth < MAXDEPTH)
...
nt = nt / nc; ddn = ddn * ddn;
s2t = 1.0f - nnt * ddn;
D, N );
)
at a = nt - nc, b = nt * n;
at Tr = 1 - (R0 + (1 - R0) *
Fr) R = (D * nnt - N * (Ddn
E * diffuse;
= true;
efl + refr)) && (depth < MAXDEPTH) {
D, N );
refl * E * diffuse;
= true;
MAXDEPTH)
survive = SurvivalProbability( diffuse, r1, r2, &R, $pdf );
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, $L, $align, $color, $emissive, $x + radiance.y + radiance.z ) > 0; } && (depth <
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, $pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```

char a[] = “abcdefghijklmopqrstuvwxyz”;
char c = ‘p’;
int position = -1;
for (**int** t = 0; t < strlen(a); t++)
 if (a[t] == c)
 position = t;

```

char a[] = “abcdefghijklmopqrstuvwxyz”;  

char c = ‘p’;  

int position = -1, len = strlen( a );  

for ( int t = 0; t < len; t++ )  

{  

    if (a[t] == c)  

    {  

        position = t;  

        break;  

    }  

}

```



Rules of Engagement

Common Opportunities in Low-level Optimization

RULE 6: Use the Power of Two

- A multiplication / division by a power of two is a (cheap) bitshift
- A 2D array lookup is a multiplication too – make ‘width’ a power of 2
- Dividing a circle in 256 or 512 works just as well as 360 (but it’s faster)
- Bitmasking (for free modulo) requires powers of 2

1-2-4-8-16-32-64-128-256-512-1024-2048-4096-8192-16384-32768-65536

Be fluent with powers of 2 (up to 2^{16});

learn to go back and forth for these: $2^9 = 512 = 2^9$.

Practice counting from 0..31 on one hand in binary.

```

...ics
& (depth < MAXDEPTH)

...
c = inside ? 1.0f : 0.0f;
nt = nt / nc; ddn = ddn * ddn;
...s2t = 1.0f - nnt * nnt;
D, N );
0)

...
at a = nt - nc; b = nt * nc;
at Tr = 1 - (R0 + (1 - R0) * c);
Tr) R = (D * nnt - N * (ddn *
E * diffuse;
= true;

...
efl + refr)) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;

MAXDEPTH)
survive = SurvivalProbability( diffuse, r,
estimation - doing it properly, closely following
df;
radiance = SampleLight( &rand, I, &L, &light
e.x + radiance.y + radiance.z) > 0) && (survive)
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Section 1.6.2
ive)

...
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



Rules of Engagement

Common Opportunities in Low-level Optimization

RULE 7: Do Things Simultaneously

- Use those cores
- An integer holds four bytes; use these for instruction level parallelism
- More on this later.

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * 2;
        ps2t = 1.0f - nnt * nnt;
        D, N );
    }
}

at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
);

E * diffuse;
= true;

efl + refr) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;

MAXDEPTH)
survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following
if;
radiance = SampleLight( &rand, I, &L, &light;
e.x + radiance.y + radiance.z) > 0) && (depth <
w = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf;
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```



Rules of Engagement

Common Opportunities in Low-level Optimization

1. Avoid Costly Operations
2. Precalculate
3. Pick the Right Data Type
4. Avoid Conditional Branches
5. Early Out
6. Use the Power of Two
7. Do Things Simultaneously

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nc;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * r);
    Tr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &light);
    e.x + radiance.y + radiance.z) > 0) && (cosThetaOut > 0)
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Section 2.1.1
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
  
```



Today's Agenda:

- The Cost of a Line of Code
- CPU Architecture: Instruction Pipeline
- Data Types and Their Cost
- Rules of Engagement



Practice

Get (from the website) project glassball.zip

Using low-level optimization, speed up this application.

1. Avoid Costly Operations
2. Precalculate
3. Pick the Right Data Type
4. Avoid Conditional Branches
5. Early Out
6. Use the Power of Two

Make sure functionality remains intact.

Target: a 10x speedup (this should be easy).



/INFOMOV/

END of “Low Level”

next lecture: “caching (1)”

```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }

    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * r);
    (Fr) R = (D * nnt - N * (ddn * ddn));

    E * diffuse;
    = true;

    refl + refr) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;

    MAXDEPTH)

    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &light);
    e.x + radiance.y + radiance.z) > 0) && (abs(radiance.x) +
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance

    random walk - done properly, closely following
    (survive)

    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```

